# A MACROECONOMIC APPROACH TO OPTIMAL UNEMPLOYMENT INSURANCE

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Paper available at https://www.pascalmichaillat.org/4.html

## BAILY-CHETTY THEORY OF OPTIMAL UI

- insurance-incentive tradeoff:
  - UI provides consumption insurance
  - but UI reduces job search
- two aspects of the debate are missing:
  - sometimes jobs may be unavailable
  - UI may affect job creation
- beacause the Baily-Chetty model is a partial-equilibrium model:
  - endogenous labor supply
  - but fixed labor market tightness

### THIS PAPER

- general-equilibrium model of optimal UI
  - endogenous labor supply
  - endogenous labor demand
  - equilibrium labor market tightness
- model captures 3 effects of UI:
  - UI may reduce job search
  - UI may alleviate rat race for jobs
  - UI may raise wages and deter job creation
- application: optimal UI over the business cycle



#### **UI PROGRAM**

- moral hazard: search effort is unobservable
- employed workers receive c<sup>e</sup>
- unemployed workers receive c<sup>u</sup>
- replacement rate R measures generosity of UI:
  - $-R \equiv 1 (c^e c^u)/w$
  - R = benefit rate + tax rate
  - workers keep fraction 1 R of earnings

#### LABOR MARKET

- measure 1 of identical workers, initially unemployed
  - search for jobs with effort e
- measure 1 of identical firms
  - post v vacancies to hire workers
- CRS matching function: l = m(e, v)
- labor market tightness:  $\theta \equiv v/e$

## MATCHING PROBABILITIES

vacancy-filling probability:

$$q(\underline{\theta}) \equiv \frac{l}{v} = m(\frac{1}{\theta}, 1)$$

job-finding rate per unit of effort:

$$f(\theta) \equiv \frac{l}{e} = m(1, \theta)$$

• job-finding probability:  $e \cdot f(\theta) < 1$ 

## MATCHING COST: $\rho$ RECRUITERS PER VACANCY

- employees =  $\left[1 + \tau(\theta)\right]$  · producers
- proof:

employees producers recruiters 
$$l = n + \rho \cdot v$$

$$l = n + \rho \cdot \frac{l}{q(\theta)}$$

$$l = \left[1 + \frac{\rho}{q(\theta) - \rho}\right] \cdot n$$

$$\equiv 1 + \tau(\theta)$$

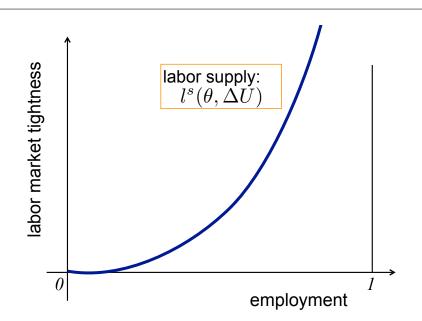
### REPRESENTATIVE WORKER

- consumption utility U(c), search disutility  $\psi(e)$
- utility gain from work:  $\Delta U \equiv U(c^e) U(c^u)$
- solves  $\max_{e} \{ U(c^{u}) + e \cdot f(\theta) \cdot \Delta U \psi(e) \}$
- effort supply  $e^{s}(\underset{+}{\theta}, \underset{+}{\Delta U})$  gives optimal effort:

$$\psi'(e^{S}(\theta, \Delta U)) = f(\theta) \cdot \Delta U$$

• labor supply  $l^{s}(\underline{\theta}, \underline{\Delta U})$  gives employment rate:

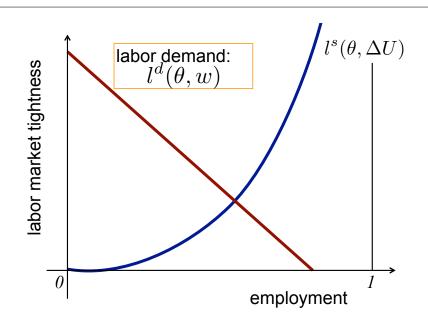
$$l^{S}(\theta, \Delta U) = e^{S}(\theta, \Delta U) \cdot f(\theta)$$



### REPRESENTATIVE FIRM

- hires *l* employees
  - $n = l/[1 + \tau(\theta)]$  producers
  - -l-n recruiters
- production function: y(n)
- solves  $\max_{l} \{y(l/[1+\tau(\theta)]) w \cdot l\}$
- labor demand  $l^d(\underline{\theta}, \underline{w})$  gives optimal employment:

$$y'\left(\frac{l^d}{1+\tau(\theta)}\right) = [1+\tau(\theta)] \cdot w$$



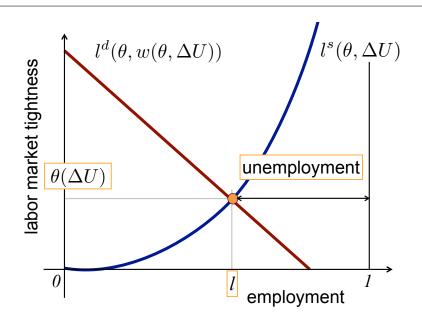
## LABOR-MARKET EQUILIBRIUM

- as in any matching model, need a price mechanism
  - general wage schedule:  $w = w(\theta, \Delta U)$
- tightness equilibrates supply & demand:

$$l^{s}(\theta, \Delta U) = l^{d}(\theta, w(\theta, \Delta U))$$

• equilibrium tightness:  $\theta(\Delta U)$ 

## LABOR-MARKET EQUILIBRIUM



## SUFFICIENT-STATISTIC FORMULA

FOR OPTIMAL UI

## **GOVERNMENT'S PROBLEM**

choose ∆U to maximize welfare:

$$SW = l \cdot U(c^{e}) + (1 - l) \cdot U(c^{u}) - \psi(e)$$

subject to budget constraint:

$$y\left(\frac{l}{1+\tau(\theta)}\right) = l \cdot c^{e} + (1-l) \cdot c^{u}$$

- to workers' response:  $e = e^{S}(\theta, \Delta U) \& l = l^{S}(\theta, \Delta U)$
- and to equilibrium constraint:  $\theta = \theta(\Delta U)$

## CONDITION FOR OPTIMAL UI

- express all the variables as a function of  $(\theta, \Delta U)$
- government solves  $\max_{\Delta U} SW(\theta(\Delta U), \Delta U)$
- first-order condition:

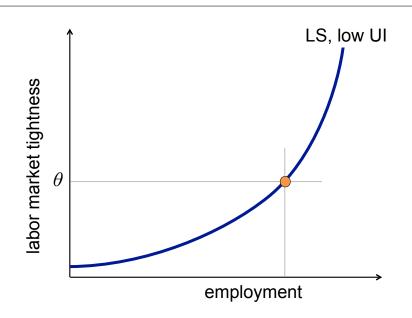
$$0 = \frac{\partial SW}{\partial \Delta U}\Big|_{\theta} + \underbrace{\frac{\partial SW}{\partial \theta}\Big|_{\Delta U} \cdot \frac{d\theta}{d\Delta U}}_{\text{Baily-Chetty formula}} + \underbrace{\frac{\partial SW}{\partial \theta}\Big|_{\Delta U} \cdot \frac{d\theta}{d\Delta U}}_{\text{correction}}$$

## **BAILY-CHETTY FORMULA**

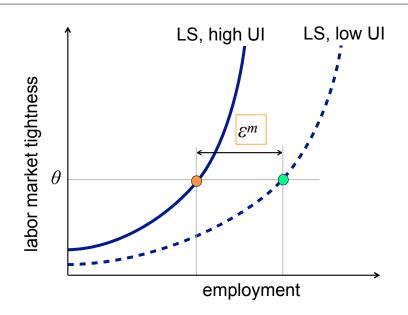
$$R = R^* \left( \epsilon^m, \frac{U'(c^u)}{U'(c^e)} \right)$$

- $\epsilon^m > 0$ : microelasticity of unemployment wrt UI
  - measures disincentive from search
  - $R^*$  is decreasing in  $\epsilon^m$
- $U'(c^u)/U'(c^e) > 1$ : ratio of marginal utilities
  - measures need for insurance
  - $R^*$  is increasing in  $U'(c^u)/U'(c^e)$

## MICROELASTICITY OF UNEMPLOYMENT



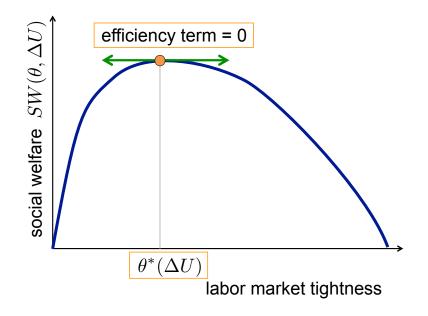
## MICROELASTICITY OF UNEMPLOYMENT



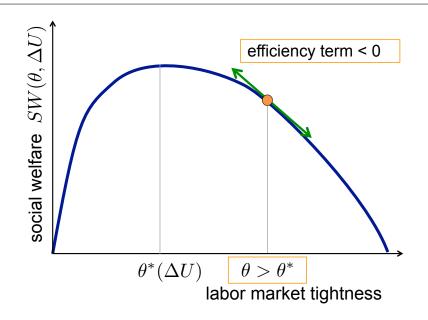
## $\partial SW/\partial heta|_{\Delta U}$ measured by efficiency term

- efficiency term depends on several sufficient statistics:
  - $\tau(\theta)$ : recruiter-producer ratio
  - u: unemployment rate
  - − 1 −  $\eta$ : elasticity of the job-finding rate  $f(\theta)$
  - ΔU: the utility gain from work

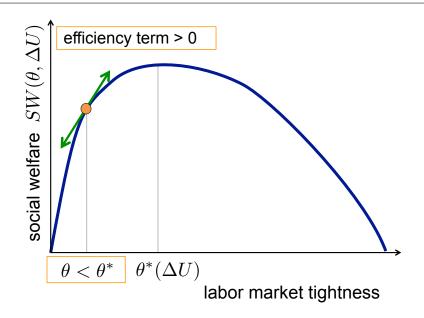
## EFFICIENCY TERM AND EFFICIENT TIGHTNESS



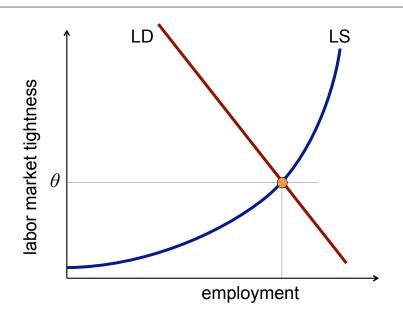
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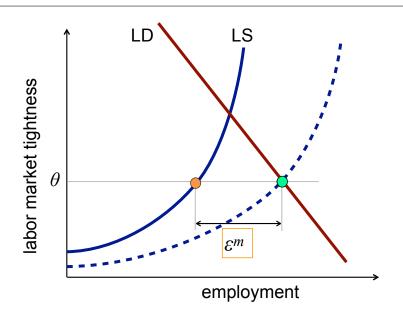
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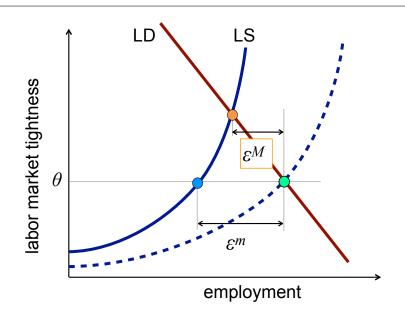
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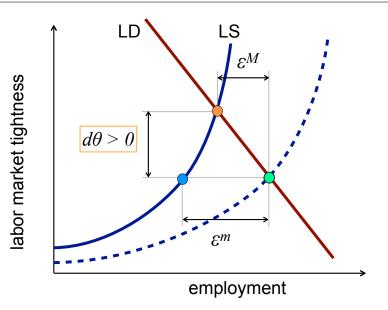
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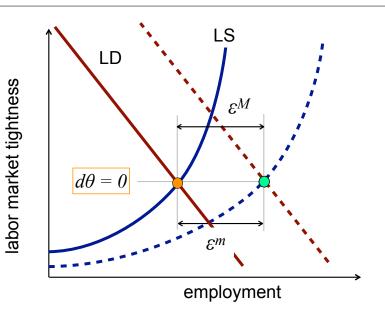
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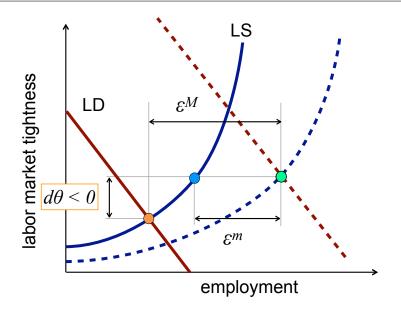
## $1-\epsilon^{M}/\epsilon^{m}$ gives effect of $\emph{UI}$ on heta



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## OPTIMAL UI FORMULA IN SUFFICIENT STATISTICS

$$R = R^* \left( \varepsilon^m, \frac{U'(c^u)}{U'(c^e)} \right) + \left( 1 - \frac{\varepsilon^M}{\varepsilon^m} \right) \cdot \text{efficiency term}$$
Baily-Chetty formula correction

## OPTIMAL UI VERSUS BAILY-CHETTY LEVEL

- optimal UI = Baily-Chetty if
  - UI has no effect on tightness:  $e^{M} = e^{m}$
  - or tightness is efficient: efficiency term = 0
- optimal UI ≠ Baily-Chetty if
  - UI affects tightness:  $e^M \neq e^m$
  - and tightness is inefficient: efficiency term ≠ 0

optimal UI > Baily-Chetty if UI pushes tightness toward efficiency

## OPTIMAL UI OVER THE BUSINESS CYCLE:

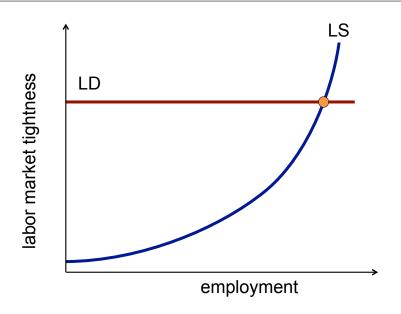
**THEORY** 

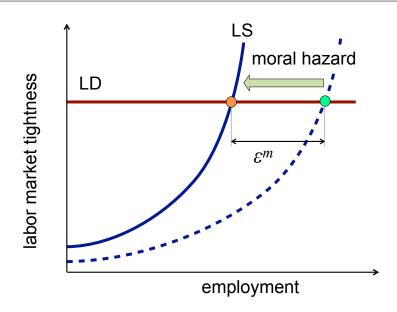
## THREE MATCHING MODELS

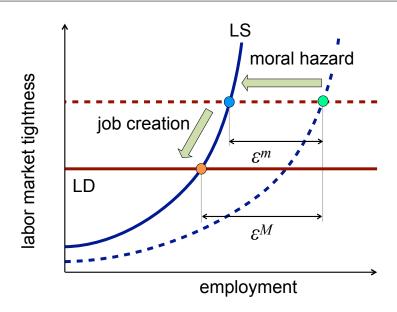
	model		
	standard	rigid-wage	job-rationing
prod. function	linear	linear	concave
wage	bargaining	rigid	rigid
reference	Pissarides [2000]	Hall [2005]	Michaillat [2012]

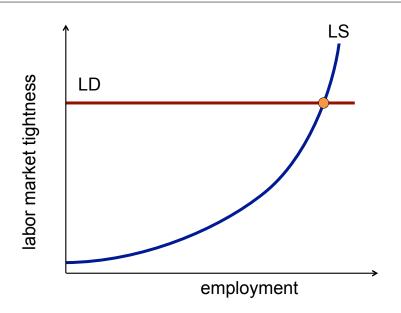
## **BUSINESS CYCLES IN THE MODELS**

- Baily-Chetty level is broadly constant
- $1 \epsilon^M/\epsilon^m$  has constant sign
- efficiency term changes sign over business cycle
  - under labor demand shocks
  - − > 0 in slumps and < 0 in booms</p>
  - generates cyclicality of optimal UI

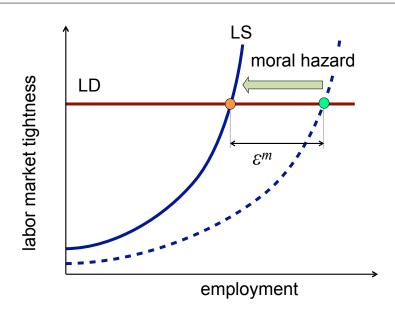


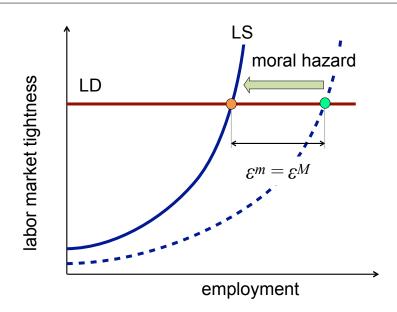




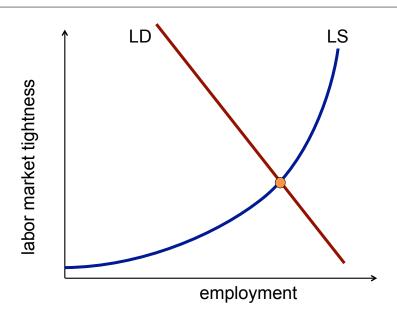


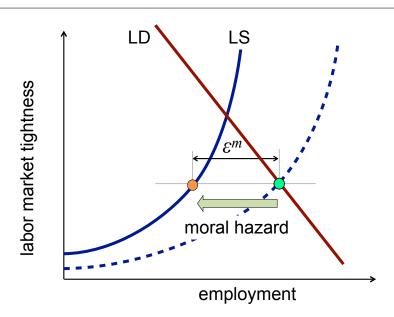
## RIGID-WAGE MODEL: $1-\varepsilon^M/\varepsilon^m=0$

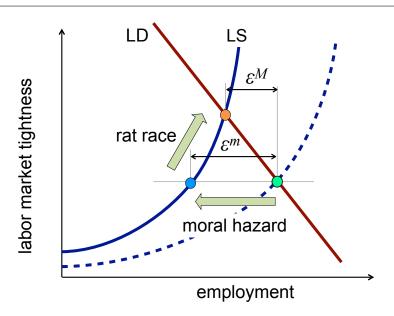




## Job-rationing model: $1 - \epsilon^M/\epsilon^m > 0$







#### CYCLICALITY OF OPTIMAL UI

- tightness is too low in slumps & too high in booms
- standard model: procyclical UI
  - moral hazard & job creation:  $1 \epsilon^M/\epsilon^M < 0$
  - UI should be reduced in slumps to stimulate tightness
- rigid-wage model: acyclical UI
  - only moral hazard:  $1 \epsilon^M / \epsilon^M = 0$
  - UI has no effect on tightness
- job-rationing model: countercyclical UI
  - moral hazard & rat race:  $1 \epsilon^M/\epsilon^m > 0$
  - UI should be raised in slumps to stimulate tightness

## OPTIMAL UI OVER THE BUSINESS CYCLE:

APPLICATION TO THE US

#### MICROELASTICITY OF UNEMPLOYMENT WRT UI

- many estimates of the microelasticity
- obtained by comparing identical jobseekers receiving different
   UI benefits in the same market
- plausible range of estimates:  $0.4 \le e^m \le 0.8$ 
  - estimates of the microelasticity of unemployment duration wrt potential duration of UI benefits
- key references:
  - Katz, Meyer [1990]
  - Landais [2015]

#### MACROELASTICITY OF UNEMPLOYMENT WRT UI

- few estimates of the macroelasticity
- obtained by comparing identical labor markets receiving different UI benefits
- plausible range of estimates:  $0 \le e^M \le 0.3$
- key references:
  - Card, Levine [2000]
  - Hagedorn et al [2016]
  - Chodorow-Reich, Coglianese, Karabarbounis [2019]
  - Dieterle, Bartalotti, Brummet [2020]
  - Boone et al [2021]

#### COMPARING MICROELASTICITY & MACROELASTICITY

• estimates obtained separately suggest  $1 - \epsilon^M/\epsilon^m > 0$ :

$$0 < \epsilon^{M} < 0.3 < 0.4 < \epsilon^{m} < 0.8$$

- implied range for the elasticity wedge: 0.25–1
  - lower bound:  $1 \epsilon^{M}/\epsilon^{m} = 1 0.3/0.4 = 0.25$
  - upper bound:  $1 \epsilon^M/\epsilon^M = 1 0/0.8 = 1$
- one exception: Johnston, Mas [2018] find  $1-\epsilon^M/\epsilon^m=0$  when they estimate  $\epsilon^m$  and  $\epsilon^M$  in MO data

#### **RESPONSE OF TIGHTNESS TO UI**

- Marinescu [2017] finds that an increase in UI raises tightness
  - corresponding elasticity wedge:  $1 \epsilon^{M}/\epsilon^{m} = 0.4$
- Levine [1993] & Farber, Valletta [2015] find that an increase in UI leads uninsured jobseekers to find jobs faster
  - → an increase in UI raises tightness

$$\rightsquigarrow 1 - \epsilon^M / \epsilon^m > 0$$

- evidence from Austria: Lalive et al [2015] find that an increase in
   UI raises tightness
  - corresponding elasticity wedge:  $1 \epsilon^{M}/\epsilon^{m} = 0.2$

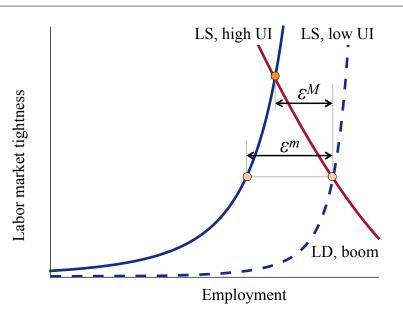
#### **RAT-RACE & JOB-CREATION CHANNELS**

- RCT evidence of rat-race mechanism:
  - negative spillover of more intense job search
  - Crepon et al [2013] in France
  - Gautier et al [2012] in Denmark
- no evidence of job-creation mechanism:
  - re-employment wages unaffected by UI
  - Krueger, Mueller [2016]
  - Marinescu [2017]
  - Johnston, Mas [2018]
  - also true in Austria: Card et al [2007]

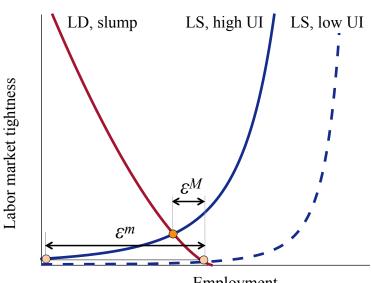
### Summary of the evidence: $1-\epsilon^{M}/\epsilon^{m} \approx 0.4$

- the evidence shows that  $1 \epsilon^M/\epsilon^M \ge 0$ 
  - reasonable median estimate:  $1 \epsilon^M / \epsilon^m = 0.4$
- the evidence supports the rat-race mechanism but not the job-creation mechanism
  - further support for  $1 \epsilon^M/\epsilon^m > 0$
- additional evidence suggests that the elasticity wedge may be larger in bad times
  - Valletta [2014]
  - Toohey [2017]

#### **ELASTICITY WEDGE IN GOOD TIMES**

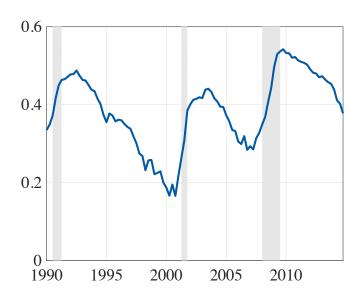


#### **ELASTICITY WEDGE IN BAD TIMES**

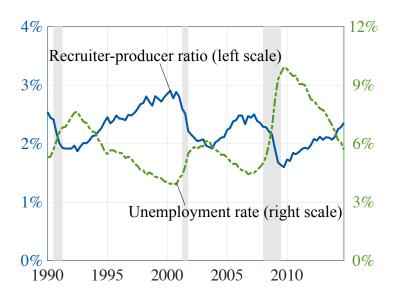


**Employment** 

#### **ELASTICITY WEDGE IN THE US**



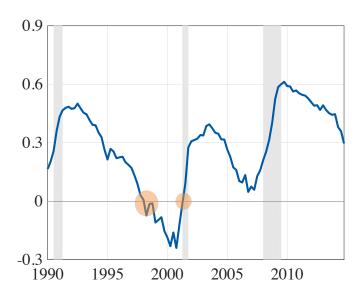
#### JOBSEEKING & RECRUITING IN THE US



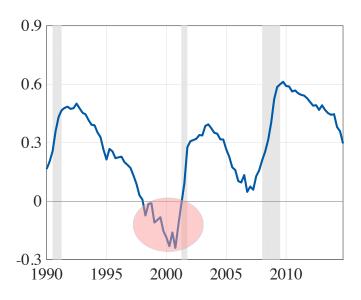
#### EFFICIENCY TERM IN THE US



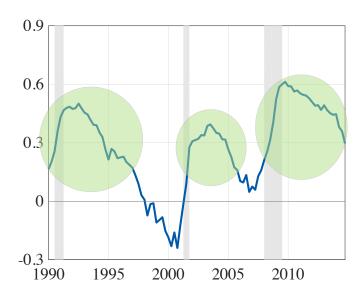
#### EFFICIENCY TERM = $0 \Rightarrow UI = BAILY-CHETTY$



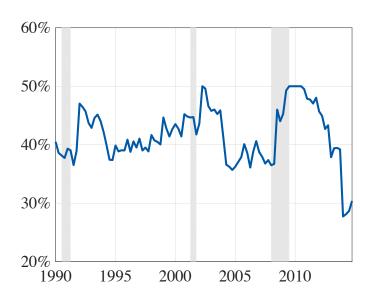
#### EFFICIENCY TERM $< 0 \Rightarrow$ UI < BAILY-CHETTY



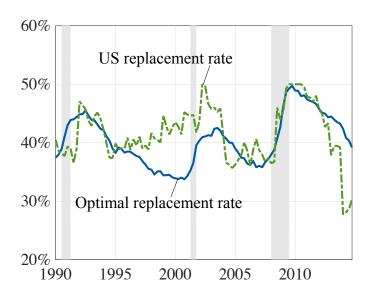
#### EFFICIENCY TERM $> 0 \Rightarrow UI > BAILY-CHETTY$



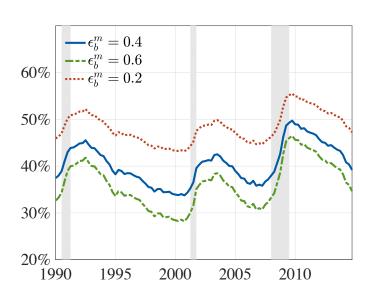
#### EFFECTIVE REPLACEMENT RATE IN THE US



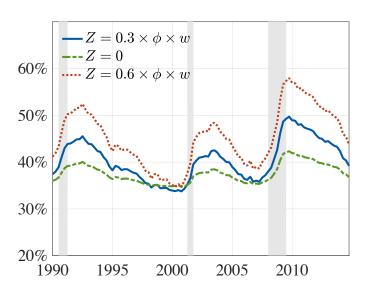
#### OPTIMAL REPLACEMENT RATE IN THE US



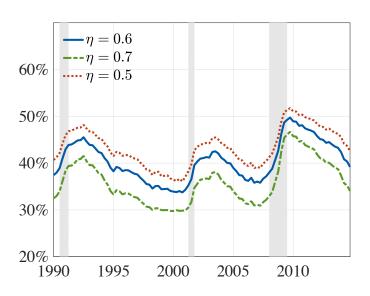
#### SENSITIVITY ANALYSIS: MICROELASTICITY



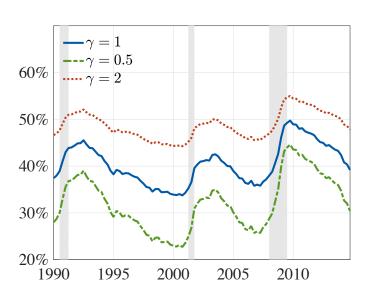
#### SENSITIVITY ANALYSIS: COST OF UNEMPLOYMENT



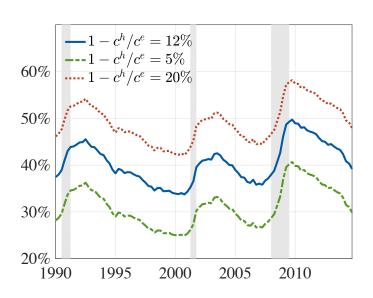
#### SENSITIVITY ANALYSIS: MATCHING ELASTICITY



#### SENSITIVITY ANALYSIS: RISK AVERSION



#### SENSITIVITY ANALYSIS: CONSUMPTION DROP



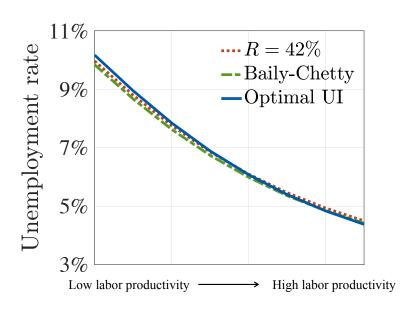
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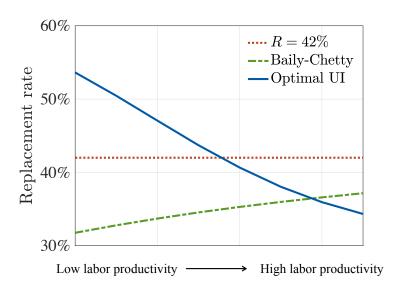
SIMULATIONS OF JOB-RATIONING MODEL

Parameter	Description	Source
$\alpha = 0.73$	Production function: concavity	$1-rac{arepsilon^M}{arepsilon^m}=0.4$
$\gamma = 1$	Relative risk aversion	Chetty [2006]
s = 2.8%	Monthly job-separation rate	CPS, 1990-2014
$\eta = 0.6$	Matching elasticity	Petrongolo,
		Pissarides [2001]
$\mu = 0.60$	Matching efficacy	$\theta = 0.43$
$\rho = 0.80$	Matching cost	$\tau = 2.3\%$
$\zeta = 0.5$	Real wage: rigidity	Michaillat [2014]
$\omega = 0.73$	Real wage: level	u = 6.1%
$\sigma = 0.17$	Disutility from home production: convexity	$\frac{d\ln(c^h)}{d\ln(c^u)} = 0.2$
$\xi = 1.43$	Disutility from home production: level	$1-\frac{c^h}{c^e}=12\%$
$\kappa = 0.22$	Disutility from job search: convexity	$\epsilon_b^m = 0.4$
$\delta = 0.33$	Disutility from job search: level	e = 1
z = -0.14	Disutility from unemployment	$Z = 0.3 \times \phi \times w$

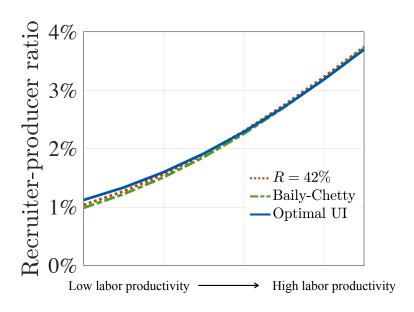
#### UNEMPLOYMENT RATE OVER THE CYCLE



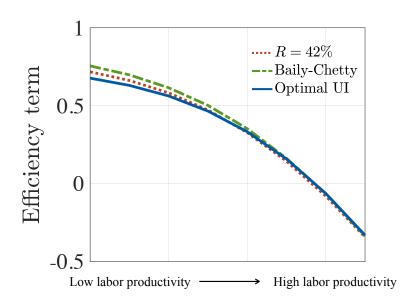
#### REPLACEMENT RATE OVER THE CYCLE



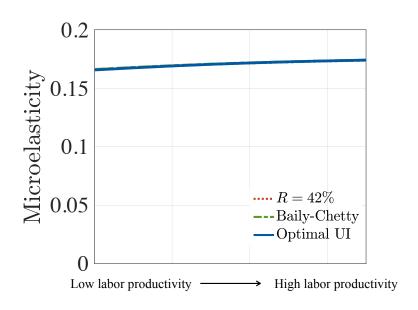
### RECRUITERS/PRODUCERS OVER THE CYCLE



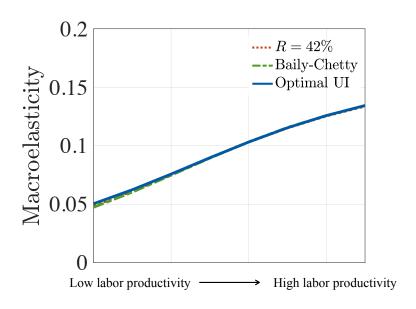
#### EFFICIENCY TERM OVER THE CYCLE



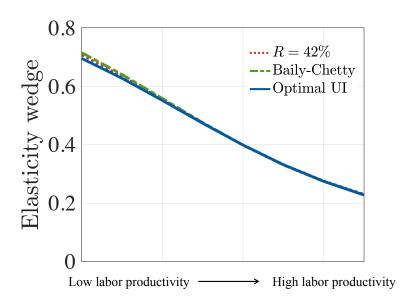
#### MICROELASTICITY OVER THE CYCLE



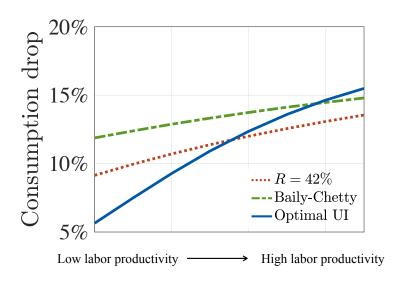
#### MACROELASTICITY OVER THE CYCLE



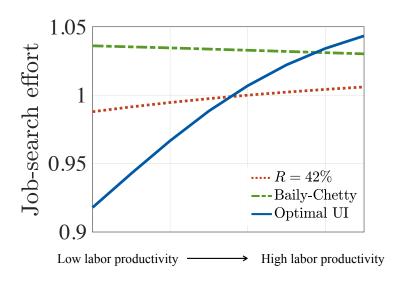
#### **ELASTICITY WEDGE OVER THE CYCLE**



#### CONSUMPTION DROP OVER THE CYCLE



#### JOB SEARCH OVER THE CYCLE



#### HOME PRODUCTION OVER THE CYCLE

