## **Problem Set 4**

The data set wagedata.dta has data for 16,492 younger workers from an administrative data set, with a daily wage in every year from 1995 to 2005. The sample is created by the program wsample2.sas as follows:

- 1) between age 22 and 38 in each year
- 2) always had at least 1 full time job in each calendar year, for which the daily wage is measured (daily wage = total earnings/days worked)
- 3) not in training in any year; not working in a subsidized job; not part-time
- 4) no gap in employment history (ie, a wage every year)
- 5) education in 3 categories: basic high school only; apprenticeship, university

## The variables in the file are as follows:

```
startage = age in 1995 (age in 2005=startage+10)
Female = 1 if female, 0 otherwise
starttenure = tenure on job in 1995 (# years)
newid = id variable
```

```
w1=log wage in 1995 ...
w11 = log wage in 2005
```

```
c1=dummy if wage in 1995 is censored ...
c11 = dummy if log wage in 2005 is censored
```

j1=counter for "job number" in 1995 (starting from 1<sup>st</sup> year person is observed working) ranges from 1+

j2= counter for job number in 1996 (if person is on same job as in 1995, j2=j1, else j2=j1+1

j11= counter for job number in 2005 (values 1,2,3,...14)

## Schooling

A person's education is measured every year: I take the highest value they ever attain. There are 3 values:

11 = finished basic high school, nothing more

13 = finished apprenticeship

18 = finished undergrad/masters level

For this problem set you will use data on w1-w11, and the other variables, to estimate a variance components model for wages. You will need to use Matlab or Gauss or MATA. You will also want to read the appendix to Abowd-Card, ECA, 1989, and take a look at the first half of the paper for a general overview.

Look at program wagecov3.sas This is sas code that creates residual wages **for men** in each year for each person (regressing on schooling and cubic in age). These are called r1-r11. It outputs the 66 independent ("LTR" = lower triangular) elements from the covariance matrix of r1-r11, as well as the 66 x 66 matrix of sampling variances/covariances of the second moments. These are placed in 2 .txt files called rescov-male.txt and vrescov-male.txt. You can replicate this is STATA if you are a stata user, or use the sas code.

The gauss program simple.prg inputs these data and fits a very simple model with

$$r_{it} = \omega_i + u_{it}$$

where  $var[\omega_i]$  is a constant,  $var[u_{it}]$  is a constant, and  $cov[u_{it}, u_{is}] = \rho^{|t-s|} var[u_{it}]$ . It has the coding for the goodness of fit statistic (see the class notes), etc. You can replicate this code in Matlab, or use the Gauss program.

a) Develop a model for the variance-covariance terms that includes a permanent person effect, a first-order autoregressive transitory error, and a pure measurement error that is uncorrelated over time. I.e., assume:

$$r_{it} = \omega_i + u_{it} + e_{it}$$

where  $e_{it}$  is iid. Fit the model by non-linear least squares (or equally weighted minimum distance), using a variation of simple.prg. Compare the fits and parameters for women versus men.

b) Try modifying your model by assuming that

$$r_{it} = \psi_t (\omega_i + u_{it}) + e_{it}$$

where  $\psi_t$  is allowed to vary over time. How do the estimates of the  $\psi_t$  terms change over time? Are they different for men and women?

NOTE: in simple.prg I have a useful subroutine "ltr":

Itr(i,j) maps from the J\*J symmetric matrix to the corresponding element of the vecLTR of this matrix. So the i,j element of the covariance matrix C is stored in the Irt(i,j) row of the vecLTR (C).