

Economics 2  
Fall 2024

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# LECTURE 12

## Capital, Interest, and Savings



# I. CAPITAL

# Capital

- **Capital** refers to any human-made aids to the production process of businesses, govt, housing:
  - Tangible capital: Land set-up for agriculture or construction, buildings and infrastructure, tools, machines, vehicles, etc.
  - Intangible capital: brands, intellectual property (software), etc.
- Capital is a stock: Increase in capital from one year to the next is called **investment** (=additions to capital)

## How much capital does a firm want to use?

- Its decision will be based on profit maximization.
- The firm looks at the marginal revenue product (mrp) of another unit of capital K (e.g. machine):
  - $mrp_K = mp_K \cdot mr$
  - $mp_K$  is the marginal product of capital (the extra output you get with an extra machine)
  - $mr$  is the additional revenue a firm earns by producing and selling one more unit.
- **Key complication:** a capital asset is durable (=lasts for a number of years)

## II. PRESENT VALUE AND INTEREST

# Poll

- Suppose I can give you each \$100 today. Or I can give you more if you wait 1 year. How much would I need to give you in 1 year to make you as happy as getting \$100 today:
- A. \$100
- B. \$103
- C. \$105
- D. \$110
- E. \$120 or more

# Time Preferences

- People prefer things today to things tomorrow = impatience
- Time preference is the reason that banks pay interest on saving deposits or why you have to pay interest if you borrow (student loan, credit card)
  - Interest is the amount extra that you receive each year above what you put into into your savings account
  - Interest is also the amount extra you have to pay each year above what you borrowed if you take a loan
- Time preferences very heterogeneous, inconsistent (behavioral economics)

# Present Value

- What a payment to be received in the future is worth to you today.
- If you have \$1 today and save it, you will have  $\$1+i$  one year from now where  $i$  is the interest rate
- Typically  $i$  is around 5% but varies quite a bit overtime and based on the saving vehicle you use
- We are going to assume a single and constant interest  $i$  for simplicity



Present value A of \$100 one year from now:

- Assuming the interest rate is 3%.

$$A(1+.03) = 100$$

$$A = \frac{100}{(1 + .03)}$$

$$A = \$97.1$$

Present value A of \$100 one year from now:

- Assuming the interest rate is 8%.

$$A(1+.08) = 100$$

$$A = \frac{100}{(1 + .08)}$$

$$A = \$92.6$$

Present value A of \$100 **two** years from now:

- Assuming the interest rate is 3%.

$$A(1+.03)(1+.03) = 100$$

$$A = \frac{100}{(1 + .03)^2}$$

$$A = \$94.3$$

## Present value of a single payment in the future:

$$PV(F) = \frac{F}{(1 + i)^t}$$

- F = future payment
- i = interest rate (expressed as a decimal)
- t = number of years in the future the payment is to be received
- If interest rate is high, future is heavily discounted
  - Recall that future climate change costs are small if we discount the future heavily

Present value of \$1000 each of the next three years:

- Assuming the interest rate is 3%.

$$\frac{1000}{(1 + .03)^1} + \frac{1000}{(1 + .03)^2} + \frac{1000}{(1 + .03)^3}$$

$$970.1 + 942.6 + 915.1$$

$$= \$2827.8$$

## Present value of a stream of payments:

PV(Stream of F's) =

$$\frac{F}{(1+i)^1} + \frac{F}{(1+i)^2} + \frac{F}{(1+i)^3} + \dots + \frac{F}{(1+i)^t}$$

- F = future payment in each year
- i = interest rate (expressed as a decimal)
- t = number of years in the future the last payment is made

### III. PURCHASING CAPITAL AND THE INVESTMENT DEMAND CURVE

## What a machine is worth to a firm today:

PV(Stream of  $mrp_K$ 's) =

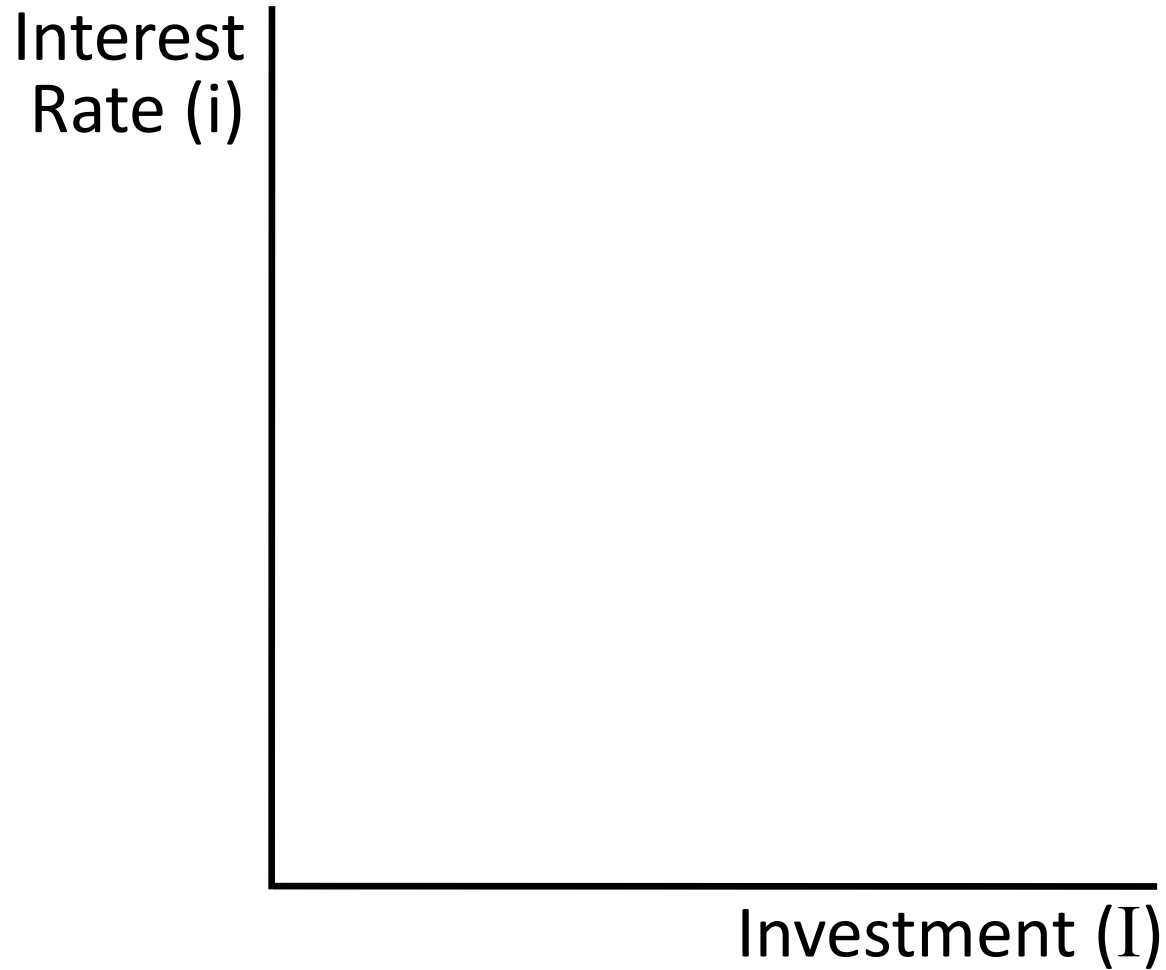
$$\frac{mrp_K}{(1+i)^1} + \frac{mrp_K}{(1+i)^2} + \frac{mrp_K}{(1+i)^3} + \dots + \frac{mrp_K}{(1+i)^t}$$

- $mrp_K$  = marginal revenue product of capital in each year
- $i$  = interest rate (expressed as a decimal)
- $t$  = lifespan of the machine

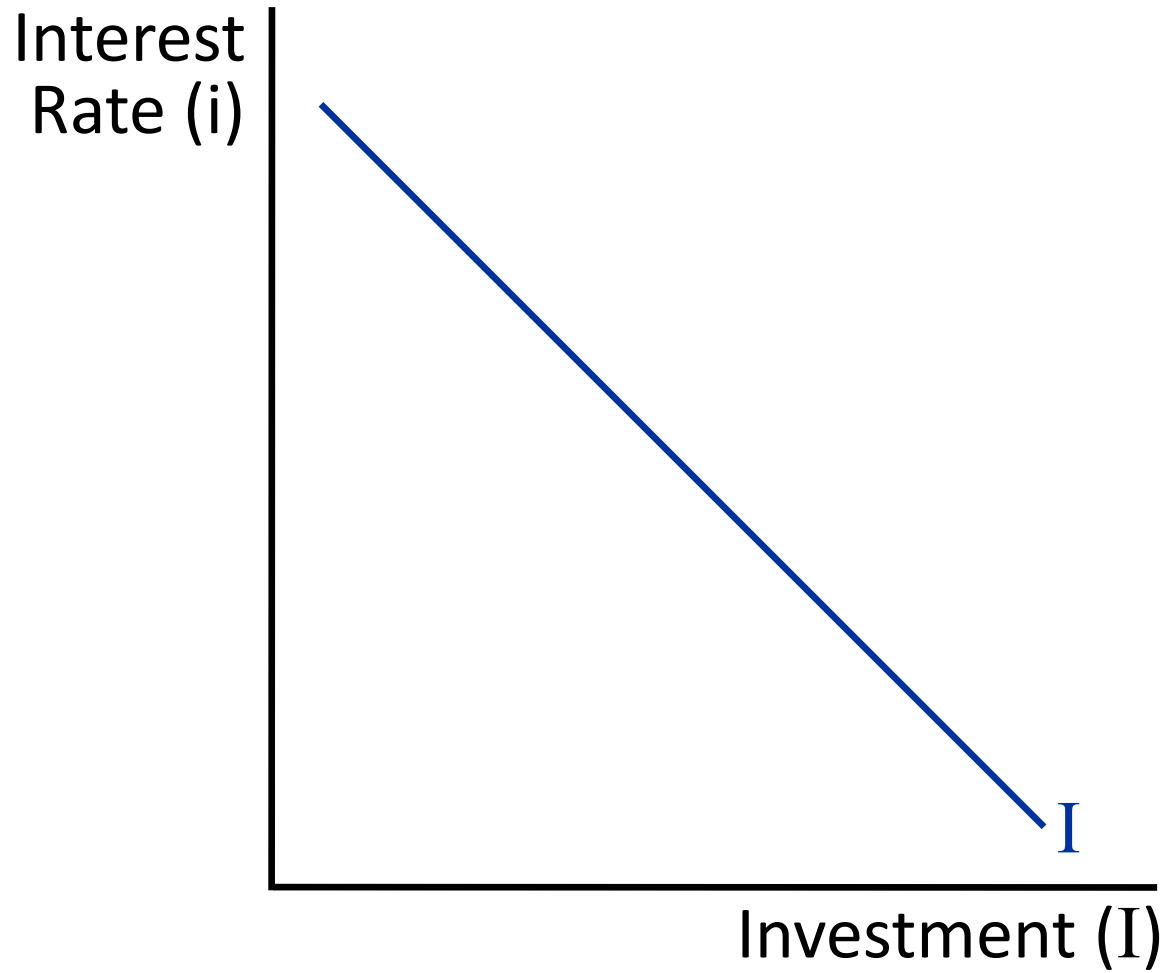
=> Machine's worth to business **declines** with  $i$



# Investment Demand Curve



# Investment Demand Curve

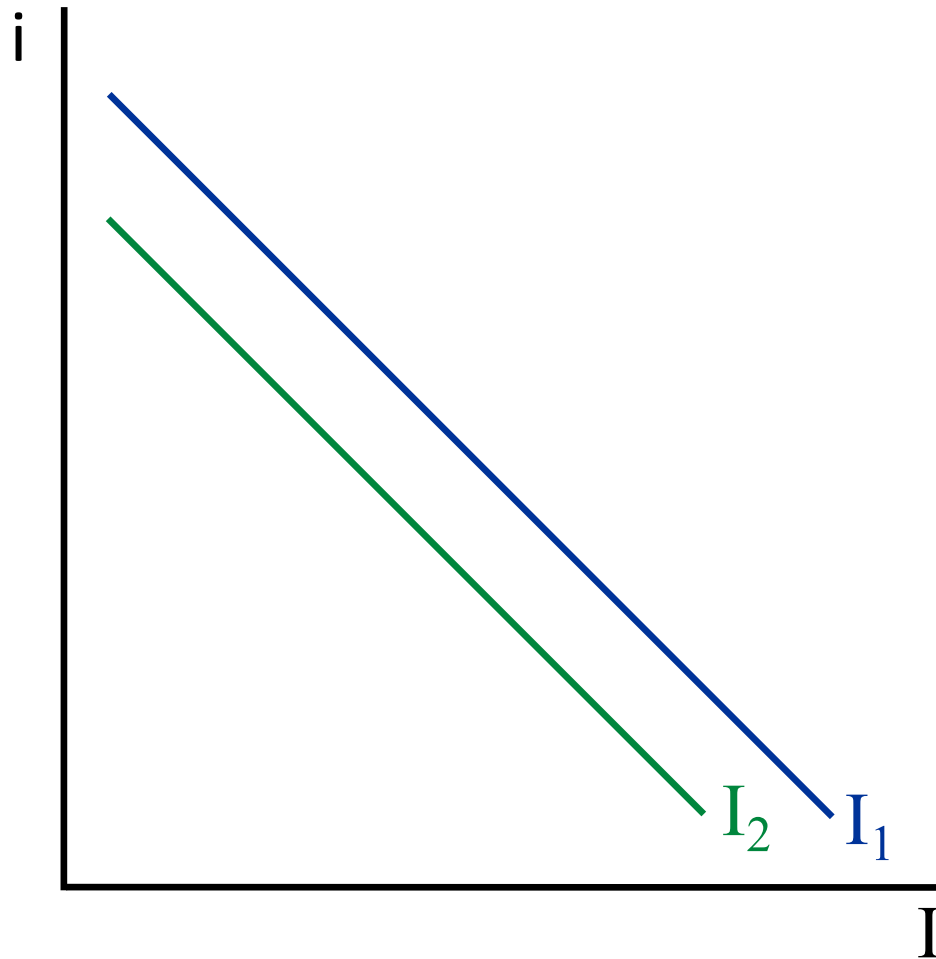


# Quiz

Why does investment by firms decline with the interest rate  $r$ ?

- A. Because investment is new capital that can be used for production for several years
- B. Because a payment in the future is less valuable when the interest rate is higher
- C. Because firms equate the cost of a new investment to the present discounted value of the extra profits the new investment will generate
- D. All of the above
- E. None of the above

# Shifts in the Investment Demand Curve (Pessimism about Future $MRP_K$ )



Recall:  $PV(\text{Stream of } mrp_K\text{'s}) = \text{Purchase Price}$

## IV. SUPPLY OF SAVINGS AND INTEREST RATE

# Saving, Consumption, and Income

- Household has disposable income  $\$Y$  (after taxes and transfers)
- $Y$  can be used for consumption  $C$  and savings  $S$

$$Y = C + S$$

- $S > 0$  means the household is adding  $S$  to its wealth (stock of past savings and inheritances)
- $S < 0$  means the household is borrowing to consume more than its income, increasing its debt and hence reducing its wealth = assets - debt

# Poll

How do you think about how much of your monthly income you decide to spend vs. save and how does this relate to the interest rate to get on your savings?

- A. I don't care about the interest rate, I just spend all the income I have and can't afford to save anything.
- B. I can save some of my income but how much I save has nothing to do with the interest rate
- C. If the interest rate is higher, I cut down my consumption and save more.
- D. If the interest rate is higher, I increase my consumption and save less.

# The Interest Rate and the Opportunity Cost of Current Consumption

- Think of a household trying to maximize its utility from consumption today and consumption in the future (=1 year from now):
  - 1) Consume \$1 today
  - 2) Or save it and consume  $\$(1+i)$  in 1 year
- When maximizing utility, consumer is indifferent at the margin between 1) and 2):

$$MU_{\text{current}} = MU_{\text{future}} \times (1+i)$$



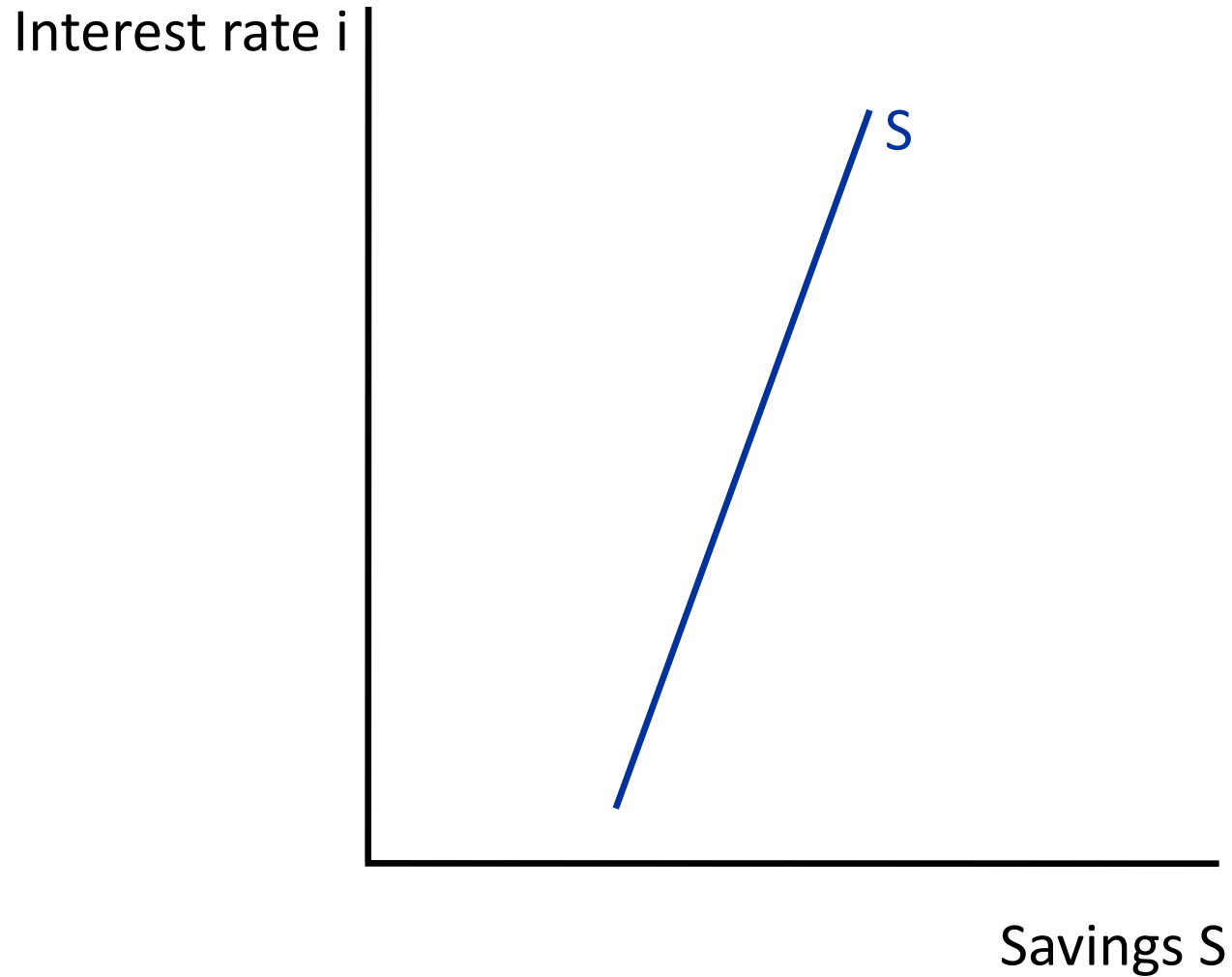
# The Interest Rate and Saving

- The condition for utility maximization between consumption today and consumption in the future:

$$MU_{\text{current}} = MU_{\text{future}} \times (1+i)$$

- If the interest rate  $i$  rises, the relative price (opportunity cost) of future consumption falls.
- $\Rightarrow$  Consume more in the future and less today (substitution effect) and hence save more
- Empirically, this channel is not very strong

# The Supply of Saving



# Quiz

How does the interest rate on your student loans will affect your spending after your graduate?

- A. It won't affect my spending because I don't have student loans
- B. Higher student loan payments will force me to cut down my other spending
- C. Higher student loan payments won't affect my spending, I'll just save less and spend the same
- D. Higher student loan payments won't affect my spending, I'll just borrow more on my credit card

# Why does the interest rate affect spending and saving in practice?

- Borrowers are low income while lenders are high income
- Low income people tend to spend everything they earn (can't afford to save)
- High income people tend to save a large fraction of any extra income they make
- A higher interest rate gives more income to lenders and correspondingly less to borrowers
- Borrowers cut spending by more than lenders increase their spending => aggregate saving goes up

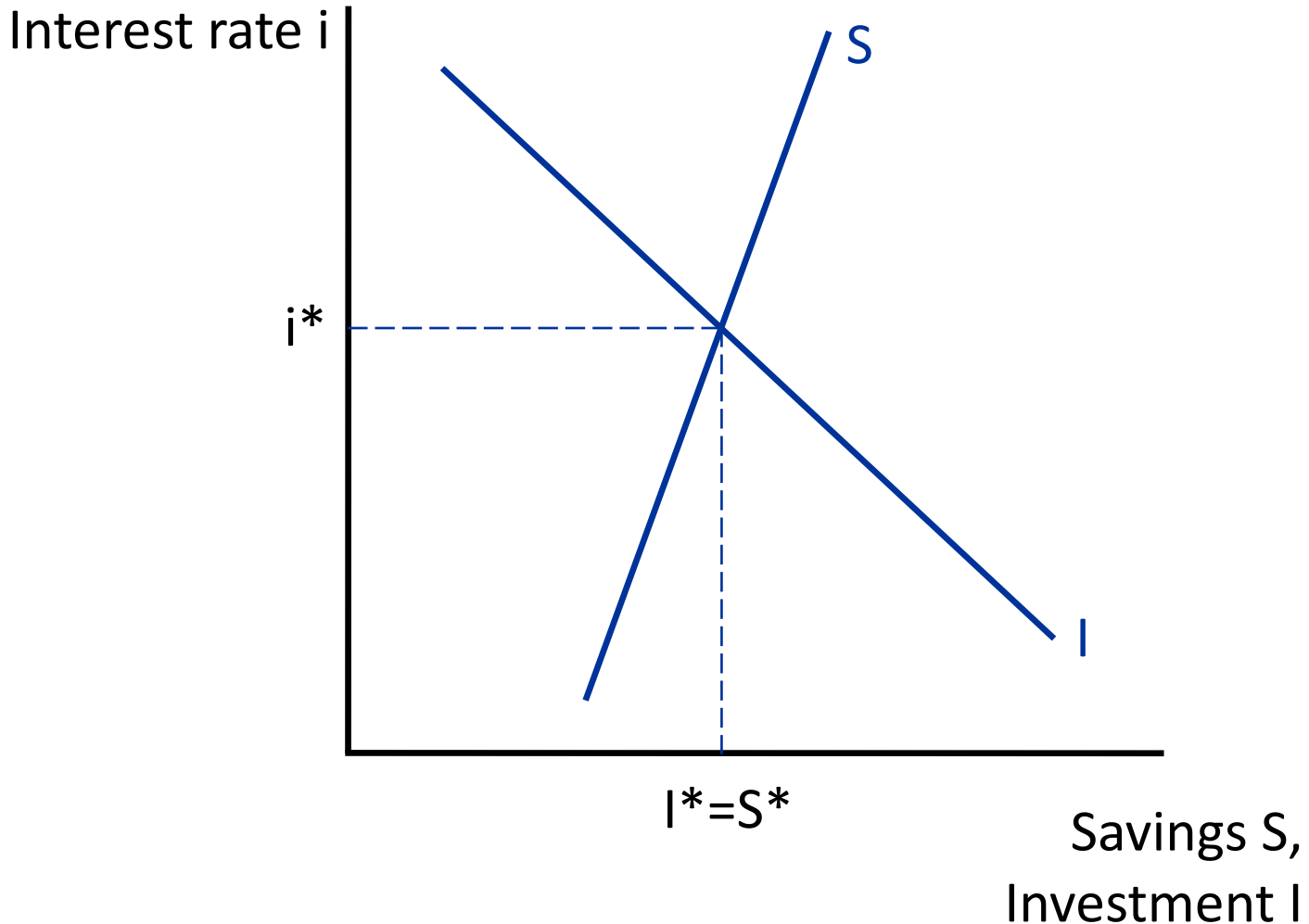
## V. THE DETERMINANTS OF INVESTMENT, SAVING, AND THE INTEREST RATE (LONG RUN)

# Market for Loanable Funds

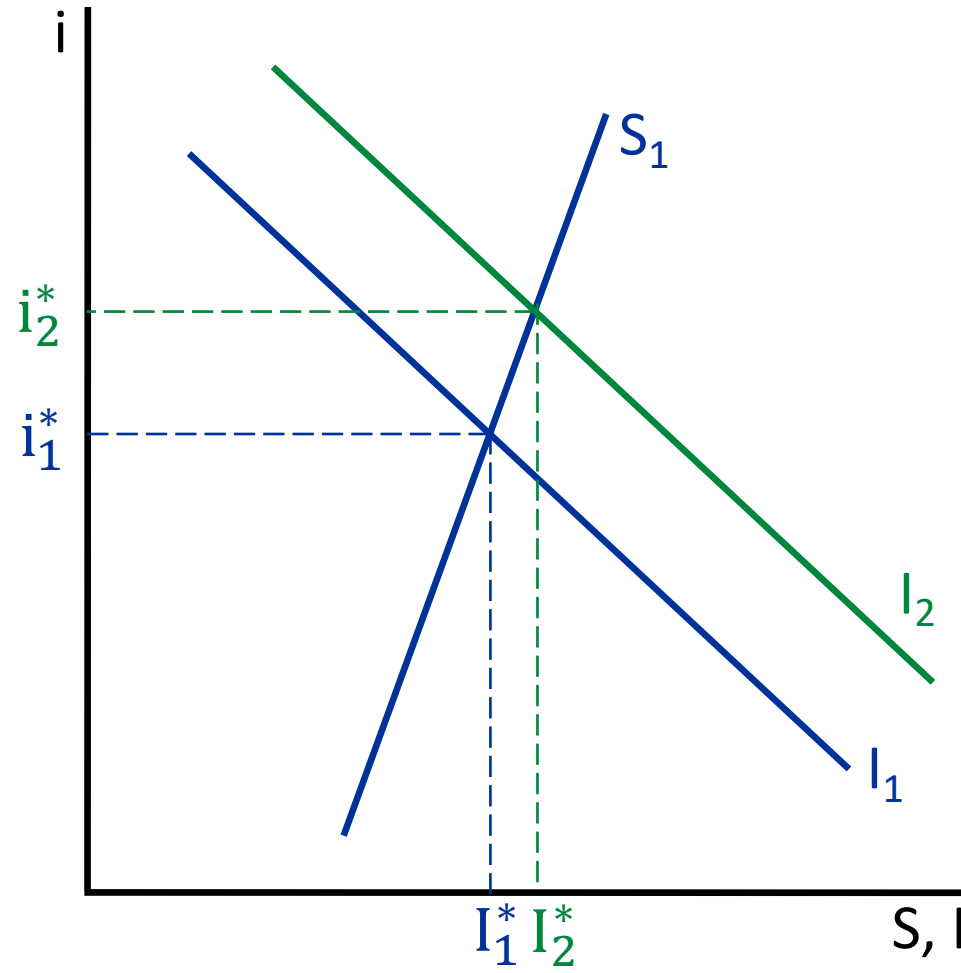
## where Investment and Saving Meet

- Demand = Investments that businesses want to fund =  $I(i)$  decreases with interest rate  $i$
- Supply = Savings provided by households or firms =  $S(i)$  increases with interest rate  $i$
- In long-run equilibrium: interest  $i^*$  adjusts so that  $I(i^*)=S(i^*)$
- In practice, many loanable funds markets
- In any closed economy: **Investment = Savings**: What is not consumed is invested

# The Long-Run Saving and Investment Market for Loanable Funds

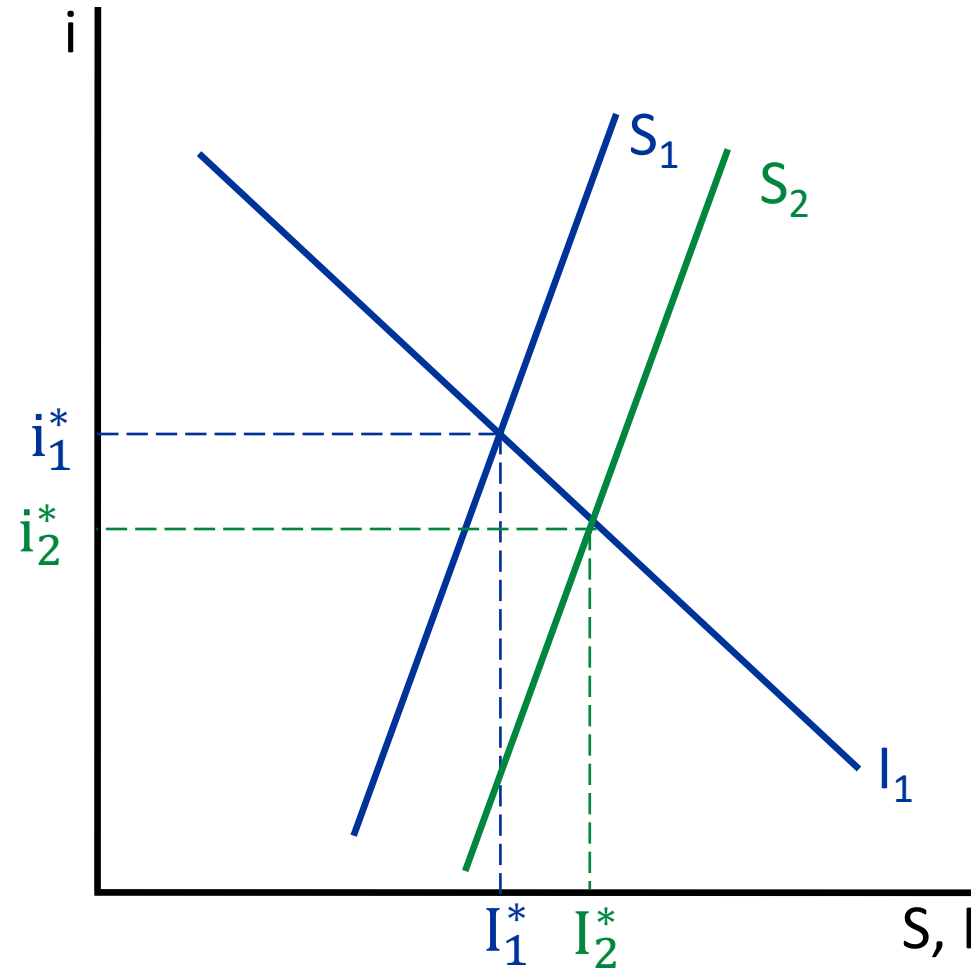


# A New Technology That Raises Future $MRP_K$ 's





# A shift out in household savings supply: people become less impatient



# VI. WEALTH FLUCTUATIONS: STOCK PRICES

# Wealth

- **Wealth** refers to the value of marketable assets (assets that are in principle tradeable). Main assets:
  - Businesses (shares of corporations, smaller businesses)
  - Housing
  - Loans and debt: loan is positive wealth for lender and negative wealth for borrower (which net out)
  - Durables (vehicles, collectibles, jewelry) small overall
- Wealth is a stock that accumulates from past savings and inheritances received
- Value of assets can fluctuate quickly and widely (stock prices)

# How are Stock Prices (value of companies) Determined?

- For publicly traded companies (listed on a stock exchange, about 5000 largest companies in US), there is a continuous market for the stock
- Sellers meet buyers and price adjusts constantly so that supply equals demand
- If more people want to buy than sell, price goes up until this is adjusted.
- How should the price be determined?

Stock price =

PV(Stream of Expected Future Profits)

Market Summary > Apple Inc

235.86 USD

+ Follow

+174.21 (282.58%) ↑ past 5 years

Closed: Oct 22, 4:01 PM EDT • Disclaimer

After hours 235.64 -0.22 (0.093%)

1D | 5D | 1M | 6M | YTD | 1Y | 5Y | Max



Open	233.88	Mkt cap	3.59T	CDP score	A-
High	236.19	P/E ratio	35.91	52-wk high	237.49
Low	232.60	Div yield	0.42%	52-wk low	164.08

Feedback

More about Apple Inc →

Apple is the highest value US company (about \$3.6T today). Stock price has been multiplied by 4 in last 5 years

# Total value of all publicly-traded stocks / GDP Ratio

Zoor 1y 5y 10y 30y **All**

1 Oct 1970 20 Oct 2024



Longtermtrends.net

Publicly traded stocks are about 1/3 of total private wealth. Value (relative to GDP) fluctuates quite a bit. Particularly high in 2024.

# What moves stock prices?

Stock price = PV(Stream of Expected Future Profits)

- A change in the interest rate.
  - Lower interest rates, all else equal, are likely to be associated with higher stock prices.
  - This is because of the usual negative effect of the interest rate on present value.
  - And because of the effect of interest rates on expected economic activity (see macro)
- Hard to see empirically as Fed picks interest rate to manage the economy (see macro)

# S&P 500 and Interest Rates



Source: Federal Reserve Bank of St. Louis, FRED.



## What moves stock prices? (cont.)

Stock price = PV(Stream of Expected Future Profits)

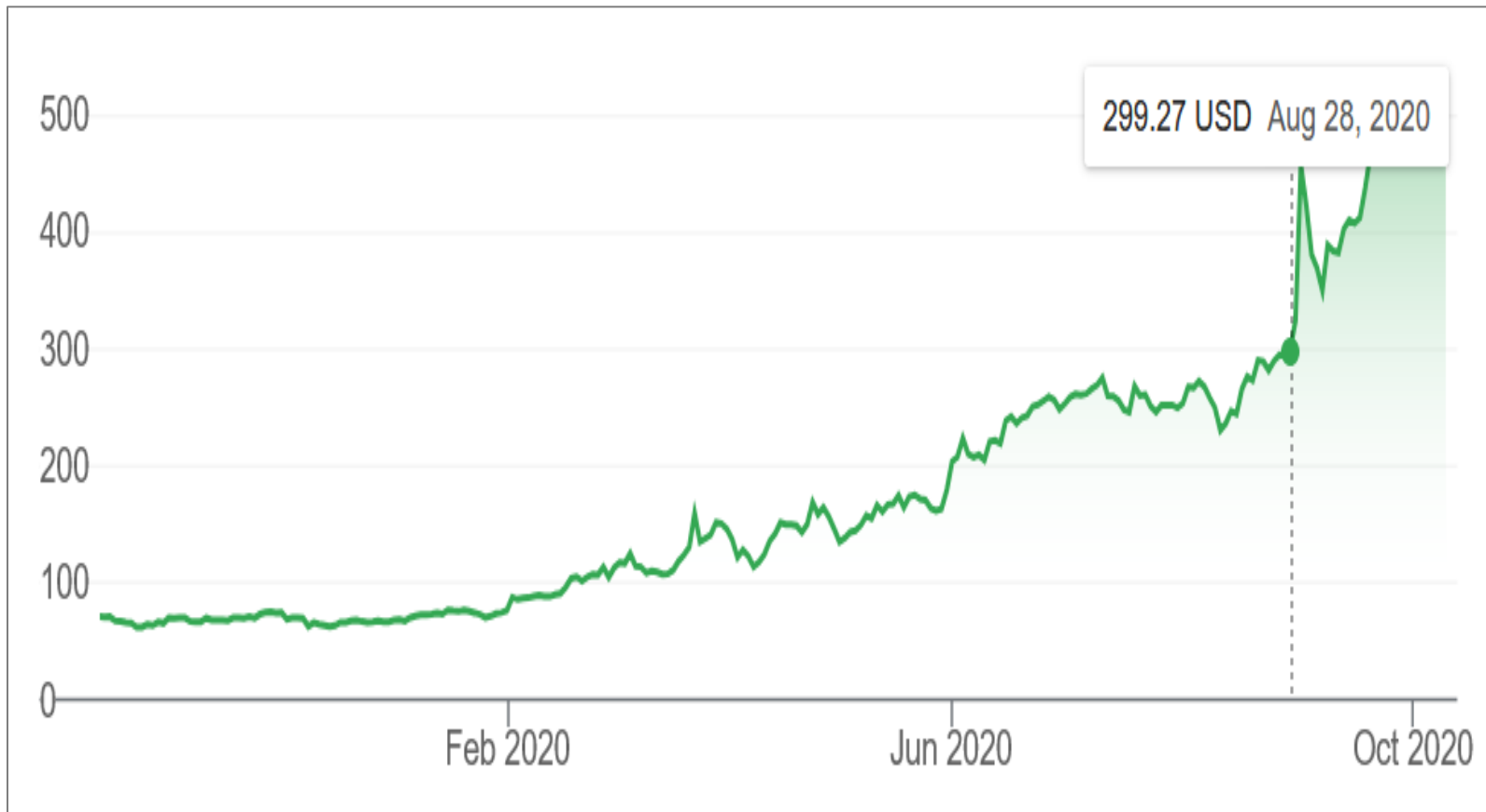
- **A change in expected future profits.**
  - If something makes people expect lower future profits, that should be associated with a lower stock price.
  - The lower expected profits could apply to a particular firm or to firms in general.
  - People can develop irrational exuberance about future profits (1929 bubble, dot-com bubble of 2000)

# S&P 500 and the Pandemic



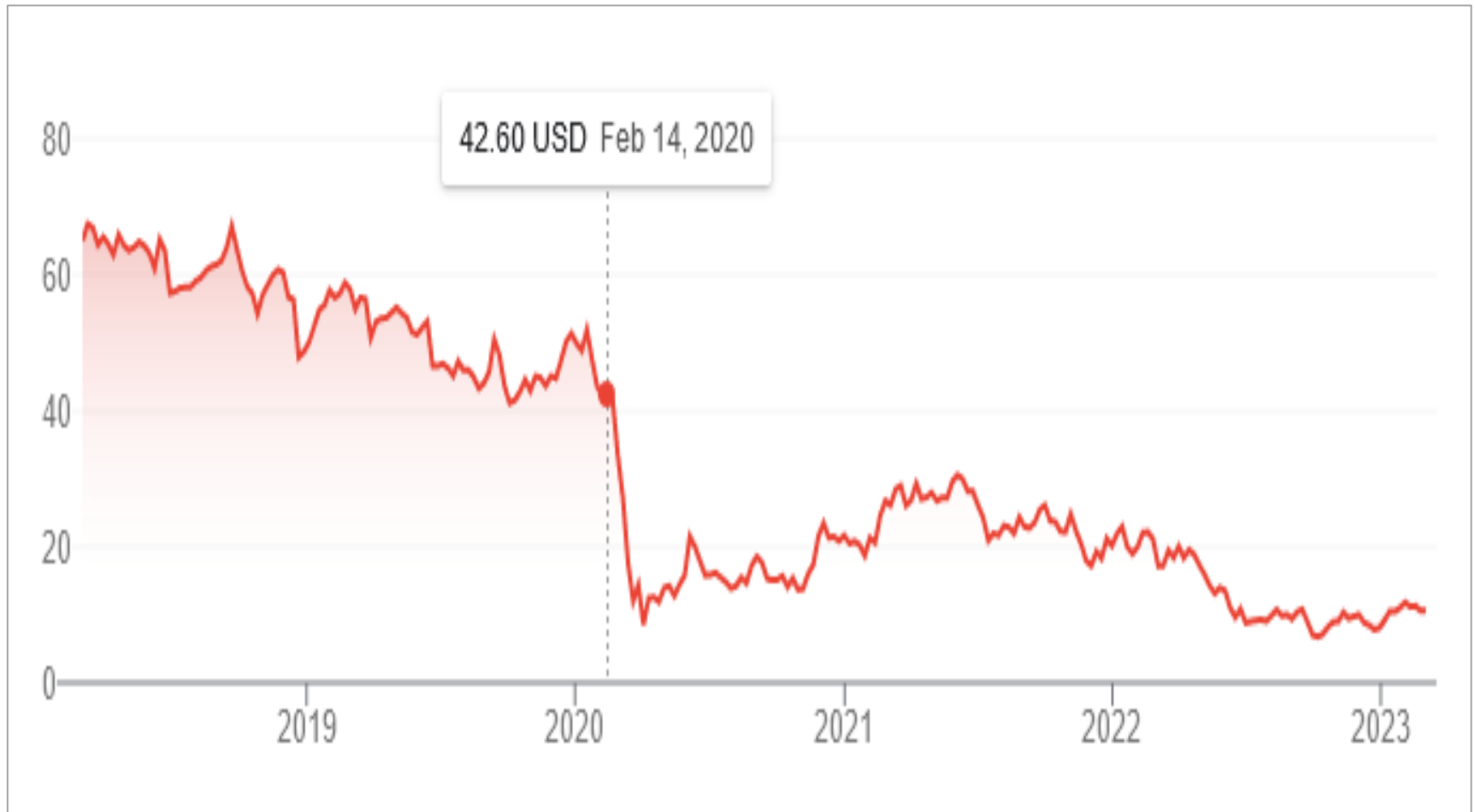
S&P500 is an index that represents the value of the largest 500 US companies (about 80% of the value of all the 5000 US companies listed on stock exchange)

# Zoom Stock Price



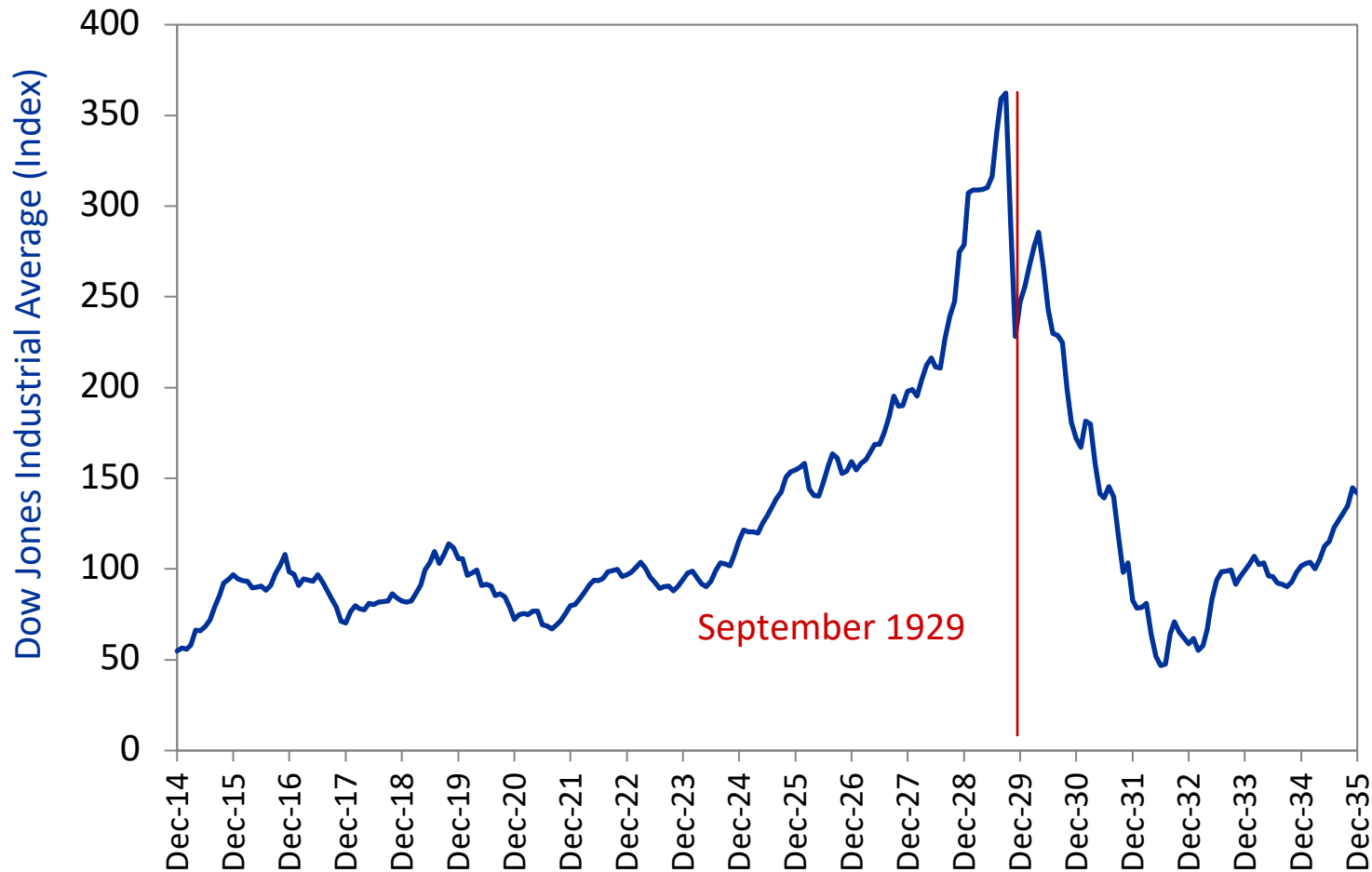
Source: Google Finance: zoom reported extraordinary 2<sup>nd</sup> quarter profits on August 31, 2020 driving up stock price by 30%

# Carnival Cruise Stock Price



Source: Market Finance

# 1920s Stock Market Bubble



Bubble arises when asset prices get disconnected from future profits and when people buy the asset hoping that prices will keep increasing, until stockholders lose confidence, sell, and prices collapse

Market Summary > Bitcoin

67,487.32 USD

+ Follow

+67,033.33 (14,765.38%) ↑ all time

Oct 22, 8:14 PM UTC · [Disclaimer](#)

1D | 5D | 1M | 6M | YTD | 1Y | 5Y | Max



1 | BTC ▾ | 67487.32 | USD ▾

More about Bitcoin →

Feedback

Bitcoin price has increased by factor 100 from \$630 in Oct 2016 to \$67,500 in Oct 2024. Total bitcoin value is \$1.3T today (1/3 of Apple)

# Poll on Bitcoin

What do you think of bitcoin, the largest crypto currency? Current price of one bitcoin is \$67,500, a hundredfold increase over the last 8 years.

- A. Bitcoin is a scam, it should be prohibited
- B. Bitcoin seems risky, I don't want to touch it
- C. Bitcoin is the future and I'd love to own some.
- D. I would like to buy bitcoins and sell them later when they are worth even more
- E. I don't know or understand what bitcoin is

# Crypto Currencies and Bubbles

- Crypto currencies are a form of asset (modern analogy to gold mining)
- They are costly to produce (electricity and computers)
- They do not provide profits nor much services
- But they have subjective value to some people and many others buy it expecting prices to rise further
- This can lead to a **speculative bubble**. Bubble bursts when owners lose confidence the asset price will keep increasing and start selling in droves
- Examples: 1929 US stock market, dotcom bubble 2000, Tulip mania of 1630s Netherlands, crypto today?



# Efficient Markets Hypothesis

- It is difficult to make money off news in the stock market because information is processed very quickly
- Example of a common short-run scam:
  - An influencer quietly buys a specific stock then tells their followers the price will increase.
  - Followers buy the stock, leading to a temporary price surge. Scammer then quickly sells its stocks while price is abnormally high.
- But hard to influence stock prices for the long-run

# How economists manage their finances

- Avoid high interest debt (such as credit card) or pay it back in priority
- Have some cushion in your bank account for unexpected expenses
- Invest extra savings in a broad passive index of stocks (such as S&P500) rather than
  - betting on specific stocks (or bitcoin) is more risky
  - Managed funds charge a lot and do not deliver higher returns on average
- Save in subsidized retirement savings 401(k)s with your employer

# References

- [CORE-The Economy](#), Chapter 10.
- Principles of Economics, Chapters 21 and 33.