Evaluating Public Programs with Close Substitutes: The Case of Head Start

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- Many government programs provide services that can also be obtained via markets or other public organizations
 - "Substitution bias" in experiments (Heckman et al., 2000)
- Possible causal estimands of interest:
 - Effect of a program offer (ITT)
 - Effect relative to participants' next best alternative (LATE)
 - Effect relative to no program
- Which of these (if any) to use in policy evaluation?

The Case of Head Start

- Head Start (HS): Publicly-funded preschool for disadvantaged children. Largest public early childhood program in the US
- Many close public and private substitutes (state pre-K, private preschool)
- Literature evaluating impact of HS on test scores finds mixed results:
 - Observational studies based on sibling designs find large persistent impacts (Currie and Thomas, 1995; Garces et al., 2002; Deming, 2009)
 - Experimental evaluation based on lotteries, the Head Start Impact Study (HSIS), finds small impacts that fade out (Puma et al, 2010; Barnett, 2011)

Media Reaction



Revisit HSIS results in view of wide availability of substitute preschools

Key facts:

- $\bullet~1/3$ of HSIS control group attended other preschools
 - Fraction increased after first year of experiment
- Most of these preschools were publicly funded

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- Toy model: focus on a single benefit (earnings) and compare to impact on government budget
 - When market for preschool substitutes clears:
 - IV-LATE is policy-relevant benefit
 - But costs need to be adjusted for "fiscal externalities"
 - When substitutes are rationed: LATE is not enough

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 - IV-LATE is policy-relevant benefit
 - But costs need to be adjusted for "fiscal externalities"
 - When substitutes are rationed: LATE is not enough
- Empirical analysis:
 - $\bullet\,$ PDV projected earnings impacts $\sim\,$ HS enrollment costs
 - But accounting for public savings \Rightarrow Benefits > Costs
 - With rationing: Benefits \gg Costs

Technology vs Market Structure

- Develop selection model parameterizing heterogeneity in effects of Head Start vs home care / other preschools
 - Identify using interactions of experimental status with household and site characteristics
 - Decompose LATE into "subLATE's" with respect to particular alternatives
 - Predict effects of changing selection into the program

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- Develop selection model parameterizing heterogeneity in effects of Head Start vs home care / other preschools
 - Identify using interactions of experimental status with household and site characteristics
 - Decompose LATE into "subLATE's" with respect to particular alternatives
 - Predict effects of changing selection into the program
- Findings:
 - Head Start and other preschools have roughly equivalent average impacts on test scores relative to home care
 - "Reverse-Roy" selection: those with lowest gains most likely to participate
 - Rate of return can be raised further by drawing in new populations

Outline

- 1 The HSIS Experiment
 - Experimental Impacts
 - Characterizing Compliers

2 Model

- Scaling up randomly
- Reforms to program features
- 3 Cost-Benefit Estimates
- 4 Selection Model
 - Identification
 - Estimation / Inference

5 Results



Background on Head Start

- Enrolls one million 3- and 4- year-olds at a cost of \$8 billion per year
- Grants awarded to public, private non-profit, and for-profit organizations
- Eligibility: 100% of FPL, with some exceptions
- Competing center-based care programs are ubiquitous:
 - State preschool programs
 - TANF
 - Child Care Development Fund (CCDF)

The Head Start Impact Study

- 1998 Head Start reauthorization included a mandate to determine program's effects: resulted in the HSIS, a large-scale randomized trial
- Stratified random sample of Head Start centers
 - Baseline randomization in Fall 2002
 - Two age cohorts: 55% age 3, 45% age 4
- We focus on summary index of cognitive outcomes based upon average of PPVT and WJ III test scores
 - Normed to have mean zero, std dev. one in control group each year

	By offe	er status	E	By preschool choic	ce
	Non-offered mean	Offer differential	Head Start	Other centers	No preschoo
Variable	(1)	(2)	(3)	(4)	(5)
Black	0.298	0.010	0.317	0.353	0.250
		(0.010)			
Hispanic	0.369	0.007	0.380	0.354	0.373
		(0.010)			
Mother is high school dropout	0.397	-0.029	0.377	0.322	0.426
		(0.017)			
Mother attended some college	0.281	0.017	0.293	0.342	0.253
		(0.016)			
Test language is not English	0.239	0.016	0.268	0.223	0.231
		(0.011)			
Income (fraction of FPL)*	0.896	0.000	0.892	0.983	0.851
		(0.024)			
Age 4 cohort	0.451	-0.003	0.426	0.567	0.413
		(0.012)			
Baseline test scores	0.012	-0.009	-0.001	0.106	-0.040
Joint p-value		0.268			
1	N 35	571	2043	598	930

Table 1: Descriptive Statistics

*Household income is missing for 19 percent of observations. Missing values are excluded in statistics for income.

			Intent-to-treat		Instrumental variables		
		3-year-olds (1)	4-year-olds (2)	Pooled (3)	3-year-olds (4)	4-year-olds (5)	Pooled (6)
Year 1	N	0.194 (0.029) 1970	0.141 (0.029) 1601	0.168 (0.021) 3571	0.278 (0.041) 1970	0.213 (0.044) 1601	0.247 (0.031) 3571
Year 2	N	0.087 (0.029) 1760	-0.015 (0.037) 1416	0.046 (0.024) 3176	0.245 (0.080) 1760	-0.022 (0.054) 1416	0.093 (0.049) 3176

Table 2: Experimental Impacts on Test Scores

			Offered	-		Not offered		
		Head Start	Other centers	No preschool	Head Start	Other centers	No preschool	complier share
Cohort	Time period	(1)	(2)	(3)	(4)	(5)	(6)	(7)
3-year-olds	Year 1	0.851	0.058	0.092	0.147	0.256	0.597	0.282
	Year 2	0.657	0.262	0.081	0.494	0.379	0.127	0.719
4-year-olds	Year 1	0.787	0.114	0.099	0.122	0.386	0.492	0.410

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		(0.029)	(0.029)	(0.021)	(0.041)	(0.044)	(0.031
	Ν	1970	1601	3571	1970	1601	3571
Year 2		0.087	-0.015	0.046	0.245	-0.022	0.093
		(0.029)	(0.037)	(0.024)	(0.080)	(0.054)	(0.049
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		(0.031)	(0.040)	(0.025)	(0.085)	(0.060)	(0.050)	
	Ν	1659	1336	2995	1659	1336	2995	
Year 4		0.038	-	-	0.110	-	-	
		(0.034)			(0.098)			
	Ν	1599			1599			

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Year 4	N	0.038 (0.034) 1599] -	-	0.110 (0.098) 1599	-	-	

Table 2: Experimental Impacts on Test Scores



- How does the presence of substitute preschools affect interpretation of the IV results?
- Care environment abbreviations:
 - h Head Start,
 - c other preschool center
 - *n* no preschool (home care)
- D_i(z): {0,1} → {h, c, n} gives child i's care environment as a function of experimental offer status z
- Revealed preference restriction on behavioral response to offer:

$$D_i(1) \neq D_i(0) \implies D_i(1) = h$$

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Five "compliance groups" of children:

• c-compliers:
$$D_i(1) = h$$
, $D_i(0) = c$

② *n*-compliers:
$$D_i(1) = h$$
, $D_i(0) = h$

3 *c*-never takers:
$$D_i(1) = D_i(0) = c$$

• *n*-never takers: $D_i(1) = D_i(0) = n$

$${igsir 0}\,$$
 always takers: $D_i(1)=D_i(0)=h$

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$$= S_c LATE_{ch} + (1 - S_c) LATE_{nh}$$

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• Weighting term *S_c* is the share of compliers drawn from other preschools:

$$S_c = \frac{P(D_i(1) = h, D_i(0) = c)}{P(D_i(1) = h, D_i(0) \neq h)}$$

Wald estimator of compliance share:

$$S_{c} = -\frac{E\left[1\left\{D_{i} = c\right\}|Z_{i} = 1\right] - E\left[1\left\{D_{i} = c\right\}|Z_{i} = 0\right]}{E\left[1\left\{D_{i} = h\right\}|Z_{i} = 1\right] - E\left[1\left\{D_{i} = h\right\}|Z_{i} = 0\right]}$$

-			Offered			Not offered		Other center
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Table 3: Preschool Choices by Year, Cohort, and Offer Status

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	Table 5. Funding		Other centers attended
	Head Start	Other centers	by $c \rightarrow h$ compliers
Largest funding source	(1)	(2)	(3)
Head Start	0.842	0.027	0.038
Parent fees	0.004	0.153	0.191
Child and adult care food program	0.011	0.026	0.019
State pre-K program	0.004	0.182	0.155
Child care subsidies	0.013	0.097	0.107
Other funding or support	0.022	0.118	0.113
No funding or support	0.000	0.003	0.001
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Benefits and Costs of Head Start

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Benefits

Increased earnings
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Tuition / time savings for parents

Reductions in crime

Health improvements

Increased earnings

Tuition / time savings for parents

Reductions in crime

Health improvements

Net Costs

Administrative costs

Increased earnings

Tuition / time savings for parents

Reductions in crime

Health improvements

Net Costs

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Reduced funding of competing preschool programs

Extra tax revenue from more productive children

Increased earnings

Tuition / time savings for parents

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Administrative costs

Reduced funding of competing preschool programs

Extra tax revenue from more productive children

Extra tax revenue from parents Table

Reduced participation in transfer programs

Savings from reduced grade repetition / Special Ed

Table 1: Summary of Cost-Benefit Studies						
	Tulsa Full- Day Preschool	Tulsa Half-Day Preschool	Oklahoma & Georgia Preschool	Head Start	Perry Preschool	
Year children entered program	2005	2005	1995/98	2002	1962	
Value of earnings gains per child	\$27,897	\$16,683	\$24,094	\$14,459	\$92,020	
Value of total benefits per child					\$180,257 ^b	
Cost of program per child	\$9,118	\$4,559	\$4,086	\$9,173	\$20,948	
Net benefit per child	\$18,779	\$12,124	\$20,008	\$5,286	\$159,309 ^b	
Benefit to cost ratio (earnings only)	3.06	3.66	5.90	1.58ª	4.39	
Benefit to cost ratio (all benefits)	-	-	-	-	8.60 ^b	
Study	Bartik	Bartik	Cascio	Duncan	Heckman	
	et al.	et al.	et al.	et al.	et al.	
	(2012)	(2012)	(2013)	(2010)	(2010b)	

A Model of Head Start Enrollment

- Continuum of applicant households on unit interval
- Government rations access to HS (ex-ante) with offers Z_i
 - Randomly assigned with probability $\delta \equiv P(Z_i = 1)$
- Competing preschools not rationed (will relax later)

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 - Randomly assigned with probability $\delta \equiv P(Z_i = 1)$
- Competing preschools not rationed (will relax later)
- Utilities: $\{U_i(h,z), U_i(c), U_i(n)\}$ where:

 $U_{i}\left(h,1
ight)\geq U_{i}\left(h,0
ight)$

• Preferred alternative as function of offer status $z \in \{0, 1\}$:

$$D_{i}(z) = \arg \max_{d \in \{h,c,n\}} U_{i}(d,z)$$

Choices:

$$D_{i} = D_{i}(1) Z_{i} + D_{i}(0) (1 - Z_{i})$$

After-tax lifetime income of cohort:

$$(1- au)pE[Y_i]$$

- $Y_i = \sum_{d \in \{n,c,h\}} Y_i(d) \mathbb{1}[D_i(Z_i) = d]$ is realized test score
- p is the market price of human capital
- τ is the tax rate for Head Start-eligible children

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Net Costs:

$$C \equiv \underbrace{\phi_h P(D_i = h) + \phi_c P(D_i = c)}_{\text{Costs}} - \left(\underbrace{\frac{R + \tau p E[Y_i]}{Revenue}}_{\text{Revenue}}\right)$$

where (ϕ_h,ϕ_c) are costs of enrollment in HS / other preschool

Increasing offer probability

Marginal effect of a change in rationing probability $\boldsymbol{\delta}$ on test scores:

$$\frac{dE[Y_i]}{d\delta} = LATE_h \cdot P(D_i(1) = h, D_i(0) \neq h)$$

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Marginal effect on budget:



Marginal Value of Public Funds

 The marginal value of public funds (MVPF) is the ratio of impacts on household welfare and the government budget (Mayshar, 1990; Hendren, 2014):

$$MVPF_{\delta} = \frac{(1-\tau)pLATE_{h}}{\phi_{h} - \phi_{c}S_{c} - \tau pLATE_{h}}$$

- MVPF gives the value of an extra dollar spent on Head Start net of fiscal externalities
- Quantifies the magnitude of "leaks" in Okun's bucket



Program Scale: Lessons

$$MVPF_{\delta} = \frac{(1-\tau)pLATE_{h}}{\phi_{h} - \phi_{c}S_{c} - \tau pLATE_{h}}$$

MVPF depends on:

- Test score impact LATE_h
 - Note: "subLATEs" not directly relevant
- Share of students drawn from competing programs, S_c
- Costs of Head Start and competing programs: ϕ_h and ϕ_c
- Conversion factor p
- Tax rate τ

What if competing schools are rationed?

- Suppose total number of competing pre-school slots is fixed
 - Now c-compliers spawn $n \rightarrow c$ compliers as someone takes abandoned slot
- MVPF becomes:

$$MVPF_{\delta,rat} = \frac{(1-\tau)p(LATE_h + S_cLATE_{nc})}{\phi_h - \tau p(LATE_h + S_cLATE_{nc})}$$

- Takeaway:
 - LATE_{nc} not directly identified by experiment
 - But chances are that ignoring rationing leads to conservative assessment (will estimate later)

- Suppose there is a Head Start program feature f that is valued by households but has no effect on potential outcomes:

 Ũ(h, Z_i, f) = U(h, Z_i) + f
 - Example: Improvements in transportation services (Executive Order 13330)
- With large enough increases in f:
 - Never takers become compliers
 - Compliers become always takers

MVPF for Program Features

MVPF for reforms to program features:

$$MVPF_{f} = \frac{(1-\tau)pMTE_{h}(f)}{\phi_{h}(f)(1+\eta) - \phi_{c}\overrightarrow{S}_{c}(f) - \tau pMTE_{h}(f)}$$

where:

$$MTE_{h}(f) = MTE_{ch}(f)\vec{S}_{c}(f) + MTE_{nh}(f)\left(1 - \vec{S}_{c}(f)\right),$$

$$MTE_{ch}(f) = E\left[Y_{i}(h) - Y_{i}(c)|U_{i}(h, Z_{i}, f) = U_{i}(c) > U_{i}(n)\right],$$

$$\vec{S}_{c}(f) = P\left(U_{i}(c) > U_{i}(n)|U_{i}(h, Z_{i}, f) = \max\left\{U_{i}(c), U_{i}(n)\right\}\right),$$

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$$\overrightarrow{S}_{c}(f) = P\left(U_{i}(c) > U_{i}(n)|U_{i}(h, Z_{i}, f) = \max\left\{U_{i}(c), U_{i}(n)\right\}\right),$$

$$\eta = \frac{d \log \phi_h(f) / df}{d \log P \left(D_i = h \right) / df} \text{ (cost elasticity of enrollment)}$$

Cost-benefit Analysis

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- Focus on 1st-year scores:
 - Most precise estimates
 - Chetty et al. (2011) find that these best predict long-run gains Figure
- Projected earnings effects:
 - Chetty et al. (2011): 1 s.d. increase in scores \rightarrow 13% increase in earnings
 - Other literature estimates: 10% or larger (Table A3)
 - $\bullet\,$ To be conservative, baseline calibration uses $10\%\,$
 - Sensitivity analysis: *breakeven* conversion factor s.t. *MVPF* = 1

Table A.5: Estimates of Test Score and Earnings Impacts				
	Test score effect	Log earnings	Log wage	Ratio: wages or
Intervention	(std. dev.)	effect	effect	earnings/test scores
(1)	(2)	(3)	(4)	(5)
Tennessee STAR	0.024	0.003	-	0.131
(1 s.d. of class quality, kindergarten)				
OLS with controls	1.0	0.18	-	0.18
(kindergarten)				
Teacher value-added	0.13	0.013	-	0.103
(1 s.d. of teacher VA, grades 3-8)				
OLS with controls	1.0	0.12	-	0.12
(grades 3-8)				
OLS with controls	1.0		0.121	0.121
(males, ages 14-22)				•••
OLS with controls	1.0	-	0.169	0.169
(females, ages 14-22)	1.0		0.105	0.102
5	0.787	0.189	-	0.240
(males, age 4)				
Perry Preschool Project	0.980	0.286	-	0.292
(females, age 4)				
OLS with controls	1.0	0.136	0.104	0.104
(males, ages 18-19)				
	Intervention (1) Tennessee STAR (1 s.d. of class quality, kindergarten) OLS with controls (kindergarten) Teacher value-added (1 s.d. of teacher VA, grades 3-8) OLS with controls (grades 3-8) OLS with controls (males, ages 14-22) OLS with controls (females, ages 14-22) Perry Preschool Project (males, age 4) Perry Preschool Project (females, age 4) OLS with controls	Test score effect Intervention (std. dev.) (1) (2) Tennessee STAR 0.024 (1 s.d. of class quality, kindergarten) 0.024 OLS with controls 1.0 (kindergarten) 1.0 Teacher value-added 0.13 (1 s.d. of teacher VA, grades 3-8) 0.025 OLS with controls 1.0 (grades 3-8) 1.0 (males, ages 14-22) 0.13 OLS with controls 1.0 (females, ages 14-22) 0.787 Perry Preschool Project 0.787 (males, age 4) 0.13 OLS with controls 1.0	Test score effect Log earnings Intervention Intervention (std. dev.) effect (1) (2) (3) Tennessee STAR 0.024 0.003 (1 s.d. of class quality, kindergarten) 0LS with controls 1.0 0.18 (kindergarten) Teacher value-added 0.13 0.013 (1 s.d. of teacher VA, grades 3-8) 0LS with controls 1.0 0.12 (grades 3-8) 0LS with controls 1.0 - (males, ages 14-22) 0LS with controls 1.0 - Perry Preschool Project 0.787 0.189 (males, age 4) Perry Preschool Project 0.980 0.286 (females, age 4) OLS with controls 1.0 0.139 0.136	Test score effect Log earningsLog wage effect(1)(2)(3)(4)(1)(2)(3)(4)Tennessee STAR0.0240.003-(1 s.d. of class quality, kindergarten)0LS with controls1.00.18-(kindergarten)1.00.130.013-Teacher value-added0.130.013(grades 3-8)0LS with controls1.00.12-(grades 3-8)0LS with controls1.0-0.121(males, ages 14-22)0LS with controls1.0-0.169Perry Preschool Project0.7870.189-(males, age 4)0LS with controls1.00.286-(females, age 4)0LS with controls1.00.1360.104

Table A3: Estimates of Test Score and Earnings Impacts

Table 6: Benefits and Costs of Head Start				
Parameter	Description		Source	
(1)	(2)	(3)	(4)	
	Panel A. Parameter values			
р	Effect of a 1 SD increase in test scores on earnings	$0.1\bar{e}$	Table A3	
e_{US}	US average present discounted value of lifetime earnings at age 3.4	\$438,000	Chetty et al. 2011 with 3% discount rate	
e_{parent}/e_{US}	Average earnings of Head Start parents relative to US average	0.46	Head Start Program Facts	
IGE	Intergenerational income elasticity	0.40	Lee and Solon 2009	
\bar{e}	Average present discounted value of lifetime earnings for Head Start applicant:	\$343,392	$[1 - (1 - e_{parent}/e_{US})IGE]e_{US}$	
$0.1\bar{e}$	Effect of a 1 SD increase in test scores on earnings of Head Start applicants	\$34,339		
$LATE_h$	Local Average Treatment Effect	0.247	HSIS	

Table 6: Benefits and Costs of Head Start			
Parameter	Description	Value	Source
(1)	(2)	(3)	(4)
S_c	Share of Head Start population drawn from other preschools	0.34	HSIS
ϕ_h	Marginal cost of enrollment in Head Start	\$8,000	Head Start program facts
ϕ_c	Marginal cost of enrollment in other preschools	\$0	Naïve assumption: $\phi_c = 0$
		\$4,000	Pessimistic assumption: $\phi_c = 0.5\phi_h$
		\$6,000	Preferred assumption: $\phi_c = 0.75\phi_h$

Table 6: Benefits and Costs of Head Start				
Parameter	Description	Value	Source	
(1)	(2)	(3)	(4)	
NMB	Marginal benefit to Head Start population net of taxes	\$5,513	$(1 - \tau)pLATE_h$	
MFC	Marginal fiscal cost of Head Start enrollment	\$5,031	$\phi_h - \phi_c S_c - \tau p LATE_h$, naïve assumption	
		\$3,671	Pessimistic assumption	
		\$2,991	Preferred assumption	
MVPF	Marginal value of public funds	1.10 (0.22) <i>p</i> -value = 0.1	NMB/MFC (s.e.), naïve assumption	
		Breakeven $p/\bar{e}=0.09~(0.01)$		
		1.50 (0.34) p-value = 0.00 Breakeven $p/\bar{e} = 0.08$ (0.01)	Pessimistic assumption	
		1.84 (0.47) p-value = 0.00 Breakeven $p/\bar{e} = 0.07 (0.01)$	Preferred assumption	

- Are Head Start and competing programs equivalent technologies?
 - Decompose *LATE_h* into "subLATEs" for compliers drawn from *c* and *n*
- Can we boost effectiveness by targeting new populations?
 - Evaluate reforms that change the complier mix
- Answering these questions requires additional assumptions

Possible Approaches to Estimating SubLATEs

- Use $Z_i \times X_i$ interactions as additional instruments (Kling et al., 2007)
 - Requires strong restrictions on effect heterogeneity (Kirkeboen et al., 2014; Hull, 2014)
- Parametric assumption on distributions within compliance groups ("principal stratification," Feller et al. 2014)
 - Allows deconvolution of complier mix into components
 - Conditions on realized selection patterns no predictions for effects of structural reforms
- Selection model
 - Semiparametric restriction on unselected potential outcome distributions
 - "Connect the dots" between identified distributions to interpolate/extrapolate

• Alternative specific indirect utilities:

$$U_{i}(h, Z_{i}) = \psi_{h}(X_{i}, Z_{i}) + v_{ih},$$

$$U_{i}(c) = \psi_{c}(X_{i}) + v_{ic},$$

$$U_{i}(n) = 0$$

• Monotonicity:
$$\psi_h(x, 1) \ge \psi_h(x, 0)$$

- Selection errors (*v_{ih}*, *v_{ic}*): unobserved tastes and constraints (e.g. accessibility) influencing participation
- Multinomial probit specification of errors:

$$(v_{ih}, v_{ic}) | X_i, Z_i \sim N\left(0, \begin{bmatrix} 1 & \rho(X_i) \\ \rho(X_i) & 1 \end{bmatrix}\right)$$

Potential Outcomes

Model for potential outcome CEFs:

$$E[Y_i(d)|X_i, Z_i, v_{ih}, v_{ic}] = \mu_d(X_i) + \gamma_{dh}v_{ih} + \gamma_{dc}v_{ic}$$

- $\{\gamma_{dh}, \gamma_{dc}\}$ terms capture selection on unobservables
- Possible selection patterns:
 - $\gamma_{hh} = -\gamma_{nh}$ (selection on gains)
 - $\{\gamma_{dh}\} = \gamma_h$ (selection on levels)
 - $\gamma_{hh} < \gamma_{nh}$ ("reverse Roy" selection)

By iterated expectations:

$$E[Y_i|X_i, Z_i, D_i = d] = \mu_d(X_i) + E[\gamma_{dh}v_{ih} + \gamma_{dc}v_{ic}|X_i, Z_i, D_i = d]$$
$$= \mu_d(X_i) + \gamma_{dh}\lambda_h(X_i, Z_i, d) + \gamma_{dc}\lambda_c(X_i, Z_i, d)$$

- Control function terms λ_d(X_i, Z_i, D_i) analogous to inverse Mills terms in standard Heckman (1979) setting Review
 - Involve evaluation of bivariate normal CDFs/PDFs (formulas provided in paper)

Effect of an offer on selected outcome mean:

$$E[Y_i|X_i = x, Z_i = 1, D_i = d] - E[Y_i|X_i = x, Z_i = 0, D_i = d]$$

$$= \gamma_{dh} \left[\lambda_h(x,1,d) - \lambda_h(x,0,d) \right] + \gamma_{dc} \left[\lambda_c(x,1,d) - \lambda_c(x,0,d) \right]$$

- With two points of support x and x', we have two equations in two unknowns
- Rank condition: CF differences not linearly dependent across x groups
 - Regression based test for under-identification
- Additional support points yield over-identification
 - Score test of separability

- Functional forms for mean utilities, correlation, and mean outcomes not essential
 - Can fully saturate and retain identification
- Key restriction is *additive separability* between observables and unobservables
 - Selection on unobservables must work "the same way" for different values of *X_i*
 - e.g. can't have Roy selection in some groups and "reverse Roy" in others
- $\{\gamma_{dh}, \gamma_{dc}\}$ terms measure how gaps between compliance group means vary with strength of compliance response

Parameterization

- Linear approximations to mean utilities $\psi_h(X, Z)$, $\psi_c(X)$, $\tanh^{-1} \rho(X) = \frac{1}{2} \log \left(\frac{1+\rho(X)}{1-\rho(X)} \right)$, and $\mu_d(X)$
- Key covariates interact with offer/enter correlation in the choice model, and interact with care alternative in the outcome model
 - Baseline test score, home language, mother's education, age cohort, Head Start center quality rating, transportation services, income
 - Previous studies find substantial heterogeneity on these dimensions in the HSIS (Bitler et al. 2014, Bloom and Weiland 2015, Walters 2015)
- Also substantial variation in treatment effects and substitution patterns across the hundreds of HSIS experimental sites (Walters 2015)
- But difficult to work with individual sites since samples are very small incidental parameters problem

- To leverage variation in market shares across sites, we use a group fixed effects approach (Bonhomme and Manresa 2015; Saggio 2012)
- Constrains sites to belong to one of K discrete categories
 - K selected using Bayesian Information Criterion (BIC)
 - Site group indicators included in X
- MATLAB code available on our websites (mnpgfe routine)

Estimation / Inference

- Two-step procedure a la Heckman (1979)
- First step: estimate multinomial probit using GHK algorithm
 - Models with site groups alternate between assigning groups and maximizing likelihood
- Second step: use probit estimates to build control functions,

$$\left\{ \hat{\lambda}_{dh}\left(X_{i},Z_{i},D_{i}
ight),\hat{\lambda}_{dc}\left(X_{i},Z_{i},D_{i}
ight)
ight\}$$

- Include CFs as additional regressors in second step regression of outcomes on covariates in each choice group
- Bootstrap for inference

	One endogenous variable	Two endogenous variables	
	Head Start	Head Start	Other centers
Instruments	(1)	(2)	(3)
Offer	0.247	-	-
(1 instrument)	(0.031)		
Offer x covariates	0.241	0.384	0.419
(9 instruments)	(0.030)	(0.127)	(0.359)
First-stage F	276.2	17.7	1.8
Overid. p-value	0.007	0.006	
Offer x sites	0.210	0.213	0.008
(183 instruments)	(0.026)	(0.039)	(0.095)
First-stage F	215.1	90.0	2.7
Overid. p-value	0.002	0.002	
Offer x site groups	0.229	0.265	0.110
(6 instruments)	(0.029)	(0.056)	(0.146)
First-stage F	1,015.2	339.1	32.6
Overid. p-value	0.077	0.050	
Offer x covariates and	0.229	0.302	0.225
offer x site groups (14 instruments)	(0.029)	(0.054)	(0.134)
First-stage F	340.2	121.2	13.3
Overid. p-value	0.012	0	.010

Table V. Two Stage Least Squares Estimates with Interaction Instruments






Figure A.I. Multinomial Probit Model Fit



Panel B. Substitute preschool participation

Figure A.I. Multinomial Probit Model Fit



Figure A.III. Model-predicted LATE h vs. IV estimates

	Least s	Least squares		
	No controls	Covariates		
	(1)	(2)		
Head Start	0.202	0.218		
	(0.037)	(0.022)		
Other preschools	0.262	0.151		
	(0.052)	(0.035)		

-

-

Table VII. Selection-corrected Estimates of Preschool Effects

 λ_h

Head Start x λ_h

Other preschools $x \lambda_h$

 λ_c

Head Start x λ_c

Other preschools x λ_c

P-value: Additive separability

_	Control function			
	Covariates (3)	Site groups (4)	Full model (5)	
Head Start	0.483	0.380	0.470	
	(0.117)	(0.121)	(0.101)	
Other preschools	0.183	0.065	0.109	
	(0.269)	(0.991)	(0.253)	
λ_h	0.015	0.004	0.019	
	(0.053)	(0.063)	(0.053)	
Head Start x λ_h	-0.167	-0.137	-0.158	
	(0.080)	(0.126)	(0.091)	
Other preschools $x \lambda_h$	-0.030	-0.047	0.000	
	(0.109)	(0.366)	(0.115)	
λ_c	-0.333	-0.174	-0.293	
	(0.203)	(0.187)	(0.115)	
Head Start x λ_c	0.224	0.065	0.131	
	(0.306)	(0.453)	(0.172)	
Other preschools x λ_c	0.488	0.440	0.486	
	(0.248)	(0.926)	(0.197)	
P-value: Additive separability	0.261	0.452	0.349	

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	(3)	(4)	(5)	
Head Start	0.483	0.380	0.470	
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Other preschools	0.183	0.065	0.109	
	(0.269)	(0.991)	(0.253)	
λ_h	0.015	0.004	0.019	
	(0.053)	(0.063)	(0.053)	
Head Start x λ_h	-0.167	-0.137	-0.158	
	(0.080)	(0.126)	(0.091)	
Other preschools $x \lambda_h$	-0.030	-0.047	0.000	
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λ_c	-0.333	-0.174	-0.293	
	(0.203)	(0.187)	(0.115)	
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	(0.248)	(0.926)	(0.197)	
P-value: Additive separability	0.261	0.452	0.349	

Table VII. Selection-corrected Estimates of Preschool Effects

		Control function				Control function		ion
	IV	Covariates	Sites	Full model				
Parameter	(1)	(2)	(3)	(4)				
LATE $_h$	0.247	0.261	0.190	0.214				
	(0.031)	(0.032)	(0.076)	(0.042)				
LATE nh	-	0.386	0.341	0.370				
		(0.143)	(0.219)	(0.088)				
LATE ch		0.023	-0.122	-0.093				
		(0.251)	(0.469)	(0.154)				

Table VIII. Treatment Effects for Subpopulations

14010 (111. 1	Control for stion				
			Control function		
	IV	Covariates	Sites	Full model	
Parameter	(1)	(2)	(3)	(4)	
Lowest predicted quintile:					
LATE $_h$		0.095	0.114	0.027	
		(0.061)	(0.112)	(0.067)	
LATE $_h$ with fixed S_c		0.125	0.125	0.130	
		(0.060)	(0.434)	(0.119)	
Highest predicted quintile:					
LATE $_h$		0.402	0.249	0.472	
		(0.042)	(0.173)	(0.079)	
LATE $_h$ with fixed S_c		0.364	0.289	0.350	
		(0.056)	(1.049)	(0.126)	

Table VIII. Treatment Effects for Subpopulations

	One endogenous variable		idogenous iables
	Head Start	Head Start	Other centers
Instruments	(1)	(2)	(3)
Offer	0.247	-	-
(1 instrument)	(0.031)		
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offer x site groups (14 instruments)	(0.029)	(0.054)	(0.134)
First-stage F	340.2	121.2	13.3
Overid. p-value	0.012	0	.010

Table V. Two Stage Least Squares Estimates with Interaction Instruments

- Next, we evaluate returns to "structural" reforms that target new populations by increasing attractiveness of Head Start
- Use the model to predict $MTE_{ch}(f)$, $MTE_{nh}(f)$ and $\vec{S}_{c}(f)$

Marginal effects on test scores and program substitution



Marginal Cost-Benefit Scenarios



Cascio and Schanzenbach (2013)



Average effect size in standard deviations



Source: Duncan and Magnuson (2013); Weiland and Yoshikawa (2013).

Note: Circle sizes reflect the inverse of the squared study-level standard error. 74 of 83 studies showed positive effects, and CEA estimates that roughly 60 percent of estimates were statistically significant at the 10 percent level.

Conclusion: Going forward...

$$MVPF_{\delta} = \frac{(1-\tau)pLATE_{h}}{\phi_{h} - \phi_{c}S_{c} - \tau pLATE_{h}}$$

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$$MVPF_{\delta} = \frac{(1-\tau)pLATE_{h}}{\phi_{h} - \phi_{c}S_{c} - \tau pLATE_{h}}$$

Our estimates suggest that as $S_c
ightarrow 1$:

$$(1- au)$$
pLATE_h $ightarrow$ 0 $\phi_h - \phi_c S_c - au$ pLATE_h $ightarrow \phi_h - \phi_c$

Conclusion: Going forward...

$$MVPF_{\delta} = \frac{(1-\tau)pLATE_{h}}{\phi_{h} - \phi_{c}S_{c} - \tau pLATE_{h}}$$

Our estimates suggest that as $S_c
ightarrow 1$:

$$(1 - \tau)$$
pLATE_h $\rightarrow 0$
 $\phi_h - \phi_c S_c - \tau$ *pLATE_h* $\rightarrow \phi_h - \phi_c$

Perhaps then we should expect that:

$$MVPF_{\delta} \rightarrow 0?$$

Depends critically on cost side: $\phi_h - \phi_c$

BONUS

Figure 1: Complier Shares and Head Start Effects



			Other centers attended
	Head Start	Other centers	by $c \rightarrow h$ compliers
	(1)	(2)	(3)
Quality index	0.702	0.453	0.446
Transportation provided	0.629	0.383	0.324
Fraction of staff with bachelor's degree	0.345	0.527	0.491
Fraction of staff with teaching license	0.113	0.260	0.247
Center director experience	18.2	12.2	12.6
Student/staff ratio	6.80	8.24	8.54
Full day service	0.637	0.735	0.698
More than three home visits per year	0.192	0.073	0.072
N	1848	366	

		1 0	Other centers attended
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	(1)	(2)	(3)
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More than three home visits per year	0.192	0.073	0.072
N	1848	366	

Table 4. Characteristics (of field Start and C	shipeting i reschoor	
	Head Start	Other centers	Other centers attended by $c \rightarrow h$ compliers
	(1)	(2)	(3)
Quality index	0.702	0.453	0.446
Transportation provided	0.629	0.383	0.324
Fraction of staff with bachelor's degree	0.345	0.527	0.491
Fraction of staff with teaching license	0.113	0.260	0.247
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N	1848	366	

	of field Start and C	ompeting i resenoor	Other centers attended
	Head Start (1)	Other centers (2)	by $c \rightarrow h$ compliers (3)
Quality index	0.702	0.453	0.446
Transportation provided	0.629	0.383	0.324
Fraction of staff with bachelor's degree	0.345	0.527	0.491
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Full day service	0.637	0.735	0.698
More than three home visits per year	0.192	0.073	0.072
N	1848	366	

	Experimental center	Attended center
	(1)	(2)
Transportation provided	0.421	0.458
Quality index	0.701	0.687
Fraction of staff with bachelor's degree	0.304	0.321
Fraction of staff with teaching license	0.084	0.099
Center director experience	19.08	18.24
Student/staff ratio	6.73	6.96
Full day service	0.750	0.715
More than three home visits per year	0.112	0.110
Ν	112	2
<i>p</i> -value	0.31	8

Table A1: Characteristics of Head Start Centers Attended by Always Takers

Notes: This table reports characteristics of Head Start centers for children assigned to the HSIS control group who attended Head Start. Column (1) shows characteristics of the centers of random assignment for these children, while column (2) shows characteristics of the centers they attended. The *p*-value is from a test of the hypothesis that all mean center charteristics are the same. The sample excludes children with missing values for either characteristics of the center of random assignment or the center attended.



No Parental Labor Supply Response

Table A2: Effects on Maternal Labor Supply		
	Full-time	Full- or part-time
	(1)	(2)
Offer effect	0.020	-0.005
	(0.018)	(0.019)
Mean of dep. var.	0.334	0.501
N		3314
N		3314

Back

Notes: This table reports coefficients from regressions of measures of maternal labor supply in Spring 2003 on the Head Start offer indicator. Column (1) displays effects on the probability of working full-time, while column (2) shows effects on the probability of working full- or parttime. Children with missing values for maternal employment are excluded. All models use inverse probability weights and control for baseline covariates. Standard errors are clustered at the Head Start center level.

• Suppose utility is over consumption (q) and leisure (\overline{l}) :

 $u\left(q,\bar{l}\right)$

• Suppose utility is over consumption (q) and leisure
$$(\overline{l})$$
:
 $u(q,\overline{l})$

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$$\equiv \tilde{y} (T - \overline{l}) + m$$

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• Compensated (Hicksian) labor supply schedule:

$$l_{c}^{*}\left(ilde{y}, ar{u}
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ight)$$

Dollar value of treatment effect

 Compensating variation CV (Δ) gives dollar value of Head Start test score impact Δ:

$$CV\left(\Delta\right)\equiv e\left(\widetilde{y},u_{0}
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• Contrast with observed earnings impacts:

$$DE(\Delta) \equiv (\tilde{y} + (1 - \tau) p\Delta) l^* (\tilde{y} + (1 - \tau) p\Delta, m) - \tilde{y} l^* (\tilde{y}, m)$$
$$DE'(0) = (1 - \tau) p l^* (\tilde{y}, m) (1 + \eta_u)$$

where η_u is *uncompensated* labor supply elasticity

An adjustment factor

• Since, CV(0) = DE(0) = 0, we have first order approximation:

$$rac{CV\left(\Delta
ight)}{DE\left(\Delta
ight)}pproxrac{CV'\left(0
ight)}{DE'\left(0
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E.g., if $\eta_u = 0.2$ would imply we need to scale observed earnings impact by 83%.
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$$\frac{CV\left(\Delta\right)}{DE\left(\Delta\right)} \approx \frac{1 + \frac{1}{2}\eta_{c}\frac{\Delta}{y}}{1 + \eta_{u} + \frac{1}{2}\eta_{u}\left(2 + \eta_{u}^{2}\right)\frac{\Delta}{y}}$$

Note: if $\eta_u \approx 0$ and $\eta_c > 0$ earnings impact *understates* welfare gain!

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- Also: if $u = u(q, \bar{l}, y)$ then extra term for "consumption value" of human capital.
- So $\frac{1}{1+\eta_u}$ scaling potentially very conservative.

MVPF

• In constant elasticity model, bang per net dollar spent is:

$$MVPF = \frac{E[CV(\Delta_{i}) | complier]}{\phi_{h} - \phi_{c}S_{c} - \tau p \frac{\partial}{\partial \delta}E\left[Y_{i}l^{*}\left(\tilde{Y}_{i}\right)\right]}$$
$$= \frac{E[CV(\Delta_{i}) | complier]}{\phi_{h} - \phi_{c}S_{c} - \tau LATE_{h}^{N}}$$
$$\geq \frac{1}{1 + \eta_{u}} \frac{(1 - \tau) LATE_{h}^{N}}{\phi_{h} - \phi_{c}S_{c} - \tau LATE_{h}^{N}}$$

where $LATE_{h}^{N} \equiv E\left[N_{i}\left(\tilde{Y}_{i}(h)\right) - N_{i}\left(\tilde{Y}_{i}(D_{i}(0))\right) | complier\right]$ gives the LATE on pre-tax earnings.

• So, we have an overestimate of MVPF by a factor of (at most) $\frac{1}{1+\eta_u}$.



CFHSSY (2011)





FIGURE VI

Review: know your Heckit

Potential outcomes

$$Y_{1i} = \mu_1 + U_{i1}$$

 $Y_{0i} = \mu_0 + U_{i0}$

• Regime switching:

$$\begin{array}{rcl} D_i^* & = & \psi_0 + \psi_1 Z_i + V_i, \\ D_i & = & \mathbf{1} \left\{ D_i^* > 0 \right\}, \end{array}$$

• Random assignment:

$$(U_{i1}, U_{i0}, V_i) \perp Z_i$$

• Result:

$$E[Y_i|Z_i = z, D_i = d] = \mu_d + E[U_{id}|Z_i = z, D_i = d]$$

= $\mu_d + \gamma_d \underbrace{\lambda_d(\pi(z))}_{\text{Control Fn}}$

where $\pi(z) = P(D_i = 1 | Z_i = z)$.

Review: control functions

$$E[Y_i|Z_i = z, D_i = d] = \mu_d + \lambda_d(\pi(z))$$

- Standard causal estimands functions of { $\mu_0, \mu_1, \lambda_0(.), \lambda_1(.), \pi(.)$ }: • ATE = $\mu_1 - \mu_0$ • MTE (z) = $\mu_1 - \mu_0 + \gamma_1 \lambda'_1(\pi(z)) - \gamma_0 \lambda'_0(\pi(z))$ • LATE = $\mu_1 - \mu_0 - (\gamma_1 - \gamma_0) \left(\frac{\pi(0) \lambda_1(\pi(0)) + (1 - \pi(1))\lambda_0(\pi(1))}{\pi(1) - \pi(0)} \right)$
- Identification challenges:
 - Getting $(\lambda_0(.), \lambda_1(.))$ requires "identification at infinity"
 - With binary instrument, need parametric structure

• Classic "two-step" Heckit:
$$\lambda_d(\pi) = \rho_d \frac{\phi(\Phi^{-1}(\pi))}{\pi}$$



Linear selection model: $E[Y_{id}|U_i] = \alpha_d + \gamma_d U_i$



Heckit model: $E[Y_{id}|U_i] = \alpha_d + \gamma_d \Phi^{-1}(U_i)$

 Folk wisdom: good instrument ⇒ parametric structure not important (Newey, Powell, Walker, 1990)

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- Heckit MTE estimate is discrete approx to derivative over range of compliance traced out by instrument.
 - In limiting case where $\pi(z') \rightarrow \pi(z)$ interpolation is exact because LATE = MTE(z)

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CF differences nearly linear

	Control function difference	Total R^2 (1)	Partial R ²	
Preschool choice			Difference in π_h (2)	Difference in π_c (3)
Head Start	v_h	0.887	0.886	0.047
	v _c	0.483	0.002	0.473
Other centers	v_h	0.930	0.929	0.549
	Vc	0.764	0.505	0.606
No preschool	v_h	0.826	0.816	0.060
	v_c	0.044	0.005	0.035

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