

# Economics 101A

## (Lecture 22)

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## Outline

1. Price Discrimination II
2. Oligopoly?
3. Game Theory
4. Oligopoly: Cournot

# 1 Price Discrimination II

## 1.1 Segmented markets

- Profit maximization problem:

$$\max_{y_A, y_B} p_A(y_A) y_A + p_B(y_B) y_B - c(y_A + y_B)$$

- First order conditions:
  
  
  
  
  
  
  
  
  
  
- Elasticity interpretation
  
  
  
  
  
  
  
  
  
  
- Firm charges more to markets with lower elasticity

- Examples:
  - student discounts
  
  - prices of goods across countries:
    - \* airlines (US and Europe)
    - \* books (US and UK)
    - \* cars (Europe)
    - \* drugs (US vs. Canada vs. Africa)
  
- As markets integrate (Internet), less possible to do the latter.

## 2 Oligopoly?

- Extremes:
  - Perfect competition
  - Monopoly
- Oligopoly if there are  $n$  (two, five...) firms
- Examples:
  - soft drinks: Coke, Pepsi;
  - cellular phones: Sprint, AT&T, Cingular,...
  - car dealers

- Firm  $i$  maximizes:

$$\max_{y_i} p(y_i + y_{-i}) y_i - c(y_i)$$

where  $y_{-i} = \sum_{j \neq i} y_j$ .

- First order condition with respect to  $y_i$ :

$$p'_Y(y_i + y_{-i}) y_i + p - c'_y(y_i) = 0.$$

- Problem: what is the value of  $y_{-i}$ ?
  - simultaneous determination?
  - can firms  $-i$  observe  $y_i$ ?
- Need to study strategic interaction

### 3 Game Theory

- Nicholson, Ch. 15, pp. 440–449 [OLD: Ch. 10, pp. 246–255].
- Unfortunate name
- Game theory: study of decisions when payoff of player  $i$  depends on actions of player  $j$ .
- Brief history:
  - von Neuman and Morgenstern, Theory of Games and Economic Behavior (1944)
  - Nash, Non-cooperative Games (1951)
  - ...
  - Nobel Prize to Nash, Harsanyi (Berkeley), Selten (1994)

- Definitions:

- Players:  $1, \dots, I$

- Strategy  $s_i \in S_i$

- Payoffs:  $U_i(s_i, s_{-i})$



- Example: Prisoner's Dilemma

- $I = 2$

- $s_i = \{D, ND\}$

- Payoffs matrix:

$1 \setminus 2$	$D$	$ND$
$D$	$-4, -4$	$-1, -5$
$ND$	$-5, -1$	$-2, -2$

- What prediction?
- Maximize sum of payoffs?
- Choose dominant strategies
- **Equilibrium in dominant strategies**
- Strategies  $s^* = (s_i^*, s_{-i}^*)$  are an Equilibrium in dominant strategies if

$$U_i(s_i^*, s_{-i}) \geq U_i(s_i, s_{-i})$$

for all  $s_i \in S_i$ , for all  $s_{-i} \in S_{-i}$  and all  $i = 1, \dots, I$

- Battle of the Sexes game:

He \ She	Ballet	Football
Ballet	2, 1	0, 0
Football	0, 0	1, 2

- Choose dominant strategies? Do not exist

- **Nash Equilibrium.**

- Strategies  $s^* = (s_i^*, s_{-i}^*)$  are a Nash Equilibrium if

$$U_i(s_i^*, s_{-i}^*) \geq U_i(s_i, s_{-i}^*)$$

for all  $s_i \in S_i$  and  $i = 1, \dots, I$

- Is Nash Equilibrium unique?

- Does it always exist?

- Penalty kick in soccer (matching pennies)

Kicker \ Goalie	L	R
L	0, 1	1, 0
R	1, 0	0, 1

- Equilibrium always exists in mixed strategies  $\sigma$

- Mixed strategy: allow for probability distribution.

- Back to penalty kick:

- Kicker kicks left with probability  $k$
- Goalie kicks left with probability  $g$

- utility for kicker of playing  $L$  :

$$\begin{aligned}U_K(L, \sigma) &= gU_K(L, L) + (1 - g)U_K(L, R) \\ &= (1 - g)\end{aligned}$$

- utility for kicker of playing  $R$  :

$$\begin{aligned}U_K(R, \sigma) &= gU_K(R, L) + (1 - g)U_K(R, R) \\ &= g\end{aligned}$$

- Optimum?

- $L \succ R$  if  $1 - g > g$  or  $g < 1/2$

- $R \succ L$  if  $1 - g < g$  or  $g > 1/2$

- $L \sim R$  if  $1 - g = g$  or  $g = 1/2$

- Plot best response for kicker

- Plot best response for goalie

- Nash Equilibrium is:
  - fixed point of best response correspondence
  - crossing of best response correspondences

## 4 Oligopoly: Cournot

- Nicholson, Ch. 14, pp. 418–419, 421–422 [OLD: p. 531, 534–535].
- Back to oligopoly maximization problem
- Assume 2 firms, cost  $c_i(y_i) = cy_i$ ,  $i = 1, 2$
- Firms choose simultaneously quantity  $y_i$
- Firm  $i$  maximizes:

$$\max_{y_i} p(y_i + y_{-i}) y_i - cy_i.$$

- First order condition with respect to  $y_i$ :

$$p'_Y(y_i^* + y_{-i}^*) y_i^* + p - c = 0, \quad i = 1, 2.$$



- Nash equilibrium:
  - $y_1$  optimal given  $y_2$ ;
  - $y_2$  optimal given  $y_1$ .

- Solve equations:

$$p'_Y (y_1^* + y_2^*) y_1^* + p - c = 0 \text{ and}$$

$$p'_Y (y_2^* + y_1^*) y_2^* + p - c = 0.$$

- Cournot -> Pricing above marginal cost

## 5 Next lecture

- Oligopoly: Bertrand
- Dynamic games
- Stackelberg duopoly
- Auctions