

**Economics 136**  
**Problem Set #4**

(Due in Lecture Tuesday, March 21)

1. Draw payoffs of following combinations of options. All the options have the same expiration date.
  - (a) Buying a call and a put with the same strike price.
  - (b) Buying a call and two puts with the same strike (this is called a *strip*).
  - (c) Buying a put with a strike price,  $X_1$ , and a call with a strike price,  $X_2$ , where  $X_1 < X_2$  (called a *strangle*).
  - (d) Buying a call with a strike price,  $X_1$ , a call with a strike price,  $X_3$ , and selling two calls with a strike price,  $X_2$ , where  $X_1 < X_2 < X_3$  and  $X_3 - X_2 = X_2 - X_1$  (a *butterfly spread*).
  
2. ACME Corp. stock currently trades at \$25 a share. Next year it will either trade at \$35 or \$15. The stock will pay no dividends, and the risk-free one-year interest rate is 10%.
  - (a) What is the price of a European Call option with a strike price of \$25? If the strike price were \$0 instead, how would that change your answer. Explain.
  - (b) Redo part (a) for a put option.
  - (c) Suppose the stock will be worth either \$40 or \$10 next year. What would be the price of a call option with a strike price of \$25. Explain intuitively.
  - (d) Redo part (c) with a risk-free rate of 15%. Explain your result intuitively.

3. You have been looking at buying stock in the newspaper company – The Daily Granite. By studying it you have ascertained that the payoffs and probabilities of those payoffs next year will be:

State	Probabilities	Price of Daily Granite stock tomorrow
1	1/5	\$120
2	1/5	\$110
3	1/5	\$100
4	1/5	\$90
5	1/5	\$80

You have the opportunity today to buy a call or put option on Daily Granite stock with a strike price of \$110.

- What are the payoffs for the call option in each state.
  - What are the payoffs for the put option in each state.
  - Graph the payoffs for each option (price of stock on x-axis and payoff of option on the y-axis)
  - Using payoffs of a stock, a call and a put from above, show how you can make a risk-free portfolio.
4. The current price of one share Widgets U.S.A. stock is \$50. It's expected that Widgets will have a return of %10 and a standard deviation of 60% over the next year. The risk-free rate is 5%. :
- Use the Black-Scholes formula (consult section 21.4 of BKM) to calculate the price of a call option on Widgets stock with an exercise price of \$60 expiring in one year.
  - Redo part (a) for a similar option that expires in two years. Explain your result intuitively.
  - Redo part (a) for a put option with the same terms.