Jobs and Matches:
Quits, Replacement Hiring, and Vacancy Chains

Yusuf Mercan†
U Melbourne

Benjamin Schoefer‡
UC Berkeley

May 2019

Abstract
In the canonical DMP model of job openings, all job openings stem from new job creation. Jobs denote worker-firm matches, which are destroyed following worker quits. Yet, employers classify 56% of vacancies as quit-driven replacement hiring into old jobs, which evidently outlived their previous matches. Accordingly, aggregate and firm-level hiring tightly tracks quits. We augment the DMP model with longer-lived jobs arising from sunk job creation costs and replacement hiring. Quits trigger vacancies, which beget vacancies through replacement hiring. This vacancy chain can raise total job openings and net employment. The procyclicality of quits can thereby amplify business cycles.

†yusuf.mercan@unimelb.edu.au
‡schoefer@berkeley.edu

*First draft: May 2015. For comments we thank Steve Davis, Chris Edmond, Michael Elsby, Lawrence Katz, Patrick Kline, Simon Mongey and Lawrence Uren, and seminar participants at Federal Reserve Bank of San Francisco, UC Berkeley, University of Houston, Santa Clara University, 2018 briq Workshop on Firms, Jobs and Inequality and AASLE 2018 Conference. We thank Charlotte Oslund (BLS) for providing the historical BLS Labor Turnover Survey data at the monthly frequency.
1 Introduction

In matching models of the labor market, firms post vacancies to recruit workers into newly created jobs. A job is a match between a particular worker and particular firm, and disappears whenever that first match dissolves. This paper studies a more realistic notion of *longer-lived jobs that outlive matches*. Job openings then comprise new jobs as well as reposted old jobs.

A central and motivating contribution of this paper is our new, direct job-level evidence for replacement hiring: 56% of real-world job vacancies are for old jobs vacated by quits – rather than 100% new job creation as in the standard model. Our source is the IAB Job Vacancy Survey, in which German employers directly classify the nature of a given job opening, distinguishing such replacement hiring from creation of a new job. This composition is masked in standard, catch-all measures of vacancies. In an event study design, we estimate that at the establishment level, one incremental quit triggers almost perfect replacement hiring.

In the aggregate, quits, which are dramatically procyclical, comove nearly one to one with hires and job openings. Our paper explores the possibility that part of this comovement causally goes from quits to hiring. In fact, we construct a counterfactual time series of job openings and hires that shuts off procyclical replacement hiring: job openings and hiring would be much smoother, falling by a third less during recessions.

We then formally study the aggregate effects of longer-lived jobs and replacement hiring by introducing two parsimonious refinements into the textbook DMP model. First, some employed workers quit, accepting outside job offers.

Second, longer-lived jobs arise from a one-time, sunk job creation cost, not due when firms repost old jobs. Hence vacancies, once created, command a strictly positive equilibrium value, and firms optimally replacement-hire following quits. Intuitively, job creation corresponds to constructing a new office from scratch; replacement hiring is to fill an empty existing office. Zero job creation costs, implying zero value of vacancies and jobs as mere matches, nest the standard DMP model.

A *vacancy chain* emerges: quitters leave behind valuable vacant jobs, which firms repost, some of which are filled by employed job seekers, who in turn leave behind their old jobs, and so forth. Vacancies beget vacancies.

In equilibrium, replacement hiring and vacancy chains can raise employment by boosting total job openings. This aggregate net effect depends on the crowd-out response of new job creation, in our model guided by the adjustment cost parameter for new job creation. We conduct a meta study of 15 empirical studies, finding that such crowd-out appears very limited in the short run. For instance, temporary hiring boosts due to targeted policy incentives do not crowd out hiring by ineligible employers (Cahuc et al. (2017)), and sharp labor demand reductions by some employers do not lead other employers to expand in the short run in the same local labor market (e.g. Mian and Sufi (2014), Gathmann et al. (2018)), even among
tradables. Consequently, in the calibrated model, quit-driven replacement hiring partially passes through into total job openings, and ultimately into aggregate net employment.

By accommodating equilibrium net effects, our model also overcomes Robert Hall’s critique of the original fixed-jobs and pure-churn vacancy chains in Akerlof et al. (1988): “The explanation given for a vacancy chain [...] is defective because it does not recognize stochastic equilibrium. As long as the unemployment rate is not changing over time, the chain does not end when someone moves from unemployment to employment: that move has to be counter-balanced by another move from employment to unemployment, which keeps the chain going.” The aggregate net effects of our calibrated model are also consistent with the empirical causal effect of job-to-job transitions on net employment levels established by Shimer (2001) and Davis and Haltiwanger (2014) across U.S. states, for which our model’s vacancy chain mechanism therefore suggests a novel rationalization.

The model additionally implies amplification of business cycles that stems from the procyclicality of quits. In our model, recessions are times when fewer jobs open up because incumbents stay put, cutting short the vacancy chain and reducing job opportunities available to the unemployed, raising unemployment. In upswings, the tightening labor market pulls employed workers out of their matches, and the vacancies they leave behind add to the surge in vacancies, pushing down unemployment further than without replacement hiring.

We close by speculating that the trend decline in churn (Davis (2008), Davis and Haltiwanger (2014), Moscarini and Postel-Vinay (2016), Mercan (2018)) may, by determining the strength of the vacancy chain, amplify labor market fluctuations, consistent with the correlations in Gali and Van Rens (2017) for the U.S. Similarly, while worker flow rates in Germany – the context of our vacancy survey – are comparable to many OECD countries (Elsby et al. (2013)), replacement hiring may play an even larger role in higher-churn labor markets such as the U.S.


2 Replacement Hiring in the Data

(i) At the job level, surveyed employers classify the majority of job openings as replacement hiring. (ii) An establishment-level event study estimates essentially one new hire per quit. At the (iii) aggregate level, hiring and job opening time series tightly track quits, and (iv) they might be much smoother in a no-replacement-hiring counterfactual.

2.1 Job-Level Evidence on Replacement Hiring from an Employer Survey

A central contribution and motivation of the paper is our novel direct evidence on the prevalence of old jobs and replacement hiring in total job openings. Our source is a representative annual employer survey of 7,500 to 15,000 establishments from 2000 to 2015 (German IAB Job Vacancy Survey). We exploit a variable on the reason for the job opening, part of a section with details on the last filled job opening in the last 12 months. The bar chart in Figure 1 Panel (a) shows that 56% of job openings are posted in response to quits. Overall, we therefore are confident about our interpretation, but propose the clarifications below in the text. Of these, 47ppt [9ppt] are permanent [temporary]. Around 35% of vacancies target permanent net job creation, and around 8% in response to temporary demand increases. The composition is quite stable between 2000 and 2015 (Appendix Figure A1 Panel (a)).

2.2 Establishment-Level Effects of Quits on Hiring

At the establishment level, we estimate an almost one-to-one effect of quits on replacement hiring. We use another annual representative establishment panel survey (LIAB, from the

---

1The vacancy survey does not definitely distinguish quits from layoffs, but the connotation of examples given (e.g., maternity leave is offered as an example cause for temporary replacement hiring, and later survey rounds separate out retirement from permanent worker departures) suggests this quit interpretation.
German IAB), from 1993 to 2008, on annual cumulative gross flows by type (quits, layoffs, hires), a “German JOLTS”.\textsuperscript{2} We focus on hiring outcomes since the point-in-time vacancy variable comes with temporal mismatch, estimating an event study for establishment e’s year-t outcome for leads/lags $L \in \{0, 1, 2, 3\}$:

$$
\frac{\{\text{Hires}_{e,t}, \text{Job Openings}_{e,t}\}}{\text{Emp}_{e,t-1}} = \beta_0 + \sum_{s=-L}^{+L} \nu_s \frac{\text{Quits}_{e,t+s}}{\text{Emp}_{e,(t+s)-1}} + \alpha_e + \alpha_t + \epsilon_{e,t}. 
$$

(1)

$\nu_s$ measures the amount of (replacement) hires (or job openings) per quit at event time $s$. $\alpha_e$ [$\alpha_t$] are establishment [year] fixed effects.

Figure 1 Panel (b) plots the estimates (complemented by regression results in Appendix Tables A1 and A2).\textsuperscript{3} One incremental quit is associated with between 0.74 and 1.0 additional hires (p-value $< 0.1\%$). Cumulating coefficients around $t = 0$ would imply even larger replacement hiring effects. The small coefficients on the leads and lags confirm that replacement hiring occurs within the year of the quit, making reverse causality (past hires triggering quits) unlikely.

Moreover, the binned scatter plots in Appendix Figure A1 Panel (b) [(c)] reveal a strikingly linear shape of the replacement hiring [job posting] relationship, consistent with job-level replacement hiring, and motivating our model of atomistic firm-jobs rather than multi-worker firms in Section 3.\textsuperscript{4}

\subsection*{2.3 Time Series Comovement}

Figure 1 Panel (c) plots the U.S. time series of quits (count per month), job openings (point in time) and new hires (count per month), averaged at the quarterly frequency. Figure 1 Panels (d) and (e) plot the detrended versions (HP-filtered, smoothing parameter of 1600).\textsuperscript{5} Aggregate quit rates are highly procyclical, and comove around one to one with hiring and job vacancy rates. For example, during the Great Recession, monthly quits per 100 workers fell from 2.5 to 1.5. Job openings per 100 workers moved almost in lockstep, falling from 3.3 to 2, similarly for monthly hires. The post-2000 data are from Job Turnover and Layoff Survey (JOLTS) for the private sector; the earlier data are from the BLS Labor Turnover Survey (LTS), which covers the manufacturing sector. Appendix Figure A1 Panel (d) confirms similar aggregate cyclical patterns for Germany; Panel (e) [(f)] does so for quits and hires [job openings] in response to

\footnotesize
\begin{itemize}
\item \textsuperscript{2}We restrict our analysis to West Germany and establishments with at least 50 employees. We exclude extreme observations ($|d \ln \text{Emp}_{e,t}| > 40\%$ employment growth and $|\text{Quit}_{e,t}/\text{Emp}_{e,t-1}| > 20\%$ ).
\item \textsuperscript{3}Appendix Table A1 Panel B shows estimates for job openings consistent with the hiring effects if annualized (multiplied by 12, supposing one-month vacancy duration), but noisier likely because job openings are measured point-in-time.
\item \textsuperscript{4}Ancillary evidence by Isen (2013), Doran et al. (2016), and Jäger and Heining (2019) is consistent with one-to-one replacement hiring.
\item \textsuperscript{5}We have found similar results with the detrending procedure advocated by Hamilton (2018), with overall larger, yet proportional, amplitudes.
\end{itemize}

4
regional business cycles (municipalities).

2.4 Counterfactual Time Series Without Replacement Hiring

Building on the previous empirical facts, we next present reduced-form counterfactual time series that would arise absent replacement hiring fluctuations – i.e. if reposted vacancies were stable, and only new job creation fluctuated. We will study the equilibrium counterfactual in the cyclical analysis of the calibrated model in Section 4.4.

Total vacancies $v = r + n$ consist of reposted old jobs $r$ and new jobs $n$. Our job-level evidence suggests a share of reposted vacancies $\rho = \frac{r}{r+n} = 0.56$ in Germany. Percent deviations from trend in total vacancies are a $\rho$-weighted average of those in $r$ and $n$:

$$\frac{dv}{v} = \rho \frac{dr}{r} + (1 - \rho) \frac{dn}{n},$$

(2)

where in practice we study deviations from an HP trend with quarterly log time series (smoothing parameter of 1600).

The object of interest is the counterfactual vacancy time series that would mechanically emerge if $dr = 0$ at all points while $n$’s path remained unaffected. We back out new job creation as total-vacancy growth net of growth in repostings by rearranging identity (2), then proxying for reposted vacancies with worker quits (exploiting the one-to-one, linear replacement hiring estimated in Section 2.2):

$$\frac{dv}{v} = (1 - \rho) \frac{dn}{n} = \frac{dv}{v} - \rho \frac{dr}{r} \approx \frac{dv}{v} - \rho \frac{d\text{Quits}}{\text{Quits}}.$$

(3)

Figure 2 Panel (a) presents this counterfactual vacancy series along with the empirical one, relying on JOLTS quit and vacancy data from 2000 through 2018. The graph reveals amplification potential: during the Great Recession, total job openings would have only dropped by 20% instead of 30%. Panel (b) illustrates the smoothing predicted for hires. Panel (c) extends the vacancy time series to 1951 using the Help Wanted Index (Barnichon (2010)), confirming the role of replacement hiring in all post-War recessions.

The Role of Churn $\rho$  The amplification potential naturally depends on $\rho$, the share of reposted vacancies in total vacancies. Our baseline calibration to $\rho = 0.56$, from the German context, is likely a lower bound for higher-churn economies such as the U.S. A back of the envelope

---

To extrapolate the quit time series to the pre-JOLTS time period, we estimate an “Okun’s law” for quits. Specifically, we regress the quarterly JOLTS detrended log quit level on the detrended unemployment rate ($R^2 = 0.88$). We then project that estimated semi-elasticity ($-0.1$) onto the full unemployment time series.
extrapolation suggests a US ballpark $\rho^{\text{US}} \approx 0.9272$. Figure 2 Panels (a)-(c) plot this more speculative counterfactual, illustrating the potential range of amplification.

3 A Model of Jobs, Matches and Replacement Hiring

We introduce longer-lived jobs, a distinction between jobs and matches, and replacement hiring into the DMP model, and then study their equilibrium consequences quantitatively in Section 4.

**Preview** We add a one-time, sunk cost per new job created, $k(n_t)$, with $k'(n_t) \geq 0$, where $n_t$ denotes the number of new, initially vacant, jobs. The net value of a newly created job, $N_t$, is the value of a vacant job $V_t$ minus upfront cost $k(n_t)$: $N_t = V_t - k(n_t)$. Free entry for new job creation pushes equilibrium $N_t$ to zero, and hence if $k(0) > 0$, the equilibrium value of a vacant job is strictly positive:

$$V_t = k(n_t).$$

(4)

Here, when a worker-firm match dissolves that leaves the job intact, the firm optimally reposts the valuable vacancy – i.e. engages in replacement hiring. Jobs outlive matches.

Such longer-lived jobs render the vacancy stock $v_t$ predetermined, following law of motion:

$$v_t = n_t + (1 - q_{t-1})v_{t-1} + r_t,$$

(5)

where $q$ denotes the vacancy filling rate.

A *vacancy chain* emerges: vacancies can meet employed workers, who quit to switch jobs, leaving their jobs vacant, which firms optimally repost, and so forth. Vacancies beget vacancies. This vacancy chain can have aggregate net effects beyond churn, on total vacancies – depending

---

7Appendix Figure A1 Panel (d) highlights that German churn is an order of magnitude below the U.S. ones (since it represents annual hires while JOLTS is monthly), consistent with cross-country evidence on worker flows (Elsby et al. (2013)). Let $\rho^i = \frac{\rho^i}{r^i + n^i}$ denote the share of repostings in total job openings for country $i$. Under the approximation of one-to-one quit–replacement hiring, $\rho$ can be stated in terms of quit rate $Q^i$ and new-job-creation rate $N^i$: $\rho^i = \frac{Q^i}{Q^i + N^i}$, such that $N^i = Q^i[1/\rho^i - 1]$. Under the perhaps extreme assumption $N^i = N^j = N$, we can express: $\rho^i = \frac{Q^i}{Q^i + N} = \frac{Q^i}{Q^i + Q^i[1/\rho^i - 1]} = \frac{1}{1 + Q^i[1/\rho^i - 1]}$. For the US and Germany, $Q^\text{US}/Q^\text{DE} \approx 10$, and then $\rho^\text{DE} = 0.56$ implies $\rho^\text{US} = 0.9272$. 

---
on the response by new jobs:

\[
\frac{dv_t}{dr_t} = \left\{ \begin{array}{ll}
\epsilon[0,1] \\
\epsilon[-1,0]
\end{array} \right\} \frac{dn_t}{dr_t} + 1.
\]

(6)

In our model, this “crowd-out” \( \frac{dn_t}{dr_t} \) is guided by the shape of job creation cost \( k(n_t) \). Since empirical crowd-out – we show in Section 4.3 – appears small in the short run, replacement hiring passes through into total job openings, some of which are filled by the unemployed, hence raising aggregate net employment.

3.1 Environment

Time is discrete. There is a unit mass of workers, with risk neutral preferences and discount factor \( \beta \), who are either employed or unemployed. There is a larger mass of potential firm entrants. Firms are single-worker jobs, owned by workers.

Jobs, Matches, Separations and Vacancies

Jobs denote long-lasting entities that can be vacant or matched. Matches denote a job that is filled by a particular worker. In each period, jobs are exogenously destroyed with probability \( \delta \): the worker becomes unemployed, the job disappears forever without replacement hiring. Matches moreover dissolve with probability \( \sigma \) (the worker becomes unemployed), or through a worker job-to-job transition (described below). These jobs – vacated by what we label “quits” going forward – remain intact with probability \( \gamma \) and trigger replacement hiring (while \( 1 - \gamma \) of match dissolutions destroy the job).

Job Creation

One new job (aggregate count \( n \)) can be created at sunk cost \( k(n) \). If \( k(n) > 0 \), firms will repost jobs vacated by quits. All vacancies also require the standard per-period maintenance cost \( \kappa \).

Matching

Both unemployed and employed workers look for jobs. Employed workers search with intensity \( \lambda \) relative to unemployed workers. Meetings between vacancies and workers follow a constant returns matching function \( M(s, v) < \min\{s, v\} \). Labor market tightness \( \theta = \frac{v}{s} \) is the ratio of vacancies \( v \) to searchers \( s = u + \lambda e \). The job [worker] finding probability for an unemployed (employed) worker [vacancy] is \( f(\theta) = \frac{M}{s} = M(1, \theta) (\lambda f(\theta)) \) [\( q(\theta) = \frac{M}{v} = M(1/\theta, 1) \)].

\( ^8 \)Fujita and Ramey (2007) use a similar cost to smooth out vacancy IRFs in a model without replacement hiring.
Timing  The timing of events within period $t$ is:

1. $s_t$, the state of the economy, is realized, including unemployment $u_t$ and beginning-of-period (inherited) vacancies $\tilde{v}_t$.\(^9\)

2. Employed workers consume a bargained wage $w_t$ and produce $y_t$, unemployed workers receive unemployment benefit $b$.

3. Firms create $n_t$ new jobs at cost $k(n_t)$ each, and pay flow cost $\kappa$ per vacancy. This determines total vacancies $v_t = \tilde{v}_t + n_t$ and market tightness $\theta_t = \frac{\nu_t}{u_t + \lambda(1-u_t)}$.

4. $f(\theta_t)u_t$ of unemployed workers find jobs, $\lambda f(\theta_t)e_t$ of employed workers switch jobs.

5. Fraction $\delta$ of jobs are exogenously destroyed; these workers become unemployed.

6. Fraction $\sigma$ of matches are exogenously dissolved; these workers become unemployed. Share $\gamma[1-\gamma]$ of jobs hit by EE quits or $\sigma$ shocks can be reposted as vacancies [are destroyed].

The law of motion for unemployment is:

$$u_t = \left(1 - (1 - \delta)(1 - \sigma)f(\theta_{t-1})\right)u_{t-1} + \frac{\delta(1 - u_{t-1})}{1 - (1 - \delta)\sigma(1 - u_{t-1})}.$$

Due to sunk cost $k(n)$, the vacancy stock is predetermined, with law of motion:

$$v_t = n_t + (1 - \delta) \left(1 - (1 - \sigma)q(\theta_{t-1})v_{t-1} + \gamma \left(\lambda f(\theta_{t-1})e_{t-1} + \sigma(1 - \lambda f(\theta_{t-1}))e_{t-1}\right)\right)$$

Below, we drop time subscripts and use primes (\('\)) to denote the next period.

3.2 Value Functions

Value functions are expressed recursively, after the aggregate state is realized (i.e. after subperiod 1).

---

\(^9\)Our experiments will comprise perfect foresight transition dynamics, so we do not make $s_t$ explicit here.
**Worker Problem**  The worker when unemployed consumes unemployment benefit $b$. She may match with a job, to start work next period (unless a match/job shock hits), or stays unemployed:

$$U(s) = b + \beta(1 - \delta)(1 - \sigma)f(\theta)\mathbb{E}[W(s')] + \beta(1 - (1 - \delta)(1 - \sigma)f(\theta))\mathbb{E}[U(s')].$$  \hspace{1cm} (9)

An employed worker consumes wage $w(s)$, and then may stay, or quit to another job, or become unemployed:

$$W(s) = w(s) + \beta(\delta + (1 - \delta)\sigma)\mathbb{E}[U(s')] + \beta(1 - \delta)(1 - \sigma)\left(1 - \lambda f(\theta) + \lambda f(\theta)\right)\mathbb{E}[W(s')].$$  \hspace{1cm} (10)

**Maximally Parsimonious On-the-Job Search**  We present a parsimonious version of job-to-job quits because its hard-wired unit-elasticity between job-to-job quit ($\lambda f(\theta)$) and unemployed job finding (UE, $f(\theta)$) turns out to produce empirically realistic quits, as shown in Panel (d) of Figure 2, where we plot the log deviations from trend of quarterly quit rate (based on the JOLTS) against the job finding rate (based on the CPS) of the unemployed (regression coefficient of UE on quit rates of 0.985, $R^2 = 0.77$).\footnote{CPS job-to-job transition measures (with short/no nonemployment spell) are slightly smoother than quits but include layoffs/job destruction, not exclusively quits.}

Appendix Section D presents a richer model that explicitly rationalizes job switching with heterogeneity in match quality, and features endogenous job search effort – with similar amplification results.

**Firm Problem**  Newly created jobs have value

$$N(s) = -k(n) + V(s).$$  \hspace{1cm} (11)

Once created, a vacancy carries value

$$V(s) = -\kappa + \beta(1 - \delta)\left[q(\theta)(1 - \sigma)\mathbb{E}[J(s')] + (1 - q(\theta)(1 - \sigma))\mathbb{E}[V(s')]\right].$$  \hspace{1cm} (12)

A vacancy incurs flow cost $\kappa$ and matches with a worker with probability $q(\theta)$, and otherwise stays vacant or is destroyed.

A filled job produces output $y$ and pays wage $w$. If the match separates ($\sigma$ shock or job-to-job quit), the job enters next period as a vacancy with probability $\gamma$ (and otherwise becomes destroyed and is worth 0), hence its value is:

$$J(s) = y - w(s) + \beta(1 - \delta)\left[\gamma(\sigma + (1 - \sigma)\lambda f(\theta))\mathbb{E}[V(s')] + (1 - \sigma)(1 - \lambda f(\theta))\mathbb{E}[J(s')]\right].$$  \hspace{1cm} (13)
Free Entry  Free-entry in job creation drives new-job values \(N(s) = -k(n) + V(s)\) to zero:

\[V(s) = k(n).\]  \hspace{1cm} (14)

3.3 Match Surplus and Wage Bargaining

The worker’s outside option is unemployment, *even for a job switcher*, who must renounce her old job before bargaining with the new employer (rather than permitting sequential bargaining as in Postel–Vinay and Robin (2002); our simplification is also used in Fujita and Ramey (2012)). Joint match surplus \(S(s)\) is

\[S(s) = J(s) - V(s) + W(s) - U(s).\]  \hspace{1cm} (15)

Wages are determined according to generalized Nash Bargaining with worker share \(\phi \in (0, 1)\) to maximize

\[(W(s) - U(s))^{\phi} (J(s) - V(s))^{1-\phi},\]  \hspace{1cm} (16)

implying linear surplus sharing, worker [firm] capturing share \(\phi [1 - \phi]\) of joint surplus \(S\): \(^{11}\)

\[
\phi S(s) = W(s) - U(s) \hspace{1cm} (18) \\
(1 - \phi)S(s) = J(s) - V(s). \hspace{1cm} (19)
\]

3.4 Stationary Equilibrium Definition

We solve the model in steady state. The stationary equilibrium of the model is a set of value functions \(W(s), U(s), J(s)\) and \(V(s)\), wage function \(w\), and new job creation \(n\) such that: (i) Worker and firm values satisfy Bellman Equations (9), (10), (12), and (13). (ii) Wage \(w\) maximizes Equation (16). (iii) Unemployment \(u\) and vacancies \(v\) follow the laws of motion (7) and (8). (iv) New job creation \(n\) satisfies free-entry condition (14).

3.5 Calibration

Panel (a) of Appendix Table A3 summarizes the calibration; Panel (b) reports the targeted moments and the model fit. We discuss below, formally and informally, how these target moments were obtained.
moments help identify the model parameters. Computational details are in Appendix B. We relegate the specification and calibration of job creation cost $k(n)$ to Section 4.

We start with standard DMP parameters set outside of the model. Our model period is a month. Discount factor $\beta = 0.9967$ targets an annual interest rate of 4%. Standard Cobb-Douglas matching function $M(s, v) = \mu s^{\eta} v^{1-\eta}$ features elasticity of matches with respect to total search effort $\eta$ and matching efficiency $\mu$. Unemployed (employed) job finding [vacancy filling] rate is $f(\theta) = \mu \theta^{1-\eta}$ ($\lambda f(\theta) = \lambda \mu \theta^{1-\eta}$) $[q(\theta) = \mu \theta^{-\eta}]$. We set $\eta = 0.5$, as standard. Inconsequential for our study of relative amplification, we set $\phi = 0.5$ (Hosios condition) and pragmatically $b = 0.9$ following Fujita and Ramey (2007), who in turn follow Hagedorn and Manovskii (2008) for sizable amplification.

GMM sets the remaining DMP parameters. Targeting a monthly UE rate of 45% (Shimer (2005)) with model counterpart $(1-\delta)(1-\sigma)f(\theta) = (1-\delta)(1-\sigma)\mu \theta^{1-\eta}$, yields $\mu = 0.6542$. Steady-state unemployment rate $\frac{EU}{EU+UE} = 5.7\%$ disciplines UE rate $\delta + (1-\delta)\sigma = 2.72\%$. Targeting job filling rate $(1-\delta)(1-\sigma)q(\theta) = 0.9$ (Fujita and Ramey (2007)) normalizes steady state market tightness $\frac{(1-\delta)(1-\sigma)f(\theta)}{(1-\delta)(1-\sigma)q(\theta)} = \theta = 0.45 = 0.5$. We then find a vacancy posting cost $\kappa = 0.1611$ consistent with free entry and this tightness, given job creation costs $k(n)$, discussed below. We pin down on-the-job search efficiency $\lambda = \frac{EE \text{ rate}}{UE \text{ rate}} = 0.056$, targeting an average monthly quit rate of 2.5% (CPS EE, Fujita and Nakajima (2016), and JOLTS quit rate). To separately identify match-separation $\sigma = 0.0051$ and job-destruction $\delta = 0.0222$ rates, we target a vacancy reposting share $\rho = \gamma(1-\delta)[\lambda f + \sigma(1-\lambda f)]e = 56\%$ (see Section 2.1).

4 Aggregate Effects of Replacement Hiring and Vacancy Chains

Job Creation Cost $k(n)$ We organize our discussion of the aggregate implications of replacement hiring and vacancy chains around job creation cost $k(n)$, specifying it in terms of deviations from steady state $\bar{n}$:

$$k(n) = k_1 + k_2 \times \frac{n - \bar{n}}{\bar{n}}. \quad (20)$$

$k_1$ guides (micro) replacement hiring by generating positively valued vacancies, which we discuss and calibrate first below. We then move to equilibrium aggregate consequences of replacement hiring by calibrating $k_2$, the degree to which hiring costs are increasing in $n$ e.g. due to adjustment costs.
4.1 Firm-Level Replacement Hiring

Free entry (14) implies that firms create vacancies until the “$k(n)$-profit” condition (replacing the standard DMP zero-profit) is satisfied in all periods:

$$\kappa + (1 - \beta(1 - \delta)) k_1 + \left(1 - \beta(1 - \delta)\right) \mathbb{E} \left[ \frac{n' - \bar{n}}{n - \bar{n}} \right] \frac{n - \bar{n}}{\bar{n}} k_2 = \beta(1 - \delta) q(\theta)(1 - \phi) \mathbb{E}[S(s')]. \quad (21)$$

Parameter $k_1 > 0$ ensures a positive ex-post value of vacancy in steady state. As a result, jobs vacated by quits are reposted. We set $k_1$ to 0.1, large enough to ensure that $k(n) > 0$ and thus $n > 0$ in all our subsequent experiments. Equilibrium entry condition (21) clarifies that $\kappa$ and $k_1$ affect steady state surplus similarly, and we let $\kappa = 0.1611$ be estimated to target normalized $\theta = 1/2$. We also set $\gamma = 1$ to match the $\sim 1.0$ (cumulative) estimate from Section 2.2.

4.2 Vacancy Chains

Our model features a vacancy chain, by which vacancies beget vacancies through quits and the associated replacement hiring. Formally, the chain tracks a single vacancy and all the additional vacancies it triggers by meeting employed workers (probability $1 - \Upsilon$), who quit and leave behind another vacancy, which we then track, and so forth. The chain ends when it meets an unemployed searcher (probability $\Upsilon = \frac{u}{u + \lambda(1 - u)}$), or is destroyed by a $\delta$-shock. The chain length $C$ counts these vacancies, obtained recursively:

$$\mathbb{E}[C] = 1 \cdot \left[ \delta + (1 - \delta) q \Upsilon \right] + (1 - \delta) q (1 - \Upsilon) (\mathbb{E}[C] + \gamma) + (1 - \delta) (1 - q) \mathbb{E}[C]$$

$$= \frac{\delta + (1 - \delta) q (\Upsilon + \gamma (1 - \Upsilon))}{1 - (1 - \delta)(1 - q \Upsilon)}. \quad (23)$$

In our calibrated model, this length is 1.88, i.e. one vacancy entails 0.88 vacancies in excess of itself.

4.3 Aggregate Equilibrium Effects

The vacancy chain is a microeconomic concept tracking the lifecycle of a single vacancy and its “offsprings”. To study the equilibrium implications of the vacancy chain, we consider a one-
time exogenous addition to the stock of inherited vacancies.\textsuperscript{13} Whether and how much such a vacancy “injection” actually adds to the total stock on net (and then affects other quantities) depends on the response in new job creation.

**Crowd-Out by New Job Creation: Model** The key response to a vacancy injection – and in fact the only contemporaneous one in the vacancy law of motion – stems from the crowd-out response by new job creation. In terms of beginning-of-period vacancy shifts $d\tilde{v}$, one additional vacancy is crowded out by $\frac{dn}{d\tilde{v}} \in [-1, 0]$, and on net raise the vacancy stock only by $(1 + \frac{dn}{d\tilde{v}}) \leq 1$. Crowd-out $\frac{dn}{d\tilde{v}}$ is an equilibrium outcome and depends on $k_2$, the increasing degree of hiring cost. In Panel (a) of Figure 3 we plot $\frac{dn}{d\tilde{v}}$ for various values of $k_2$, along with total-vacancy response $\frac{dv}{d\tilde{v}} = 1 - \frac{dn}{d\tilde{v}}$, where $dx = x_t - \bar{x}$ denotes level deviation from steady state. The simulated data plots the first-period (hence largest) response to a (beginning-of-period) “vacancy injection” $\epsilon_s^0$ shock:\textsuperscript{14}

$$v_t = n_t + (1 - \delta) \left( (1 - (1 - \sigma)q(\theta_{t-1}))v_{t-1} + \gamma(\sigma + (1 - \sigma)\lambda f(\theta_{t-1}))e_{t-1} \right) + \epsilon_s^0$$

In calculating the underlying impulse responses, we focus on perfect foresight transition dynamics following one-time, unanticipated shocks out of steady state, using a shooting algorithm (details in Appendix B.3). We plot and discuss the full impulse response functions (IRFs) for new job creation (and unemployment and vacancies) in Appendix Section C.

$k_2 = 0$ provides an extreme benchmark of perfect neutrality of vacancy inflows such as from replacement hiring: full crowd-out ($\frac{dn}{d\tilde{v}} = -1$) and no pass-through into total vacancies ($\frac{dv}{d\tilde{v}} = 0$), since $n$ adjusts such that $v^* = \theta^* \cdot n$, and $\theta$ remains – as in the standard DMP model – the equilibrating variable. Reposting then merely tilts the composition from new to old jobs in the economy, despite longer-lived jobs and reposting.

By contrast, for all $k_2 > 0$, replacement hiring has net effects on aggregate labor market outcomes. Intuitively, at the original $\bar{n}$, a vacancy injection incipiently lowers $V$ a lot (as $q$ falls and $w$ increases due to higher $\theta$), beyond the original free-entry-consistent $k(n)$. Free entry leads $n$ to fall, the process that drives the adjustment to the new equilibrium by again raising $V$ and, due to $k_2 > 0$, also lowering $k(n)$. The incidence between $k(n)$ and $V$ – whether new jobs fully restore the original total-vacancy level, and $V$ and $k(n)$ to the original levels – depends on the shape of $k(n)$. When $k'(n) > 0$ ($k_2 > 0$), the fall in new job creation stops “prematurely”, at a lower equilibrium $k(n) = V$, hence implying higher total job openings. Under $k_2 > 0$ [$k_2 \rightarrow \infty$], repostings are offset less than one to one [not at all] and thus pass through [completely] into total job openings and aggregate employment.

\textsuperscript{13} This ad-hoc experiment may capture, e.g., cyclical shifts in public employment or sectoral shocks.

\textsuperscript{14} The shock hits in period $t = 1$ (beginning of period), and is zero for all $t \neq 1$. We consider a shock small enough, specifically 1\% of steady state vacancy stock, to not crowd out $n_1$ below zero, although we have checked that crowd-out is quite stable in shock size.
Empirical Evidence for Crowd-Out, and Calibration of $k_2$  We calibrate $k_2$ by matching the model crowd-out to empirical targets. In Figure 3 Panel (b), we conduct a meta study and convert 15 suitable empirical studies into implied crowd-out measures. Strikingly, nearly every study points towards zero (if not positive) short-run crowd-out. For example, subsidies boosting hiring among eligible firms do not curb hiring by ineligible employers in the same labor market (Cahuc et al. (2017)), and sharp hiring (employment) reductions do not lead unaffected employers in the same local labor market to expand in the short run even within the tradable sector (e.g. Mian and Sufi (2014), Gathmann et al. (2018)). Some caveats apply to our extrapolation from local to aggregate crowd-out.\footnote{First, most studies do not differentiate between employment and hiring (although Cahuc et al. (2017) do and find similar estimates (Table 3)). Second, we do not rescale the spillover-treated (e.g. tradable) sector to the full labor market (e.g. by \(\text{Share Tradable}^{1}\)), which would further increase the positive estimates. Third, agglomeration forces may mask crowd-out (Moretti (2010), Gathmann et al. (2018)). Fourth, non-local other (e.g., capital) markets may imply larger crowd-out for national experiments. Fifth, mismeasured labor market overlaps may bias crowd-out away from \(-1\), although matching functions appear consistent across levels of aggregation (Petrongolo and Pissarides (2001)). Moreover, e.g. Gathmann et al. (2018) show robustness to year-industry-location cells.} Based on the preponderance of the evidence, we set $k_2 = 1$, still implying some crowd-out, $\frac{dn_t}{d\bar{v}} = -0.1183$.

Equilibrium Effects of Reposting: the Vacancy Multiplier  To investigate the dynamic equilibrium effects of a (one-time, perfectly transitory) vacancy injection $\varepsilon_1^{\bar{v}}$ such as arising from reposting, we define a vacancy multiplier, which cumulates the vacancy inflows generated by the shock (as deviations from steady state $\bar{v}_{s\text{inflow}}$) over horizon $h$,

$$M(h) = \sum_{s=1}^{h} \left( v_{s\text{inflow}} - \bar{v}_{s\text{inflow}} \right) / \varepsilon_1^{\bar{v}},$$  \hspace{1cm} (24)

where $v_{s\text{inflow}} = n_s + (1 - \delta)\gamma(\sigma + (1 - \sigma)\lambda f(\theta_{s-1}))e_{s-1} + \varepsilon_1^{\bar{v}}$ captures the total inflow of newly created and reposted vacancies (with $\varepsilon_1^{\bar{v}} = 0 \forall s \neq 1$).

In addition, we decompose the multiplier. First, we plot the “one-only” multiplier that would arise if only one of the variables shifted (the rest held at steady state). Second, we plot the “all-but-one” complementary multiplier: if all variables adjusted except for the variable of interest kept at its steady state.

Figure 4 Panel (c) (impulse response in companion Panel (a)) reveals that the equilibrium multiplier reaches around 1.37. The immediate vacancy pass-through in period one is 0.88 = 1 + $\frac{dn_t}{d\bar{v}}$, and after 3 (6) [12] months the multiplier has reached 1.03 (1.16) [1.29]. The first implication is the positive level: rather than being crowded out as in the standard DMP model, an exogenous vacancy injection raises the aggregate vacancy stock. This result motivates our discussion of business-cycle amplification in Section 4.4 below.

Second, the multiplier exceeds 1.00, implying that the model features amplification akin to the micro vacancy chain: a given vacancy injected into the economy “generates” an additional 0.37
vacancies in excess of itself. The “one-only” decompositions in Panel (c) clarify that much of the multiplier is due to the job finding boost – the equilibrium analogue of the micro vacancy chain. Still, at 1.37 the equilibrium multiplier remains below the micro vacancy chain (1.88), confirming the importance of the equilibrium perspective. Here, the “all-but-one” decomposition Panel (d) (IRFs in (b)) clarifies that crowd-out by new job creation is the culprit: if \( n \) were held at steady state, the multiplier would reach around 2.25, even exceeding the micro vacancy chain (1.88). Hence our limited crowd-out calibration of \( k_2 \) leaves new job creation with a quantitatively important role.

Appendix Figure A4 illustrates the larger multiplier in an economy with lower crowd-out of 5.95% (rather than 11.83%, using \( k_2 = 3.1 \)).

4.4 Business Cycle Implications

We close with a natural application: amplification of business cycle shocks stemming from the dramatic procyclicality of quits and hence of replacement hiring, as foreshadowed in the empirical counterfactual in Section 2.4.

Figure 5 presents the impulse responses from three experiments. To isolate the incremental amplification from the vacancy multiplier, we juxtapose our model (green solid lines) with two benchmarks that deactivate it, but otherwise feature the same steady state and adjustment costs. (While \( k_2 = 0 \) would generate neutrality, it would also shut off adjustment cost \( k'(n) \), independently generating amplification. While \( \gamma = 0 \) would shut off reposting, it would also change steady-state flows, surplus and the discounting of the shock process.)

First, in the “no (incremental) reposting economy” (blue dashed lines), we artificially hold acyclical (at steady state) any fluctuations in reposting inflows in the vacancy law of motion.\(^{16}\) Second, we add a “full crowd-out economy” (red dash-dotted lines), where vacancy creation costs \( k(\cdot) \) depend on total vacancy inflows rather than only newly created job openings \( n \), generating full crowd-out as new and reposted inflows are perfect substitutes therein.\(^{17}\)

**Aggregate Productivity** The first row of Figure 5 presents IRFs to productivity shocks (Shimer (2005), Hagedorn and Manovskii (2008); similar results for discount factor shocks (Hall (2017)), where \( y \) increases exogenously by 1.5% at \( t = 1 \) (log persistence \( \rho_z = 0.975 \), following Fujita and Ramey (2007)).

Higher productivity stimulates job creation. Labor market tightness and job finding rates increase, lowering unemployment but also raising job-to-job quits. In the full model, the quitters leave vacancies behind, boosting total vacancies, some of which the unemployed fill, amplifying

\(^{16}\) Here perhaps an unmodelled actor neutralizes reposting fluctuations by adding and subtracting to \( \delta \) (but not to \( n_t \)) to obtain: \( v_t = n_t + (1 - \delta)(1 - (1 - \sigma)q(\theta_{t-1}))v_{t-1} + \gamma(\sigma + (1 - \sigma)\lambda f(\bar{\theta})\bar{e}) \).

\(^{17}\) Specifically, creation costs become \( k(\cdot) = k_1 + k_2 \frac{\bar{e}_t}{\bar{e}_{t-1}} \), where inflows \( \iota_t = n_t + \gamma(\sigma + (1 - \sigma)\lambda f(\bar{\theta}_{t-1}))\bar{e}_{t-1} \).
the unemployment response. The amplification from the vacancy chain becomes clear when compared to the smoother no-incremental-reposting variant (where repostings do not enter) and in the full-crowd-out economy (where repostings exist but are fully crowded out). These two economies only differ in $n$, where the absence of reposting forces new job creation to adjust total vacancies.

A relative response of the economies with and without reposting isolates the incremental amplification potential of the mechanism. As an amplification statistic, we consider the peak of the cycle in the reposting economy, where the unemployment rate is 4.0% below trend, while in this period the unemployment rate is 3.2% below trend in the no-reposting economy, i.e. 0.8ppt lower. That is, the reposting mechanism provides $\frac{0.8}{3.2} = 25\%$ relative amplification. We have confirmed that this relative statistic is invariant to the absolute amplification (conditional on a given crowd-out level), which can be scaled arbitrarily by e.g. shifting $b$ (e.g., Hagedorn and Manovskii (2008), Ljungqvist and Sargent (2017)).

By contrast, lowering crowd-out (by adjusting $k_2$) dramatically increases relative amplification. Figure 3 left Panel plots this relative amplification statistic as a function of crowd-out-guiding parameter $k_2$. Appendix Figure A5 illustrates the cyclical behavior in an economy with half the crowd-out of our baseline model (i.e. 5.95% rather than 11.83%, using $k_2 = 3.1$ rather than one). Here, this amplification statistic rises to 77.1%.

**On-the-Job Search and Quits** In the second row of Figure 5, we increase on-the-job search efficiency $\lambda$ by 1% at $t = 1$ (returning to its steady state level at rate $\rho_\lambda = 0.975$).

Vacancies increase through a conventional “labor supply” channel by facilitating vacancy filling (lowering labor market tightness $\theta = \frac{\text{Job Openings}}{\text{Unemployed + On-the-job Searchers}}$, as in e.g. Shimer (2001), Krause and Lubik (2006), Nagypál (2008), Eeckhout and Lindenlaub (2018), and Moscarini and Postel-Vinay (2018)). In the no-reposting model, new job creation achieves this vacancy increase. In the full crowd-out model, new job creation actually falls to offset the surge in repostings. $n$ is stable in the full model on net, balancing limited crowd-out with the labor supply channel. Interestingly, due to random search, the employed searchers crowd out their unemployed peers, dramatically raising unemployment in the models without the vacancy chain and with full crowd-out. By contrast, the full model nearly eliminates this spillover, as the job-to-job quitters free up job opportunities for the unemployed.

**Matching Efficiency** The last row of Figure 5 raises matching efficiency $\mu$ by 1% (persistence $\rho_\mu = 0.975$), discussed as a potential cyclical driver in e.g. Barnichon and Figura (2011), Davis et al. (2013), Cheremukhin and Restrepo-Echavarria (2014), and Furlanetto and Groshenny (2016).

Higher matching efficiency stimulates job creation and – unlike the asymmetric $\lambda$ shock – lowers unemployment. But faster matching also depletes the vacancy stock. Replacement hiring replenishes the vacancy stock, pushing the unemployment rate even lower. Interestingly,
the no-reposting economy has a strong new job creation response, whereas the full-crowd-out economy spikes and then sharply drops.

5 Conclusion

Our paper has presented evidence on the role of quits and replacement hiring in the behavior of job openings. We have integrated these features into a matching model that distinguishes between short-lived worker-firm matches, and longer-lived jobs that persist even after a given match dissolves. In our model, quits trigger vacancies, which in turn beget other vacancies through replacement hiring.

Amplification arises, as during recessions incumbents hold on to their jobs, cutting short the vacancy chain and the job opportunities available to the unemployed, raising unemployment. Conversely, in upswings, the tightening labor market pulls workers out of their matches, leaving behind additional jobs for the unemployed to fill.

The amplification potential of the vacancy chain falls in the degree of short-run crowd-out between the reposted vacancies for old jobs, and new job creation. Our meta study of employment spillover estimates suggests this crowd-out to be low.
References


Cahuc, Pierre, Carcillo, Stéphane, and Barbanchon, Thomas Le (2017). “The Effectiveness of Hiring Credits”.

Cerqua, Augusto and Pellegrini, Guido (2018). “Local Multipliers at Work”.


Jäger, Simon and Heining, Jörg (2019). “How Substitutable are Workers? Evidence from Worker Deaths”.


Figure 1: Replacement Hiring in the Data

(a) Composition of Job Openings in Germany

Notes: Panel (a): Composition of job openings (last filled job at establishment) by reason, 2000-15 averages. The temporary category includes seasonal factors. New job creation is phrased as a labor-demand increase ("Mehrbedarf"); replacement hiring is literal translation ("Ersatz"), where the temporary category includes maternity leave and sickness. The survey excludes apprentices, "mini-jobs", contract renewals or temp.-to-perm. switches, temp workers, and subsidized ("1 euro") jobs. Source: IAB Job Vacancy Survey.

(b) Event Study of Hires following Quits

Notes: Panel (b): Establishment level event study of hires (per year) on quits (per year). We plot 95% confidence bands for the 3-lag/lead specification, estimating regression model (1), detailed in text. Source: IAB LIAB.

(c) U.S. Time Series of Job Openings, Hires and Quits

Notes: Panel (c): Time series of quarterly averages of monthly data on job openings (point in time), and hires (count per month) and quits (count per month), all as rates (per 100 employees); Panels (d) and (e) plot detrended versions (HP-filtered with parameter 1600). Sources: BLS Labor Turnover Survey and JOLTS.

(d) Cyclicality of Job Openings and Quits

Notes: Panel (d): Establishment level event study of hires (per year) on quits (per year). We plot 95% confidence bands for the 3-lag/lead specification, estimating regression model (1), detailed in text. Source: IAB LIAB.

(e) Cyclicality of New Hires and Quits

Notes: Panel (e): Establishment level event study of hires (per year) on quits (per year). We plot 95% confidence bands for the 3-lag/lead specification, estimating regression model (1), detailed in text. Source: IAB LIAB.
Figure 2: Counterfactual Time Series and Quit Cyclicality

(a) Counterfactual Job Openings

(b) Counterfactual Hires

(c) Counterfactual Job Openings - HWI

(d) Cyclical component of UE job finding rates (CPS, our construction) and quit rates (JOLTS, count of quits per month per 100 employees). A regression reveals a linear coefficient of UE on quit rates of 0.985 ($R^2 = 0.77$).

Notes: All time series are quarterly, logged and HP-filtered with smoothing parameter $\lambda = 1600$. Consistent with the decomposition exercise, they are in levels (counts), rather than rates (per 100 workers). The monthly time series (JOLTS, CPS) have been averaged at the quarterly frequency. Panel (a): Actual and counterfactual job openings from JOLTS. Panel (b): Actual and counterfactual hires from JOLTS. Panel (c): Actual and counterfactual job openings from the Help Wanted Index. Panel (d): Cyclical component of UE job finding rates (CPS, our construction) and quit rates (JOLTS, count of quits per month per 100 employees). A regression reveals a linear coefficient of UE on quit rates of 0.985 ($R^2 = 0.77$).
Empirical Meta Study: Short-Run Employment Crowd-Out

In Spain, including spillovers in other sectors/industries such as tradables (manufacturing), 2001-8, in Spain. T.7 C.3 reports a -0.027 employment effect same factor (given first stage precision), implying the least positive multiplier). Moretti and Thulin (2013) (positive). We rescale the elasticity (and SEs) by 0.2/0.09 into a sensitivity, where FIRE [manuf. emp shares in 1990 are 0.09 [0.2] (App. Fig. A1) (most conservative study). Gathmann et al. (2018) study the local employment effect of business subsidies (capital) in Italy, 1995-2006. In T.3 C.8 shows spillover effects of subsidized tradable firms' emp. on nontradable emp. at 10-year horizon (1980, 1990, 1990-2001). Table 10 Column 1 Row 1 reports effects for nontradable emp. (Caveat: migration effects.)

Market effects of industry growth, with a shift-share instrument, in US cities for 1980-90, 1990-2000. Model 3 in T.1 C.3 presents the job multipliers for tradable on nontradables. Mian and Sufi (2014) study the local labor market effects of coal sector boom-bust cycles in the US from a 1970-89. T.6 C.1, “All Years,” “Traded sector” report the local job estimates of temporary employment subsidies (short-time work) in Italy. The indirect spillover effect (reduced-effect factor of fraction of elig. workers in LLM on incl. firm emp. growth (\(d(N_{\text{non}})/d(N_{\text{non}})\)) is reported as \(β_1^D = -0.00937\) (T.3 C.3, divided by 100); i.e. the market-level sensitivity, norm. by total emp., is \((d(N_{\text{non}})/d(N_{\text{non}})) = β^D · (N_{\text{non}}/N_{\text{tot}})\), where \(N_{\text{non}}/N_{\text{tot}} = 0.75\) (source: corresp. with authors). The market-level direct effect traced out is \(β^D \times d(N_{\text{non}}/N_{\text{tot}})\), where \(β^D = 0.284\) (T.2 C.1) is the direct firm-level effect. Subsidy eligibility (\(d(N_{\text{non}}/d(N_{\text{non}})\)). Hence, the implied market-level job-for-job crowd-out of incl. emp. in response to policy-induced direct emp. effect, \(d(N_{\text{non}})/d(N_{\text{non}}) = \left(\left[d(N_{\text{non}})/d(N_{\text{non}})\right]/[d(N_{\text{non}})/N_{\text{tot}}]\right) \times [N_{\text{non}}/N_{\text{tot}}]/N_{\text{tot}}\) is reported as \(d(N_{\text{non}})/N_{\text{tot}}\) is given by \(β^D \cdot s^1/\sqrt{s} = (-0.00397)\cdot 0.75/0.284 = -0.025\). We thank the authors for detailing this calculation. We similarly rescale the indirect effect SE (T.3 C.3) by the same factor (given first stage precision) as 0.022161 - 0.75/0.284 = 0.0037. Jofre-Monseny et al. (2018a) examine the local labor market effects (LMEs) of large plant closures in Spain, including spillovers in other sectors/industries such as tradables (manufacturing), 2001-8, in Spain. T.7 C.3 reports a -0.027 employment effect per job loss (SE 0.053) in unaffected manufacturing industries. Marchand (2012) estimates local job multipliers of the 1971-81 and 1996-2006 booms in the Canadian energy sector; T4a reports IV estimates the manuf. emp. sensitivity to energy emp. Acemoglu et al. (2016) examine the LMEs of import competition from China, from 1999 to 2007/11, in the US. The ratio of emp. effects of nonexposed to exposed tradables (T.7 C.6), implies a crowdout of -6.928 \times 10^{-5} /(-1.68) = 4.112 \times 10^{-4}. We construct clustered by state SE with an IV strategy (tradable as the dep. var., exposed tradable as endog. indep. var., instrument being the import shock). Black et al. (2005) estimate the local labor market effects of coal sector boom-bust cycles in the US from a 1970-89. T.6 C.1, “All Years,” “Traded sector” reports the local job multiplier of tradable emp. to treated mining, 0.02 (SE 0.009). Cahuc et al. (2017) study a hiring subsidy in France for small firms and low-paying jobs, 2008-9. T.4 Column 4 [T.5 last column] reports the estimates on eligible (small) [ineligible] (larger) firms as 0.138 [0.008], implying 0.008/0.138 = 0.058 crowd-out. Diff-in-Diff estimates for eligible (0.011) and ineligible (0.002) jobs (sorted by wage cutoff) in T.3 C.1 and 2 imply a second crowd-out (-in) estimate of 0.002/0.011 = 0.018. T.1 and F.3 suggest that the larger number of small eligible firms roughly makes up for their size discount, implying similar employment shares, so we interpret the percent effects as sensitivities. We provide standard error ballparks by simply rescaling the ineligible-effect SEs by 1/direct effect. 

Jofre-Monseny et al. (2018b) study the effect of quasi-ex. public emp. shifts on private sector emp. in Spain at 10-year horizons (1980, 1990, 1990-2001). Table 10 Column 1 Row 1 reports effects for nontradable emp. (Caveat: migration effects.) Cerqua and Pellegrini (2018) study the local employment effect of business subsidies (capital) in Italy, 1995-2006. In T.3 C.8 shows spillovers effects of subsidized tradable firms’ emp. on non-subsidized tradable firms. Gathmann et al. (2018) (and relatedly Berge and Schmullien (2015)) investigate local labor market effects of establishment-level emp. contractions in Germany. T.4 C.5, 7 restrict the spillover analysis to the tradable sector. The size of an average mass layoff event is 0.019 of total local emp. (T.1 P.A), and the tradable sector is on average 0.39 of total local emp. (In 36). Hence the tradable emp. shock induced is -0.019/0.39 = 0.049 (similar to the -0.045 year-effect C.7). The one-year -0.015 log emp. effects on other est.’s excl. the shrinking firm imply a -0.015/(-0.049) = -0.31 crowd-in (approx: firm has small initial emp. share). We scale the SE by the same factor. 

Moretti (2010) studies LMEs of a quasi-ex. expansion of the financial sector in Delaware, US; the shortest horizon is 1980-7. The response of directly treated FIRE industries is 0.549 (T.5 C.1), vs. 0.077 on tradable (manuf.) emp. (T.5 C.6), hence a 0.077/0.549 = 0.141 spillover (positive). We rescale the elasticity (and SEs) by 0.2/0.09 into a sensitivity, where FIRE [manuf. emp shares in 1990 are 0.09 [0.2] (App. Fig. A1) (most conservative year, implying the least positive multiplier). Moretti and Thulin (2013) replicate Moretti (2010) (described above) for Swedish regions, from 1995-2001, and 2001-7. T.8 center C reports the IV estimates for tradable emp. on other tradables (we report the least positive among the two industry variants).
Figure 4: Decomposing the Vacancy Multiplier

**One-Only Decomposition**

- Only job creation \( n \)
- Only contact rate \( f \)
- Only employment \( e \)
- Total effect

**All-But-One Decomposition**

- Constant job creation \( n \)
- Constant contact rate \( f \)
- Constant employment \( e \)
- Total effect

Notes: The figure presents impulse responses (Panel (a) and (b)) and cumulative vacancy multipliers (Panel (c) and (d)) of vacancy inflows in response to a perfectly transitory exogenous increase in the vacancy stock by 1%, for simulated time series and its components. The variables are normalized by the size of vacancy injection \( \varepsilon_1 \), which is not plotted. The left panels additionally present “one-only” inflows (that only permit one variable to move from steady state); the right panels present “all-but-one” inflows (that keep only one variable at steady state). The total effect is \((n_t + (1 - \delta)\gamma(\sigma + (1 - \sigma)\lambda f_{t-1})e_{t-1} + \varepsilon^\delta_t - \tilde{\varepsilon}^{\text{inflow}})/\varepsilon_1 \). We then decompose this total effect. The one-only decomposition features (i) the only job creation \( n \) effect \((n_t - \bar{n})/\varepsilon_1 \), (ii) the only contact rate \( f \) effect \((1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} - \tilde{f}\varepsilon^\delta_t/\varepsilon_1 \), (iii) the only employment \( e \) term, where we plot the sum of (iii.a) the mechanical employment rate effect \((1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} - \tilde{f})/\varepsilon^\delta_t \), (iii.b) the small effect of the employment change on quits through \( \sigma \) shocks \((1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} - \tilde{f})(e_{t-1} - \tilde{e})/\varepsilon^\delta_t \), as well as (iii.c) the small interaction between the two \((1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} - \tilde{f})(e_{t-1} - \tilde{e})/\varepsilon^\delta_t \).
Figure 5: Impulse Responses: The Role of Reposting and Limited Crowd-Out

New Job Creation

Vacancy Stock

Unemployment

Notes: Impulse response functions of new job creation, vacancy stock and unemployment to aggregate productivity, on-the-job search intensity and matching efficiency shocks. Y-axes measure percent deviations from steady state. The graphs arise from three model variants: the baseline model with reposting and imperfect crowd-out (green solid line), the no-incremental-reposting economy (blue dashed, where repostings are held at steady state yet the job creation cost mirrors the baseline model), and the full-crowd-out economy (red dash-dotted, where job creation costs depend on total inflows rather than new job creation, yet there is reposting).
### Supplementary Evidence on Replacement Hiring

Table A1: Establishment-level Regressions

| A. Dependent Variable: $\frac{\text{New Hires}_{et}}{\text{Emp}_{et-1}}$ |
|----------------------------------|---|---|---|---|---|---|
|                                  | (1) | (2) | (3) | (1) | (2) | (3) |
| Quits$_{et}$ - Emp$_{et-1}$      | .736 | .727 | .733 | .824 | .817 | .821 |
| Establishment FE                 | ✓   | ✓   | ✓   | ✓   | ✓   | ✓   |
| Year FE                          | ✓   |   |   | ✓   |   |   |
| Year x Industry FE               | ✓   | ✓   | ✓   | ✓   | ✓   | ✓   |
| Year x State FE                  | ✓   |   |   | ✓   |   |   |
| N                                | 24509 | 24509 | 24509 | 18015 | 18015 | 18015 |
| R$^2$                            | .64 | .64 | .64 | .66 | .67 | .67 |

| B. Dependent Variable: $\frac{\text{Job Openings}_{et}}{\text{Emp}_{et-1}}$ |
|----------------------------------|---|---|---|---|---|---|
|                                  | (1) | (2) | (3) | (1) | (2) | (3) |
| Quits$_{et}$ - Emp$_{et-1}$      | .048 | .046 | .047 | .071 | .069 | .068 |
| Establishment FE                 | ✓   | ✓   | ✓   | ✓   | ✓   | ✓   |
| Year FE                          | ✓   |   |   | ✓   |   |   |
| Year x Industry FE               | ✓   | ✓   | ✓   | ✓   | ✓   | ✓   |
| Year x State FE                  | ✓   |   |   | ✓   |   |   |
| N                                | 23209 | 23209 | 23209 | 16964 | 16964 | 16964 |
| R$^2$                            | .37 | .37 | .37 | .35 | .36 | .35 |

Notes: Regressions run at the establishment level. Standard errors reported in parenthesis and clustered around establishments. Sample restricted to West German establishments with at least 50 employees and less than 40% absolute employment change. Data are annual covering 1993-2008. Source: LIAB sample of the IAB Establishment Survey.
Table A2: Event Study: Timing of Hires and Quits

<table>
<thead>
<tr>
<th>Lead/Lag</th>
<th>All (1)</th>
<th>All (2)</th>
<th>All (3)</th>
<th>All (4)</th>
<th>Positive Quits (1)</th>
<th>Positive Quits (2)</th>
<th>Positive Quits (3)</th>
<th>Positive Quits (4)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>-.060 (0.067)</td>
<td>.016 (0.096)</td>
<td>-.008 (0.086)</td>
<td></td>
<td>.060 (0.158)</td>
<td>-.115 (0.074)</td>
<td>-.123 (0.132)</td>
<td></td>
</tr>
<tr>
<td>-2</td>
<td></td>
<td>.051 (0.057)</td>
<td>.064 (0.098)</td>
<td>.078 (0.091)</td>
<td></td>
<td>.011 (0.089)</td>
<td>.010 (0.150)</td>
<td>-0.005 (0.129)</td>
</tr>
<tr>
<td>-1</td>
<td>.736 (0.067)</td>
<td>.753 (0.068)</td>
<td>.815 (0.095)</td>
<td>.818 (0.127)</td>
<td>.824 (0.086)</td>
<td>.928 (0.097)</td>
<td>1.03 (0.140)</td>
<td>.903 (0.164)</td>
</tr>
<tr>
<td>0</td>
<td></td>
<td>.050 (0.069)</td>
<td>.079 (0.086)</td>
<td>.192 (0.104)</td>
<td></td>
<td>.030 (0.102)</td>
<td>.044 (0.136)</td>
<td>.070 (0.129)</td>
</tr>
<tr>
<td>+1</td>
<td></td>
<td></td>
<td>.086 (0.085)</td>
<td>-.055 (0.088)</td>
<td></td>
<td></td>
<td>-.001 (0.122)</td>
<td>-.258 (0.122)</td>
</tr>
<tr>
<td>+2</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>.161 (0.139)</td>
<td></td>
<td>.037 (0.226)</td>
</tr>
<tr>
<td>+3</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Establishment FE</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>Year FE</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>N</td>
<td>24509</td>
<td>11414</td>
<td>5732</td>
<td>2832</td>
<td>18015</td>
<td>6433</td>
<td>2912</td>
<td>1385</td>
</tr>
<tr>
<td>R²</td>
<td>.64</td>
<td>.67</td>
<td>.63</td>
<td>.65</td>
<td>.66</td>
<td>.64</td>
<td>.62</td>
<td>.73</td>
</tr>
</tbody>
</table>

Notes: Regressions run at the establishment level. Standard errors reported in parenthesis and clustered around establishments. Sample restricted to West German establishments with at least 50 employees and less than 40% absolute employment change. Data are annual covering 1993-2008. Source: LIAB sample of the IAB Establishment Survey.
Figure A1: Further Evidence on Quits, Hiring, Job Openings and Layoffs from Germany

Notes: Panel (a) plots the time series of breakdown of last filled job, 2000-15. The shift in the later years is perhaps due to a redesign of the survey introducing a subcategory for death/retirement-triggered replacement hiring (a smaller share, here subsumed in total long-term replacement hiring). Source: IAB Job Vacancy Survey. Panels (b) and (c) present binned scatter plots illustrating the replacement-hiring/quit sensitivity estimated using establishment–year observations in regression model in Appendix Table A1 Column (1), i.e. all variables are residualized. Panel (d) plots aggregate (average) quit, hiring, job opening and layoff rates in Germany. Panels (e) and (f) plot the establishment hires/job opening rates with respect to district (Kreis) level economic conditions, again binned scatter plots of the underlying micro observations (residualized by year and establishment fixed effects), i.e. we estimate establishment $e$’s year-$t$ worker flow outcome to the log unemp. in location $l$ (Source: Regional Database Germany (Federal Statistical Office and the Statistical Offices of the Länder)): \[
\text{Outcome}_{e,t} = \beta_0 + \beta_1 \ln(\text{Unemp}_l) + \alpha_e + \alpha_t + \epsilon_{e,t}\]
B Computational Details

B.1 Calibration

Table A3: Calibration and Model Fit of Baseline Model

(a)Calibrated Parameters and Values

<table>
<thead>
<tr>
<th>A. PREDETERMINED</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Discount factor ( \beta )</td>
<td>0.9967</td>
<td></td>
</tr>
<tr>
<td>Worker bargaining share ( \phi )</td>
<td>0.5</td>
<td></td>
</tr>
<tr>
<td>Elasticity of matching function ( \eta )</td>
<td>0.5</td>
<td></td>
</tr>
<tr>
<td>Unemployment benefit ( b )</td>
<td>0.9</td>
<td></td>
</tr>
<tr>
<td>Reposting rate ( \gamma )</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>Vacancy creation cost ( k_1 )</td>
<td>0.1</td>
<td></td>
</tr>
<tr>
<td>( k_2 )</td>
<td></td>
<td>1</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>B. ESTIMATED</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative efficiency of OJS ( \lambda )</td>
<td>0.0556</td>
<td></td>
</tr>
<tr>
<td>Scale of matching function ( \mu )</td>
<td>0.6542</td>
<td></td>
</tr>
<tr>
<td>Job destruction ( \delta )</td>
<td>0.0222</td>
<td></td>
</tr>
<tr>
<td>Match separation ( \sigma )</td>
<td>0.0051</td>
<td></td>
</tr>
<tr>
<td>Vacancy posting cost ( \kappa )</td>
<td>0.1611</td>
<td></td>
</tr>
</tbody>
</table>

(b) Target Moments and Model Fit

<table>
<thead>
<tr>
<th>Target</th>
<th>Data</th>
<th>Model</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unemployment rate</td>
<td>0.057</td>
<td>0.057</td>
<td>CPS - Shimer (2005)</td>
</tr>
<tr>
<td>Job-to-job rate</td>
<td>0.025</td>
<td>0.025</td>
<td>CPS - Fujita and Nakajima (2016)</td>
</tr>
<tr>
<td>Unemployed job finding rate</td>
<td>0.45</td>
<td>0.45</td>
<td>CPS - Shimer (2005)</td>
</tr>
<tr>
<td>Reposted vacancy share</td>
<td>0.56</td>
<td>0.56</td>
<td>IAB German Job Vacancy Survey</td>
</tr>
<tr>
<td>Job filling rate</td>
<td>0.9</td>
<td>0.9</td>
<td>Fujita and Ramey (2007)</td>
</tr>
</tbody>
</table>
B.2 Solution: Steady State

Instead of working with individual Bellman Equations for workers and firms, we work with the value of surplus from a match, which is sufficient to characterize worker decisions. This approach has the added advantage of not requiring wage levels while solving the model. We use value function iteration to solve the model. We outline the algorithm below.

1. For a given parameterization of the model, start with an initial guess of market tightness $\theta_0$.

2. For each guess of $\theta_n$ in iteration $n$:
   (a) Iterate on $S(s)$ given in Footnote 11 to solve for match surplus.
   (b) Iterate on the law of motion in equation (7) to compute the steady-state values of employment and unemployment rates.
   (c) Solve the market tightness level $\hat{\theta}_{n+1}$ that satisfies the free-entry condition in equation (14), and law of motion for vacancies in equation (8). Calculate its absolute deviation from $\theta_n$.
   (d) If the deviation is less than the tolerance level, stop. Otherwise update the guess for market tightness to $\theta_{n+1} = \omega \theta_n + (1 - \omega)\hat{\theta}_{n+1}$ with a dampening parameter $\omega < 1$.

B.3 Solution: Transition Dynamics

In this section we outline the algorithm used to solve for the transition path of the model to a one-time unanticipated shock.

1. Fix the number of time periods it takes to reach the new steady state, $T$.

2. Compute the steady state equilibrium for a given set of model parameters according to the algorithm in Section B.2. Since we are interested in transitory shocks, the new steady state at $T$ will be the same.

3. Guess a sequence of market tightness, $\{\theta^0_t\}_{t=1}^{T-1}$.

4. Solve for the sequence of match surplus, $\{S_t\}_{t=1}^{T-1}$ and vacancy values $\{V_t\}_{t=1}^{T-1}$ backwards, given path $\{\theta^0_t\}_{t=1}^{T-1}$, the shock, and the terminal values of $S_T$ and $V_T$.

5. Compute the sequence of market tightness $\{\theta^1_t\}_{t=1}^{T-1}$ consistent with the worker and vacancy laws of motion, induced by the decisions implied by $\{S_t\}_{t=1}^{T-1}$ and $\{V_t\}_{t=1}^{T-1}$.

6. Check if $\max_{1 \leq t < T} |\theta^1_t - \theta^0_t|$ is less than a predetermined tolerance level. If yes, continue, if no update $\{\theta^0_t\}_{t=1}^{T-1}$ and go back to step 3.

7. Check if $|\theta^1_T - \theta^0_T|$ is less than a predetermined tolerance level. If yes stop, if not increase $T$ and go back to step 1.
C Additional Results on Vacancy Injection Experiment

This section completes the discussion of the equilibrium multiplier from Section 4.3. In Figure A2, we present the IRFs following the vacancy injection shock. In the baseline model, labor market tightness, job finding and quits increase, hence repostings boost total vacancies, such that unemployment falls further. The smaller and shorter-lived response of the no-incremental-reposting economy clarifies the incremental amplification as well as internal propagation from the vacancy multiplier. Lastly, in the full-crowd-out economy $n$ fully neutralizes the injection.

Figure A2: Impulse Responses from Vacancy Injection

Notes: Impulse response functions of new job creation, vacancy stock and unemployment to an exogenous vacancy injection shock. Y-axes measure percent deviations from steady state. The graphs arise from three model variants: the baseline model with reposting and imperfect crowd-out (green solid line), the no-incremental-reposting economy (blue dashed, where repostings are held at steady state yet the job creation cost mirrors the baseline model), and the full-crowd-out economy (red dash-dotted, where job creation costs depend on total inflows rather than new job creation, yet there is reposting).

\[ \tilde{\nu} \]

\[ \tilde{\nu}_t = n_t + (1 - \delta)\left( (1 - (1 - \sigma)q(\theta_{t-1}))\nu_{t-1} + \gamma(\sigma + (1 - \sigma)\lambda f(\bar{\theta}))\epsilon_t + \epsilon_t^0, \right. \]

where $\epsilon_t^0 > 0$ in the first period and zero afterwards. 

---

\footnote{In the no-reposting counterfactual follows law of motion $\nu_t = n_t + (1 - \delta)\left( (1 - (1 - \sigma)q(\theta_{t-1}))\nu_{t-1} + \gamma(\sigma + (1 - \sigma)\lambda f(\bar{\theta}))\epsilon \right) + \epsilon_t^0$, where $\epsilon_t^0 > 0$ in the first period and zero afterwards.}
D Extended Model: Match Heterogeneity and Endogenous Search

Our extension endogenizes on-the-job search and rationalizes it with heterogeneity in match disamenities. The modified model can be solved similarly using the algorithm in B.2, and IRFs can be generated using the algorithm in B.3. Once calibrated to realistic quit levels and cyclicality, it behaves very similarly to our parsimonious model presented in the main text.

Structure of Extended Model  Let $\xi \in [\xi, \bar{\xi}]$ denote match disamenity. New jobs start from the lowest disamenity, which then evolves following first order Markov chain $P(\xi'|\xi)$. Hence all new jobs are accepted, and the disamenity distribution over existing matches does not enter the free-entry condition. Workers choose search effort $s$ subject to convex cost $c(s)$. The worker and firm problems then become:

$$U(s) = \max_{s_U \geq 0} \left\{ b - c(s_U) + (1 - \delta)(1 - \sigma)s_U f(\theta)\mathbb{E}[W(\xi, s')] + (1 - (1 - \delta)(1 - \sigma)s_U f(\theta)\mathbb{E}[U(s')]] \right\}$$

$$W(\xi, s) = \max_{s_E \geq 0} \left\{ w(\xi, s) - \xi - c(s_E) + \beta(1 - \delta)(1 - \sigma)\mathbb{E}[W(\xi', s')] + \beta(1 - \delta)\mathbb{E}[U(s')] \right\}$$

$$V(s) = -\kappa + \beta (1 - \delta) \left\{ q(\theta) - (1 - \sigma)\mathbb{E}[W(\xi, s') | J(\xi, s')] + (1 - q(\theta)(1 - \sigma))\mathbb{E}[V(s')] \right\}$$

$$J(\xi, s) = y - w(\xi, s) + \beta (1 - \delta) \left\{ \gamma s_E^* f(\theta)\mathbb{E}[V(s')] + \gamma(1 - s_E^*) f(\theta)\mathbb{E}[V(\xi', s')] \right\}$$

With heterogeneity in matches, we need to keep track of the worker distribution. Accordingly, the laws of motion for vacancies, unemployment and employment now become

$$v_t = n_t + (1 - \delta)(1 - (1 - \sigma)q(\theta_{t-1}))v_{t-1} + \gamma\left( \lambda f(\theta_{t-1}) \int \bar{\xi} \delta \xi - (\bar{\xi} - \xi)c_{t-1}(\bar{\xi})d\bar{\xi} \right)$$

$$+ \int \left( \sigma + (1 - \sigma)P(\xi > \xi c | \bar{\xi}) \right) (1 - \lambda f(\theta_{t-1})s_E(\bar{\xi}))e_{t-1}(\bar{\xi})d\bar{\xi} \right)$$

$$u_t = (1 - (1 - \delta)(1 - \sigma)\delta(\theta_{t-1}))u_{t-1} + (1 - u_{t-1})$$

$$+ (1 - \delta)(1 - \sigma)\int P(\xi > \xi c | \bar{\xi})(1 - \lambda f(\theta_{t-1})s_E(\bar{\xi}))e_{t-1}(\bar{\xi})d\bar{\xi} + (1 - \delta)\sigma(1 - u_{t-1})$$

$$e_t(\xi) = (1 - \delta)(1 - \sigma)\int P(\xi|\bar{\xi})(1 - \lambda f(\theta_{t-1})s_E(\bar{\xi}))e_{t-1}(\bar{\xi})d\bar{\xi} \forall \xi \neq \bar{\xi}$$

And $\xi < \xi c$

$$e_t(\xi) = (1 - \delta)(1 - \sigma)\int P(\xi|\bar{\xi})(1 - \lambda f(\theta_{t-1})s_E(\bar{\xi}))e_{t-1}(\bar{\xi})d\bar{\xi} + s_E f(\theta_{t-1})u_{t-1} + \lambda f(\theta_{t-1})\int s_E(\bar{\xi})e_{t-1}(\bar{\xi})d\bar{\xi}$$

$$e_t(\xi) = 0 \forall \xi > \xi c$$

where $\xi c(s)$ denotes the endogenous separation cutoff implicitly defined by $W(\xi c, s) = U(s)$. 32
Calibration of Extended Model  

We now provide one specific version of the more general model above to show that the extended model implies a similar amplification role of the replacement hiring channel (conditional on matching similar targets). The calibration strategy is analogous to the baseline except for the process that governs transitions between job types and endogenous on the job search, features we elaborate on below.

To maximize intuition and to economize on free parameters, we assume that there are two match types: good and bad jobs. We set disutility from working in a good job to $\xi = 0$ and in a bad job to $\bar{\xi} = 0.1$. As we focus on EE mobility, we ensure that this drop does not merit endogenous separations into unemployment at any point in our transitions. All jobs (whether formed out of unemployment or employment) start off as a good type. A distinct feature of this economy is therefore the evolution of the stock of searchers (in bad jobs), which follows a law of motion, whereas our baseline model has a constant fraction of employed searchers. Each period, the Markov process $P(\xi|\bar{\xi})$ has good jobs downgrade to a bad type with probability $p_D$; bad jobs upgrade to the good quality with probability $p_U$. To jointly identify $(p_D, p_U)$, we target a steady state on-the-job seeker share of 0.23, a number we take from Faberman et al. (2018) as the fraction of employed workers that report to be actively searching for another job – in our model the share of employed workers in the bad job type. We pin down the split between upgrades and downgrades (which can be thought of inflow and outflow probabilities into the bad state, where on-the-job search provides a second outflow margin) by targeting the elasticity of the EE quit rate to the UE job finding rate, depicted in Figure 2 Panel (d), and discussed in the main text in Section 3. This target ensures that our model exhibits a realistic quit cyclicality, as well as remains comparable to the baseline model (which we constructed to match the near-unit elasticity between quits and UE rates from the data.)

We further assume that the cost function for job search effort is quadratic $c(s) = 0.5s^2$. (We have also experimented with other functional form choices but prefer the quadratic setup, by which the level of optimal search effort is transparently related to its benefits.) We finally choose $k_2$ to yield a comparable crowd-out in this economy compared to the baseline economy of $-0.1183$, which implies $k_2 = 2.85$. We set $b = 0.7$ (but note that the comparison to the baseline model is limited due to the additional job search costs and job qualities).

Table A4 summarizes model parameters under this calibration and the extended model’s fit. We underpredict the elasticity of EE quit to UE rates, implying that the extended model will understate replacement hiring compared to the baseline model.\(^4\)

In response to our aggregate shocks, the extended model exhibits again strong amplification from the vacancy chain, mirroring our discussion in Section 4.4.

---

\(^2\)Intuitively, more “churn” between job types related to the Markov process will attenuate the elasticity of the stock of the bad jobs to shifts in EE (which otherwise would unrealistically attenuate the elasticity of EE to UE rates, one of our targets).

\(^3\)We again focus on relative/differential amplification, as to net out the inherent attenuation from the adjustment cost nature of $k_2$.

\(^4\)Permitting differential job search costs might be another lever to increase the quit/UE elasticity.
Table A4: Calibration and Model Fit: Extended Model

(a) Calibrated Parameters and Values

<table>
<thead>
<tr>
<th>A. PREDETERMINED</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Discount factor</td>
<td>$\beta$</td>
<td>0.9967</td>
</tr>
<tr>
<td>Worker bargaining share</td>
<td>$\phi$</td>
<td>0.5</td>
</tr>
<tr>
<td>Elasticity of matching function</td>
<td>$\eta$</td>
<td>0.5</td>
</tr>
<tr>
<td>Unemployment benefit</td>
<td>$b$</td>
<td>0.7</td>
</tr>
<tr>
<td>Reposting rate</td>
<td>$\gamma$</td>
<td>1</td>
</tr>
<tr>
<td>Vacancy creation cost</td>
<td>$k_1$</td>
<td>0.1</td>
</tr>
<tr>
<td></td>
<td>$k_2$</td>
<td>2.85</td>
</tr>
<tr>
<td>Disutility of work in good job</td>
<td>$\xi$</td>
<td>0</td>
</tr>
<tr>
<td>Disutility of work in bad job</td>
<td>$\xi$</td>
<td>0.1</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>B. ESTIMATED</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative efficiency of OJS</td>
<td>$\lambda$</td>
<td>1.14</td>
</tr>
<tr>
<td>Scale of matching function</td>
<td>$\mu$</td>
<td>0.8188</td>
</tr>
<tr>
<td>Job destruction</td>
<td>$\delta$</td>
<td>0.0221</td>
</tr>
<tr>
<td>Match separation</td>
<td>$\sigma$</td>
<td>0.0046</td>
</tr>
<tr>
<td>Vacancy posting cost</td>
<td>$\kappa$</td>
<td>0.8</td>
</tr>
<tr>
<td>Probability of downgrading to bad job</td>
<td>$p_D$</td>
<td>0.1248</td>
</tr>
<tr>
<td>Probability of upgrading to good job</td>
<td>$p_U$</td>
<td>0.3159</td>
</tr>
</tbody>
</table>

(b) Target Moments and Model Fit

<table>
<thead>
<tr>
<th>Target</th>
<th>Data</th>
<th>Model</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unemployment rate</td>
<td>0.057</td>
<td>0.0567</td>
<td>CPS - Shimer (2005)</td>
</tr>
<tr>
<td>Job-to-job rate</td>
<td>0.025</td>
<td>0.0252</td>
<td>CPS - Fujita and Nakajima (2016)</td>
</tr>
<tr>
<td>Unemployed job finding rate</td>
<td>0.45</td>
<td>0.4425</td>
<td>CPS - Shimer (2005)</td>
</tr>
<tr>
<td>Reposted vacancy share</td>
<td>0.56</td>
<td>0.56</td>
<td>IAB German Job Vacancy Survey</td>
</tr>
<tr>
<td>Job filling rate</td>
<td>0.90</td>
<td>0.90</td>
<td>Fujita and Ramey (2007)</td>
</tr>
<tr>
<td>Share of employed actively searching</td>
<td>0.23</td>
<td>0.2265</td>
<td>Faberman et al. (2018)</td>
</tr>
<tr>
<td>Elasticity of EE w.r.t UE rate</td>
<td>1</td>
<td>0.9378</td>
<td>CPS and JOLTS</td>
</tr>
</tbody>
</table>
Figure A3: Impulse Responses: Extended Model

Notes: Impulse response functions of new job creation, vacancy stock and unemployment to aggregate productivity, on-the-job search intensity and matching efficiency shocks. Y-axes measure percent deviations from steady state. The graphs arise from three model variants: the full model with reposting and imperfect crowd-out (green solid line), the no-incremental-reposting economy (blue dashed, where repostings are held at steady state yet the job creation cost mirrors the baseline model), and the full-crowd-out economy (red dash-dotted, where job creation costs depend on total inflows rather than new job creation, yet there is reposting).
E  Low Crowd-Out Economy

Figure A4: Decomposing the Vacancy Multiplier: Low-Crowd-Out Economy

Notes: The figure presents impulse responses (Panel (a) and (b)) and cumulative vacancy multiplier (Panel (c) and (d)) of vacancy inflows in response to a perfectly transitory exogenous increase in the vacancy stock by 1%, for simulated time series and its components. The variables are normalized by the size of vacancy injection $\epsilon_{1}^0$, which is not plotted. The left panels additionally present “one-only” inflows (that only permit one variable to move from steady state); the right panels present “all-but-one” inflows (that keep only one variable at steady state). The total effect is $(n_t + (1 - \delta)\gamma(\sigma + (1 - \sigma)\lambda f_{t-1})e_{t-1} + \epsilon_{1}^0 - \bar{\epsilon}_{\text{Inflow}})/\epsilon_{1}^0$. We then decompose this total effect. The one-only decomposition features (i) the only job creation $n$ effect $(n_t - \bar{n})/\epsilon_{1}^0$, (ii) the only contact rate $f$ effect $(1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} \bar{f} - \bar{\epsilon}_{\text{Inflow}})/\epsilon_{1}^0$, (iii) the only employment $e$ term, where we plot the sum of (iii.a) the mechanical employment rate effect $(1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} \bar{f} (e_{t-1} - \bar{\epsilon})/\epsilon_{1}^0$, (iii.b) the small effect of the employment change on quits through $\sigma$ shocks $(1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} \bar{f} (e_{t-1} - \bar{\epsilon})/\epsilon_{1}^0$, as well as (iii.c) the small interaction between the two $(1 - \delta)\gamma(1 - \sigma)\lambda f_{t-1} \bar{f} (e_{t-1} - \bar{\epsilon})/\epsilon_{1}^0$. 

36
Figure A5: Impulse Responses: Low-Crowd-Out Economy

**Notes:** Impulse response functions of new job creation, vacancy stock and unemployment to aggregate productivity, on-the-job search intensity and matching efficiency shocks. Y-axes measure percent deviations from steady state. The graphs arise from three model variants: the *full* model with reposting and imperfect crowd-out (green solid line), the *no-incremental-reposting* economy (blue dashed, where repostings are held at steady state yet the job creation cost mirrors the baseline model), and the *full-crowd-out* economy (red dash-dotted, where job creation costs depend on total inflows rather than new job creation, yet there is reposting).